

# Missouri Department of Transportation Bridge Division

**Bridge Design Manual** 

Section 6.1

Revised 04/27/2010

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# 1- Seismic Analysis & Design Specifications

Seismic design of bridges shall conform to AASHTO Division I-A, 1996 and Interims thru 1998. (Refer also to the 1998 Commentary for Division I-A.) Seismic retrofitting of existing bridges shall conform to the Seismic Retrofitting Manual for Highway Bridges, FHWA-RD-94-052, May 1995. Seismic isolation systems shall conform to AASHTO Guide Specifications for Seismic Isolation Design, 1999.

#### Applicability of Guidelines

#### AASHTO Div. I-A, 3.1

This section supplements the above documentation and does not apply to culverts, movable bridges, bridges with spans greater than 500 feet, suspension bridges, cable-stayed bridges, or arch-type bridges. There are special considerations for single-span bridges, temporary bridges and bridges with stage construction.

#### AASHTO Div. I-A, 3.11 and 3.12

#### Seismic Design Philosophy

Bridges may suffer damage but should have a low probability of collapse. Hazard to human life should be minimized, and essential bridges should continue to function after an earthquake. Bridges are designed for good ductility and displacement control and are allowed to suffer minor, acceptable damage in order to prevent major, unacceptable damage.

#### AASHTO Div. I-A, 3.6

#### Seismic Design Force Concepts

As shown in Figure 6.1.1-1(a), a two span bridge can be modeled as a single –degree-of-freedom lumped-mass system (Figure 6.1.1-1(b)). For a single-degree-of-freedom lumped-mass system, the total elastic seismic design force is equal to

$$F = m \times c_s \times g$$

where:

m is the total structural mass

cs is the elastic seismic response coefficient

g is the gravitational acceleration constant

The elastic seismic response coefficient is given by the dimensionless formula

#### AASHTO Div. I-A, Equation 3-1

$$C_s = \frac{1.2AS}{T^{0.67}}$$

where

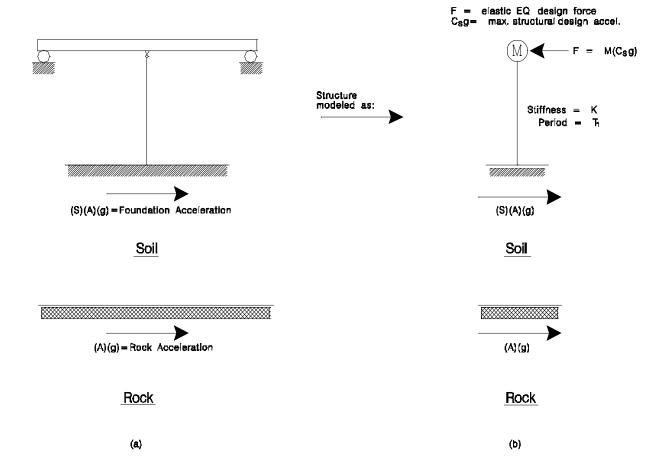
A = the acceleration coefficient on rock from AASHTO Division I-A, Article 3.2; the acceleration coefficients for Missouri are shown in Figure 6.1.1-2.

S = the dimensionless coefficient for the soil profile characteristics of the site as given in *Article 3.5.* S = 1.0, 1.2, 1.5, and 2.0 for soil profile type I, II, III, and IV respectively.

T = the fundamental period of the bridge,

$$T = 2\pi \sqrt{\frac{m}{k}}$$

where: k is the structural lateral stiffness m is the structural mass



<u>Figure 6.1.1-1</u> <u>Single-Degree-of-Freedom Lumped-Mass System</u> (a) Two-Span Bridge: (b) Bridge Structural Model

The elastic design acceleration spectra shown in Figure 6.1.1-3 is a plot of structural period  $\mathbf{T}$  versus the maximum acceleration quantity of the structure. For example: a bridge with the foundation period  $\mathbf{T}_1$  is subjected to an earthquake having a rock acceleration of  $A \times g$ . The maximum

acceleration of this bridge during the whole seismic excitation will be  $C_{\rm S1} \times g$  (See Figure 6.1.1-3).

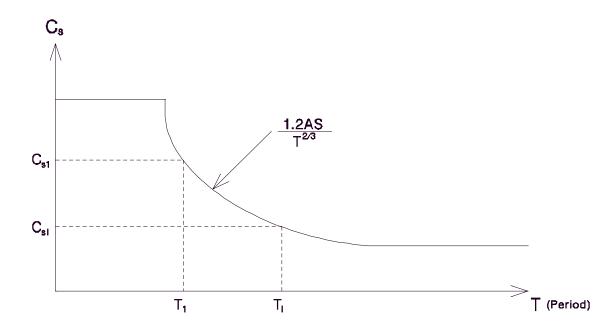


Figure 6.1.1-3
Elastic Design Acceleration Spectrum

From Figure 6.1.1-1, it can be seen that the acceleration of soil is larger than the acceleration of rock by an amplification factor **S**. Soil type is important to the evaluation of ground acceleration. From Figures 6.1.1-1 and 6.1.1-3, stated briefly, the design acceleration spectrum is a plot of the maximum acceleration to a specified seismic load for all possible single degree-of-freedom systems.

Using the above mentioned concept, AASHTO considers four analysis procedures to calculate elastic earthquake design force for the *Multiple Degree of Freedom (MDOF) System* in order of increasing complexity. Theses are:

Procedure 1 – Uniform Load Method

Procedure 2 – Single-Mode Spectral Method

Procedure 3 – Multi-Mode Spectral Method

Procedure 4 – Time History Method

MoDOT practice is to use the Multi-Mode Method for all bridges, because the Uniform Load and Single-Mode Methods are inadequate for irregular bridges and the Time History Method requires an excessive level of numerical integration time and time history records being used. A seismic structural analysis program, such as SEISAB, performs a linear elastic multi-mode response spectrum analysis, accounting also for inertial effects, damping,

**SD001** 

#### Seismic Analysis & Design Specifications

and modal combination, and determines seismic forces and displacements at individual joints and members.

In the *Multi-mode Spectral Method*, the seismic deign force,  $\mathbf{P}$ , of a specific structural component can be calculated by taking the square root of the sum of the squares (*SRSS*) or the complete quadratic combination (*CQC*) of the design for  $\mathbf{P}_i$  corresponding to the  $i^{th}$  mode of the structural component.

SRSS approach: 
$$P=\sqrt{\prod_{i=1}^{n}(P_i)^2}$$
 CQC approach: 
$$P=\sqrt{\prod_{i=1}^{n}P_i\alpha_{ij}P_j}; i,j,=1,n$$
 where:

$$\alpha_{ij} = \frac{8\rho^2 (1+q)q^{3/2}}{(1-q^2)^2 + 4\rho^2 q(1+q)^2}$$
 and  $q = \frac{w_j}{w_i}$ 

where n = the total number of modes of structure considered,  $P_i$  is calculated according to seismic design force  $F_i$  which is the design force corresponding to the structural  $i^{th}$  mode with fundamental period of  $T_i$  and seismic response coefficient of  $C_{si}$ ,  $P_i$  and  $F_i$  represent internal force of individual structural component and external seismic force applied to the structure respectively,  $P_j$  is similar to  $P_i$ ,  $\alpha_{ij}$  is the cross-correlation coefficient indicating the cross-correlation between modes i and j,  $w_i$  is the natural frequencies corresponding to the  $i^{th}$  mode and  $\rho$  is the damping ratio (i.e. 0.05). For more detailed descriptions of procedures 1, 2, 3, and 4, see AASHTO Division I-A 4.3-4.6 and for a more detailed description of how to calculate  $P_i$  and  $F_i$ , see AASHTO Division I-A Commentary C.4.5.4.

For Seismic Performance Category (SPC) **A**, the above mentioned analysis procedure is not required.

For a **regular** bridge in SPC **B**, **C**, or **D**, procedure 1 and 2 are the minimum required analysis methods, procedure 3 is strongly recommended. A **regular** bridge, as described in AASHTO *Division I-A, 4.2* has less than seven spans, no abrupt changes in weight, stiffness, or geometry and no large change in these parameters from span to span, or support to support (abutments excluded). Any bridge not satisfying the definition of a **regular** bridge is considered to be **irregular**. For an **irregular** bridge, procedure 3 must be used. The designer may use procedure 4 in place of procedure 3 if so desired.

Multi-mode spectral analysis is recommended for most bridges. Time History analysis is generally not recommended because its application requires considerable engineering judgement and experience.

New: April 2000



Figure 6.1.1-2 Seismic Map

# Seismic Performance Category (SPC), Acceleration Coefficient (A)

#### AASHTO Div. I-A, 3.2-3.4, and foldout map (Figure 1.5) at back of Division I-A

Missouri is divided into four Seismic Performance Categories (SPC A, B, C and D, see Figure 6.1.1-2), based on Acceleration Coefficients (A). The map for SPC and rock acceleration A is based on a 90% probability that the horizontal rock acceleration will not be exceeded in the 50-year lifetime of the bridge, corresponding to a return period of 475 years. For Missouri, the maximum A=0.36. For bridges with A > 0.29, an additional factor called Importance Classification (IC) is used to distinguish between SPC C and D.

#### Elastic and Plastic Design

#### AASHTO Div. I-A, 3.7

In some cases, bridges can resist seismic forces elastically, that is, without permanent deformations. In other cases, it is not economical to design a bridge for elastic behavior under seismic loading, so the bridge may be designed for inelastic (plastic) behavior. However, plastic design requires careful detailing to ensure ductility and connections with higher energy absorption characteristics. Plastic behavior is nonlinear, but AASHTO Division I-A allows an approximate analysis procedure using a linear elastic analysis along with the application of a response modification factor (R) to account for the assumed level of ductility and redundancy. This allows the use of linear elastic analysis programs such as SEISAB (or any other seismic analysis program). Response modification factors are specified in AASHTO 1-A, Article 3.7. An example of ductility demand is described below:

In an elastic seismic analysis, a column in a multiple-column bent is subjected to an elastic moment,  $M_e$ , and a rotation,  $\theta_{\text{max}}$  at the bottom of the column. The dashed line in Figure 6.1.1-4 represents the elastic moment demand. If plastic behavior is allowed and a maximum ductility factor,  $\mu$ , equal to 5 is used, then  $\mu = \frac{\theta_{\text{max}}}{\theta_p} = 5$ . The column is then sized so that its plastic moment capacity,  $M_p$ , is greater than or equal to the modified elastic moment,  $M_{\text{ME}}$ , such that  $M_{\text{ME}} = \frac{M_e}{(R=5)}$ . This is based on the assumption that the deformations produced by a given seismic input force, F, are essentially the same for both elastic column behavior and for column yielding behavior at a ductility demand of  $\mu=5$ . Response modification factors (R) are allowed because of component ductility capacity and because of redundancy provided by adjacent columns, piers, and abutments.

AASHTO Div. I-A, 1992 Commentary C3.6

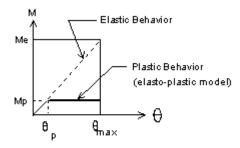


FIGURE 6.1.1-4: Moment Ductility Demand on a Column

 $\theta_{
m max}$  = rotation at bottom of column (elastic or plastic)  $\theta_{
m p} \ = \ \frac{\theta_{
m max}}{\mu}$   $M_{_{\it e}} \cong 5 \! \times \! M_{_{\it p}}$ 

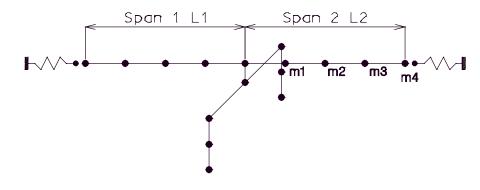
#### Structural Analysis Model

The bridge is usually modeled using idealized linear elements, connection nodes and lumped masses. The lumped masses are placed throughout the structure (see Figure 6.1.1-5) to model the mass distribution (a mass matrix, [M]). Structural stiffness is approximated using linear springs for substructures (a stiffness matrix, [K]). A coefficient of damping is selected for the overall system (usually 5%, represented by a damping matrix, [C]). The displacements, velocities and accelerations of the system are represented by  $\{x(t)\}$ ,  $\{\dot{x}(t)\}$  and  $\{\ddot{x}(t)\}$  vectors in the structural dynamic analysis equation as shown below:

$$[M]\{\ddot{x}(t)\} + [C]\{\dot{x}(t)\} + [K]\{x(t)\} = \{F_{eq}\} \qquad \text{eq.(1)}$$
 in which:

 $\{F_{eq}\}$  is the seismic induced force vector

The development of multi-mode response spectrum analysis is based on the above dynamic equation.



where: m1 ~ m4 = Lumped Masses m1 = 1/4M2 m2 = 1/4M2 m3 = 1/4M2 m4 = 1/8M2

where **M2** = total mass of span 2

Figure 6.1.1-5 Lumped Mass Model of a General Bridge

#### **Directional Load Cases**

The AASHTO Div. I-A specifications specify two major load cases to provide for combinations of longitudinal and transverse seismic forces:

Case I = L + 0.3\*T (This is loading case 3 in SEISAB.) Case II = 0.3\*L + T (This is loading case 4 in SEISAB.)

#### AASHTO Div. I-A, 3.9

#### **Group Loading**

The group loading includes dead load (D), earth pressure (E) and seismic (EQ) loads, and other possible loadings such as buoyancy (B) and stream flow pressure (SF). Thus:

Group Load = 1.0\*(D+B+SF+E+EQ),

# AASHTO Div. I-A, 6.2 and 7.2

This is to be considered as a Load Factor group loading, but it may also be considered as a Service Load if the allowable overstresses in Division I-A are used. Wind and temperature loads are not included in this group and need not be applied simultaneously with seismic loads.

# Seismic Performance Category Specifications

#### AASHTO Div. I-A, Sections 5, 6 and 7

Each Seismic Performance Category has its own seismic specifications. All categories require minimum support lengths at expansion gaps and adequate connections between superstructure and substructure. Categories B, C and D have additional specifications concerning foundations, abutments, special pile requirements, column design and footing design. See AASHTO Division I-A for details of specifications.

# 2.1 - Flowchart of Seismic Analysis Procedure

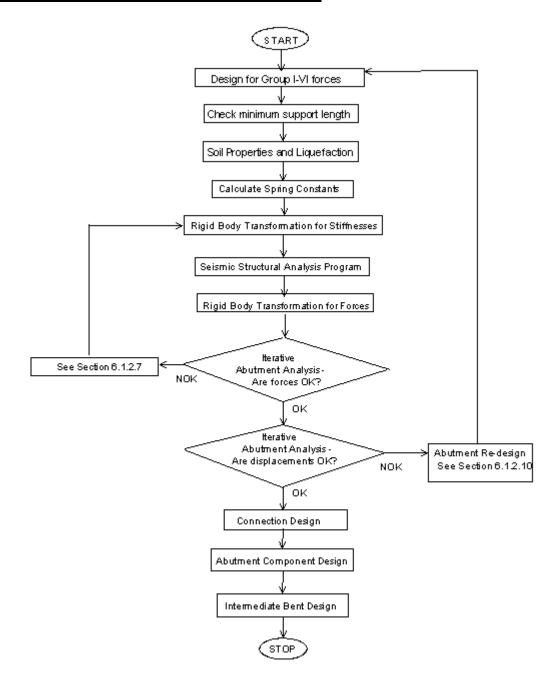


Figure 6.1.2.1-1

# 2.2 - Checklist for Seismic Computations

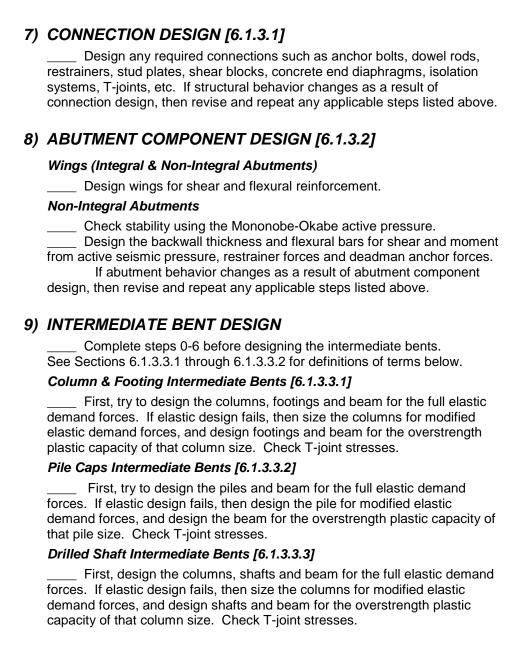
See the flowchart, Figure 6.1.2.1-1, in Section 6.1.2.1 or the corresponding section of the Bridge Manual. Section references below are in brackets [].

GROUP I-VI DESIGN
The bridge should have already been designed for Group I-VI loads. If expansion gaps are present, check seismic support lengths [6.1.2.3].
SOIL PROPERTIES
Determine the soil properties at each bent as a function of depth at each bent [6.1.2.4].
Check the factor of safety against liquefaction [6.1.2.5], for all layers of soil that might liquefy, before determining all spring constants.
STIFFNESSES
Determine the stiffnesses at applicable piles, footings and abutments using the approved stiffness methods [6.1.2.6].
RIGID BODY TRANSFORMATION (Stiffnesses)
Use RBT to compute the equivalent master joint stiffness matrix at abutments and pile footings [6.1.2.7].
SEISMIC STRUCTURAL ANALYSIS PROGRAM
Prepare the input for the SEISAB, SAP2000 or any seismic analysis program, and run the program to perform a seismic analysis.
RIGID BODY TRANSFORMATION (Forces)
Use RBT and the master joint's force output from the Seismic Structural Analysis Program to compute the individual element forces at the original local slave joints [6.1.2.7].
ITERATIVE ABUTMENT ANALYSIS
Check soil pressures and pile stresses against allowables as described in the iterative abutment analysis flowchart [6.1.2.10]. If necessary, either perform remedial actions or reduce the spring constants and iterate until pressures and stresses are within allowable limits.  When abutment element forces are OK, check resultant abutment displacement against the allowable. If the displacement is excessive, perform remedial actions and iterate until displacements are within allowable limits [6.1.2.10].

# Seismic Design - Section 6.1

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Seismic Analysis Model



# 2.3 - Minimum Support Length

At expansion gaps (near abutments, intermediate bents and hinges), the substructure must accommodate differential seismic displacements between the substructure and the superstructure. The minimum support length capacity, N(c), of the substructure beam shall meet or exceed the minimum support length demand, N(d), of the superstructure girders.

$$N(c) > = N(d)$$

At fixed bents, minimum support length need not be calculated.

AASHTO Div. I-A, 3.10 AASHTO Div. I-A, 5.3, 6.3, 7.3

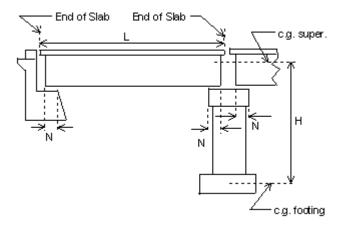


Figure 6.1.2.3-1: Minimum Support Length

# Seismic Performance Categories A & B

# **English Units**

 $N(d) = [8 + 0.02*L + 0.08*H]*(1 + 0.000125 S^{2}), \text{ (inches)}$ 

Metric Units

 $N(d) = [203 + 1.67*L + 6.66*H]*(1 + 0.000125 S^2), (mm)$ 

# Seismic Performance Categories C & D

#### **English Units**

 $N(d) = [12 + 0.03*L + 0.12*H]*(1 + 0.000125 S^{2}), (inches)$ 

Metric Units

 $N(d) = [305 + 2.5*L + 10*H]*(1 + 0.000125 S^2), (mm)$ 

Note: For term definition, see the following page.

# Seismic Design - Section 6.1

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Seismic Analysis Model

#### AASHTO Div. I-A, 3.10

# Term Definitions for SPC A, B, C and D:

N(d) = minimum support length demand, in inches or mm

L = in feet or meters, as defined below

L= length of the bridge deck unit to the adjacent expansion joint or to the end of the bridge deck. For hinges within a span, L shall be the sum of , the distances to either side of the hinge. For single span bridges, L equals the length of the bridge deck. Units of L are feet or meters.

H = in feet or meters, as defined below:

H = (For abutments) The average height, from the c.g of the superstructure to the c.g. of the footing, for all bents supporting the bridge deck to the next expansion joint. H = 0 for single span bridges.

H = (For column intermediate bents) The height from the c.g. of the superstructure to the c.g. of the average footing at the expansion bent only.

H = (For pile cap & drilled shaft intermediate bents) The height from the c.g. of the superstructure to a point 5 times the pile diameter below the groundline, at the expansion bent only.

H = (For hinges within a span) The average height, from the c.g. of the superstructure to c.g. of the footing, for the two bents adjacent to the hinge.

S = Skew angle of the support, measured from a line normal to the span, in degrees.

N(c) = The shortest distance (in any direction) from the end of the girder and the edge of the substructure beam, in inches or mm, measure normal to the face of the substructure beam.

# 2.4 - Material Properties

# 2.4.1 - Soil Properties

#### Soil Profiles

From the boring data in the design layout file, determine the soil properties at known cores and borings. <u>Cores</u> describe soil types in each soil layer plus soil property test data at regular depth increments (usually 5 feet). <u>Borings</u> only describe soil types in each soil layer, without the test data. When soil properties are not well-documented at all bent locations, estimate soil properties based on the best available information. On a profile sheet, draw the cores and borings to scale at their appropriate stations and elevations. Match up soil types from borings to estimate properties from cores, or use linear interpolation between known cores.

#### Standard Penetration Test (SPT)

The most common test data reported in cores are Standard Penetration Test (SPT) blowcounts per foot (N). If only SPT data are known, other properties can be estimated using correlation charts. See Table 6.1.2.4-2 for correlations of N,  $\phi$ , c (same as S),  $\gamma$ , E,  $\nu$ , and other soil properties. Correlations with N blowcounts are fairly reliable for sands, but are less reliable for clays. The SPT blowcounts are given for three 6" intervals, and the first datum is thrown out in order to avoid seating errors. The soil shear strength, in KSF, can be estimated as S = N / 10. Hereafter, N represents (N<sub>1</sub>)<sub>60</sub> which represents the standard penetration test blowcounts corrected to 60% of the theoretical free fall energy delivered by the hammer system used to the top of the drill stem and to a overburden stress of 1 ton/ft².

#### Example:

Given: SPT data = 6 / 9 / 8 in 6" increment layers Compute: Soil Shear strength in KSF The 6 blows for the first 6" are ignored.

N = (9 in 6") + (8 in 6") = (17 blows per 12") = 17 blows/foot.S = N / 10 = 17 / 10 = 1.7 KSF = Soil Shear Strength

The standardized penetration resistance  $(N_1)_{60}$  is based on standardized equipment and procedure (E. Kavazanjian, etc., 1997). Other "non-standard" equipment and procedural details can affect the measured penetration resistance, and require correction of the blow counts in order to develop the  $(N_1)_{60}$ . The details of corrections can be found in the reference by E. Kavazanjian, etc., 1997.

MoDOT soils specialists perform the SPT tests and provide corrected penetration resistance  $(N_1)_{60}$ .  $(N_1)_{60}$  is included in the standard soil parameters request form as shown in Table 6.1.2.4-1. This form shall be used to request soil parameters in the request for soundings.

#### Compacted Backfill at Abutments

#### MO. Std. Specs. 203.3.4, 206.4.9

Backfill at abutments shall be compacted to 95% of maximum density, and it may consist of sands, clays, silts, gravels, or a mixture. Call the District, and ask what type of borrow soil will be used for compacted fill at abutments. Table 6.1.2.4-2 may be used for estimating Young's Modulus (E).

# Bridge Manual

# Seismic Design - Section 6.1

Page 2.4.1-2

Seismic Analysis Model

#### **Ultimate Soil Pressure at Abutments**

For integral and non-integral end bents, use 7.7 KSF as the ultimate soil pressure. This is based on CalTrans' recommendations, usage by other state DOT's, and tests performed at the University of California at Davis.

		Bridg	e Divi	Bridge Division Request for Soil Properties	duest f	or Soi	l Pro	pertie	ဖွ			
		=09N=N	SPT Blowco	SPT Blowcounts per 12" or per 300mm to 60% machine efficiency for granular soil in Category A. or for cohesive soil in category A. B. C. or D.	300mm to 60% n	nachine efficie	ncy for gran	ularsoil in Ca	itegony Aorfi	or cohesive soi	l in category /	A, B, C, or D.
Job #:		N=(N1)60=		SPT Blowcounts per 12" or per 300mm, corrected to 1 TSF overburden and to 60% machine efficiency for granular soil in Category B, C, or D.	300mm, correcte	d to 1 TSF ove	rburden an	1 to 60% mac	hine efficienc	y for granular:	soil in Catego	ny B, C, or D.
County:		<b>≡</b>		phi angle, internal angle of friction, degrees	of friction, degr	see						
Bridge #:		Su =		For clay, the undrained shear strength. For rock, the shear capacity, ksf or kPa	hear strength.	For rock, th	ne shear	apacity, k	sfor kPa			
Route: _		γ=		Weight per unit volume, pcf or kN/m <sup>4</sup> 3 (Saturated unit wt. below WT, Natural unit wt. above WT)	ocf or kN/m^3 (	Saturated u	nit wt. be	ow WT, N	itural unit v	rt. above W	E	
		Ш		Elastic Modulus of soil, ksf or kPa, where: E = 2*(1+v)*G and v =Poisson's ratio = 0.35(sand), 0.45(clay), 0.20 (rock	sfor kPa, whe	ere: $E = 2^*($	1+v)*Gar	d v =Poiss	on's ratio =	0.35(sand)	, 0.45(clay)	, 0.20 (rock)
		= Ew		Rock mass modulus for intact rock, ksf or kPa (AASHTO Div. 1, Section 4.4.8.2)	ntact rock, ksf	for kPa (AA	SHTO Di	. I, Section	4.4.8.2)			
		RQD =		Rock Quality Designation, %	,, %							
Bent No's.	Structural Type	z # z #	ф (degrees)	Su (ksfor kPa)	ې EorEm (pcforkN/m^3) (ksforkPa)	E or Em (ksf or kPa)	88 8 9	Allowable Allowable friction bearing (ksf or kPa) (ksf or kPa)	Allowable bearing   (ksf or kPa)	* F. S. Water Liquefaction table Ele.	Water table Ele.	** AASHTO soil profile type
	Bridge (Seismic Category A)	×									×	
	Bridge (Seismic Category B, C or D)	×	×	×	×	×				×	×	×
	Drilled Shafts (Category A)	×	×	×	×	×	×	×	×		×	
	Drilled Shafts (Category B,C or D)	×	×	×	×	×	×	×	×	×	×	×
	Ret. wall (Category A)	×	×		×						×	
	Ret. wall (Category B, C or D)	×	×		×						×	
	* Provide safety factors for liquefaction for the recommended seismic magnitude at the bridge site. The magnitude shall be based on	quefactio	on for the	recommend	ed seismic n	nagnitude	at the b	ridge sit	e. The m	gnitude s	hall be b	ased on
	the probabilities of exceedance of 10% in 50 years. (approximately corresponding to a return period of 500 years)	ance of 1	0% in 50 y	/ears. (appro	ximately co	rrespondii	ng to a	return pe	riod of 5	00 years)		
	Provide soil profile type (type I, II, II or IV based on AASHTO DIV. I-A, Sec. 3.5) at each boring location Note: If an item above is checked, then 'X' indicates the soil properties required at each boring location.	type I, II, cked, th	III or IV ba en 'X' indi	ised on AASI cates the so	HO Div. I-A, il properties	Sec. 3.5) required	at each at each	ooring lo boring k	cation cation.			
	Other req'd soil properties:		i:									
	(or special instructions)		5:									
			ဗ									
			4									

Table 6.1.2.4-1 Soil Parameter Request Form

Seismic Analysis Model

Soil Properties

 TABLE 6.1.2.4-2: SOIL PROPERTY CORRELATIONS

 In the absence of experimentally-determined soil properties, these values may be used as rough estimates.

GRANULAR	SOKS/	SORS / SANDS& GRAI	GRAVELS									
	09(1N)	ф	"S	Δ'n		Э	Poisson's	soil type	Apj	Ysal.	(.T.W.Wolad)tew	K(f) *
	(blows#t.)	(geg)	(kst)	(relative density)	grain size	(ksf)	ratio, v	distribution	(bcd)	(bcd)	dry(above W.T.)	(bcj)
Very Loose	0-5	27.00	0-0.5	0.10	fine	100.00	0.25	uniform	88.00	115.00	wet	10
					medium	100.00	0.15	mixed	95.00	120.00	dry	15
Loose	5-10	28-30	0.5-1.0	0.2 - 0.4	fine	160-240	0.25	uniform	91.00	118.00	wet	70
					medium	200-600	0.2-0.25	mixed	99.00	123.00	dry	25
Medium	10-20	30-33	1.0 - 2.0	0.4 - 0.5	fine	240-300	0.25	uniform	97.00	122.00	wet	55
					medium	800-800	0.25-0.3	mixed	104.00	127.00	dry	95
Medium Dense	20 - 35	33 - 37	2.0 - 3.5	9.0 - 5.0	fine	300-400	0.25	uniform	103.00	126.00	wet	8
					medium	800-1000	0.3-0.35	mixed	110.00	131.00	dry	158
Dense	35-70	37 - 44	3.5 - 7.0	6.0 - 8.0	fine	400-600	0.25	uniform	109.00	130.00	wet	125
					medium	1000-1600	0.35-0.4	mixed	116.00	135.00	dry	225
Very Dense	75.00	45.00	8.00	0.95	fine	700.00	0.25	uniform	112.00	133.00	wet	150
					medium	1700.00	0.45	mixed	119.00	138.00	dry	270

(over)

			108.00	0.35 (unsat.)				
0.0035	3000:00	134.00		0.50 (sat.)	1500-2000	0912	75.00	Very Hard
			106.00	0.36 (unsat.)				
0.004	2000:00	129.00		0.50 (sat.)	1000-1500	3.5 - 7.0	35 - 70	Hard
			96.00	0.37 (unsat.)				
0.005	1000.00	123.00		0.50 (sat.)	650-1000	2.0 - 3.5	20 - 35	Very Stiff
			86.00	0.38 (unsat.)				
0.007	900.005	116.00		0.50 (sat.)	300-650	1.0 - 2.0	10 - 20	Medium Stiff
			76.00	0.39 (unsat.)				
0.01	100.00	110.00		0.50 (sat.)	150-300	0.5 - 1.0	5 - 10	Soft
			73.00	0.40 (unsat.)				'
0.02	20:00	105.00		0.50 (sat.)	50-150	9'0 - 0	9-0	Very Soft
(in./in.)	(bc)	(bcd)	(bct)	ratio, v	(kst)	(kst)	(blows/ft.)	
* 052	¥ (₩) ×	Ysat.	λqιλ	Poisson's	Э	<sup>™</sup> S = ɔ	Neo	

No = Standard Penetration Test blowcount, blows / ft., to 60% machine efficiency

angle of internal friction, for cohesionless sands and gravels, degrees

c = cohesion of cohesive clays and silts, ksf

Su = shear strength of soil at a given normal stress, ksf.

For sands (c = 0),  $S_u = p^* tan(\phi)$ , where  $p = effective normal stress, or <math>S_u = N / 10$ , in ksf.

For clays ( $\phi$ =0),  $S_u$  = c, and therefore shear capacity is independent of normal stress

For mixed soils ( $\phi$ -c soils),  $S_u = c + p * tan(\phi)$ 

For clays, c can be estimated from (unconfined compression strength, Qu)/2) E = Young's Modulus = Elastic Modulus, ksf. E = <math>2\*(1+v)\*G

G = Shear Modulus, ksf

 $\gamma$  = soil unit weight, pcf.  $\gamma$  =  $\gamma_{any}^{*}$  (1 + w), where w = water content, unitless K = f = slope (variation) of linear subgrade modulus.

 $\epsilon_{50}$  = strain at 50% of the maximum difference in principal stresses, unitless For further estimation of soil properties, see also AASHTO Div. I, Ch. 4. W.T. = water table elevation, feet

\*: For p-y curve analysis

(cont.)

CLAYS & SILTS

SOILS /

COHESIVE

# Seismic Design - Section 6.1

Page 2.4.2-1

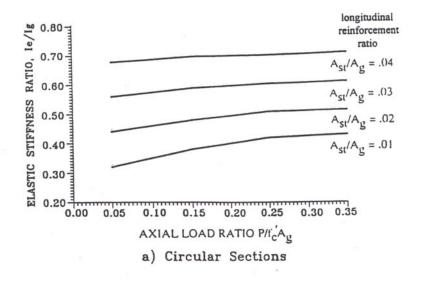
Seismic Analysis Model

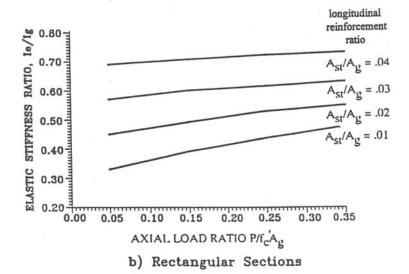
#### 2.4.2 - Concrete Properties

The concrete compression strength, f'c, should be a probable, rather than a minimum. 1.5 f'c shall be used in the seismic analysis. This over the specified strength recognizes the typically conservative mix designs and the natural strength gain with concrete age.

The flexural rigidity of columns, beam cap and c.i.p. piles should be calculated based on the cracked sections, rather than gross member section. Natural periods should also be based on the cracked sections. The flexural rigidity of the cracked section is defined as the rigidity at which the first steel rebar reaches the yield limit state.

Figure 6.1.2.4.2-1 shows the moment of inertia ratio,  $I_e/I_g$ , for circular and rectangular columns.





#### Where:

A<sub>g</sub> = gross section area

 $A_{st}$  = steel section area

 $I_a$  = gross moment of inertia

 $I_e$  = effective moment of inertia of cracked section

f'c = compressive strength of unconfined concrete

P = applied axial compressive load

Figure 6.1.2.4.2-1 Adjustment Factors for Effective Stiffness for Concrete (Priestly et al, 1996)

# Bridge Manual

# **Seismic Design - Section 6.1**

Page 2.4.3-1

Seismic Analysis Model

# 2.4.3 - Steel Properties

Yield strength of reinforcement should be based on mill certificate or tensile test results if available. If not, a nominal strength of 1.1 times the specified minimum strength should be assumed, resulting in 66 ksi yield strength for grade 60 reinforcement. (Priestly et al,1996; FHWA, 1995)

# 2.5 - Liquefaction

# **Conditions for Liquefaction**

Volume II of report #FHWA/RD-86/102, sections 4.2-4.3

When subjected to seismic ground motions, some soils tend to liquefy - that is, to lose most of their shear strength. When ground shaking is intense and of long duration, soil pore pressures can build up and exceed the intergranular stress, causing loss of grain contact and loss of cohesion. Liquefaction of soil can lead to extremely large displacements and dramatic structural failure. Some high-risk factors for liquefaction might include:

Water Table Location = below water table, saturated, or water content greater than 0.9 \* Liquid Limit,

Soil type = poorly-drained cohesionless soils or nonplastic silts with Liquid Limit < 35%,

Soil gradation = uniformly-graded and fine particle size, low percentage of plastic fines (< 5%),

Relative Density = loose, with relative density,  $D_R < 50\%$ ,

Confining pressure = low confinement pressure, in top 50 feet of soil, Intensity of ground shaking = exceeding critical acceleration levels, close to epicenter,

Duration of shaking = long duration, numerous cycles.

# When to Check Liquefaction

The Soil Report should include the factor of safety against liquefaction, but if it is not the bridge designers should calculate the factor of safety against liquefaction for each <u>saturated</u> (submerged under the water table) soil layer at each bent. Do not check compacted abutment fill near vertical end drains. If the factor of safety against liquefaction is less than 1.3, then consider the possibility of liquefaction as explained in Step 3 below. If both the designer and checker agree that the factor of safety against liquefaction is less than 1.0, then consult the Structural Project Manager about the possibility of lengthening piles, increasing pile sizes, or soil strengthening measures.

AASHTO Div. I-A, 1992 Commentary, C6.3.1(A), C6.4.1(A), C6.5.1(A)

# Step 1:

Compute the seismically-induced (active) cyclic stress ratio,  $\frac{ au_{\scriptscriptstyle av}}{\sigma_{\scriptscriptstyle o'}}$  .

$$\frac{\tau_{av}}{\sigma_{o'}} = 0.65 * A * \sigma_T * \frac{r_d}{\sigma_{o'}}$$

 $\tau_{\text{av}}$  = average earthquake-induced shear stress on the sand layer under consideration, psf

 $\sigma_{o}'$  = initial effective overburden pressure, psf (Use  $\gamma' = \gamma_t - \gamma_w$ ) below the watertable, where  $\gamma_w$  = 62.4 pcf)

A = Acceleration Coefficient

 $\sigma_T$  = total stress at mid-layer of soil, psf, =  $\Sigma \gamma_t * H_t$  for each layer from the ground surface down to the layer being investigated.

 $r_{\rm d}$  = a stress reduction factor varying from 1.0 at ground surface to 0.9 at about 30 feet deep, remaining at 0.9 for depths below 30 feet

# Step 2:

Determine the (resistive) cyclic stress ratio,  $\frac{\tau}{\sigma'}$ , as described below.

From Fig. 6.1.2.5-1, enter with  $(N_1)_{60}$  and M, and determine the (resistive)

cyclic stress ratio, 
$$\frac{\tau}{\sigma'_{\nu}}$$
 . (N<sub>1</sub>)<sub>60</sub> is described in Section 6.1.2.4.

In the absence of getting a Richter magnitude, M, from the geotechnical engineer, the USGS deaggregation map can be used or the following table may also be used, where "A" represents the design acceleration coefficient.

A = 0.04g	M = 4.25
A = 0.08g	M = 4.75
A = 0.16g	M = 5.75
A = 0.33g	M = 7.00
A = 0.50g	M = 8.50

The USGS deaggregation maps are available on the internet at: http://geohazards.cr.usgs.gov/eq/.

# Step 3:

Calculate the factor of safety against liquefaction.

$$FS = \frac{\text{Re } \textit{sistive}}{\textit{Active}} = \frac{\textit{Step } 2}{\textit{Step } 1} \ge 1.3 \text{ (desired) or } 1.0 \text{ (required)}$$

If FS  $\geq$  1.3, then analyze the bridge on the assumption that liquefaction will not occur. If FS < 1.3, then assume liquefaction might occur within the layer under consideration: this consists of running two seismic analyses to design the bridge for both possibilities of: a) liquefaction and b) no liquefaction. Note that superstructures may be subject to large lateral movement when soil liquefation is considered in the seismic analysis. Hence, expansion bearings shall be designed to tolerate these movements. For CIP concrete piles, determine the maximum pile moment and depth, with and without liquefaction, and design reinforcement down to the development length below that depth, as necessary.

#### AASHTO Div. I-A, 6.4.2(C), 7.4.2(C)

The residual strength of the liquefied soil layer may be considered. The calculation of residual strength is described below.

#### **Residual Strength**

Liquified soil has a residual shear strength, S<sub>r</sub>, which can be considered for the pile stiffness computations. When not enough information is available, use a residual strength of zero. The residual shear strength shall not be more than the non-liquefied shear strength.

The residual shear strength of liquefied soil can be estimated by using the corrected penetration resistance,  $(N_1)_{60}$ , as described previously, but with an additional correction factor,  $N_{corr}$ , for fines contents to generate an equivalent "clean sand" blowcount value  $(N_1)_{60\text{-CS}} = (N_1)_{60} + N_{corr}$ , where  $N_{corr}$  values are shown in Table 6.1.2.5-1.

Percent Fines	N <sub>corr</sub> (blows/ft)
10%	1
25%	2
50%	4
75%	5

Table 6.1.2.5-1 Corrections to Blowcounts for Percent Fines (N<sub>corr</sub>)

Figure 6.1.2.5-2 presents an updated correlation between  $S_r$  and  $(N_1)_{60\text{-CS}}$  (FHWA-SA-97-076, 1997). For  $(N_1)_{60\text{-CS}} > 16$  blows, continue the curve as a straight line at the same slope as at 16 blows.

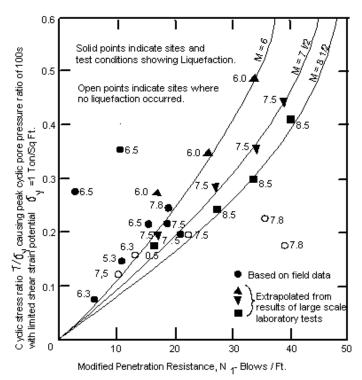


Figure 6.1.2.5-1 Resistive Cyclic Stress Ratio (AASHTO Div. I-A 1998 Commentary, Figure CA1) Note: AASHTO's  $N_1$  is actually  $(N_1)_{60}$ 

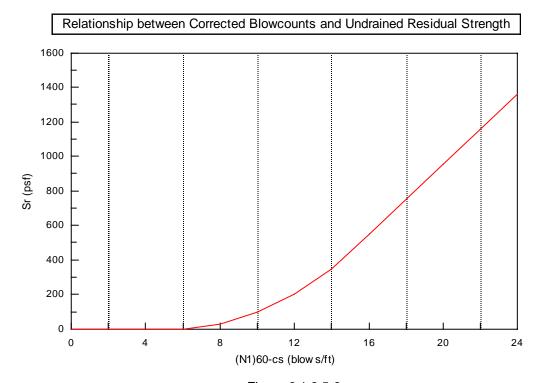


Figure 6.1.2.5-2 Relationship between Corrected Blowcounts ( $N_1$ )<sub>60-CS</sub> (Blows/ft) and Undrained Residual Strength  $S_r$  (psf). (FHWA-SA-97-076, 1997)

# **2.6 Spring Constants**

#### 2.6.1 - Modeling Abutment Stiffnesses

#### "Full-Zero" Abutment Stiffnesses

For the "full-zero" stiffness approach, one abutment's backfill is in compression (full soil springs are engaged) while the other abutment's backfill is in tension (this backwall soil spring is zero because soil tensile strength is negligible. Note that although the backwall soil stiffness is zero, the pile, beam and wing stiffnesses are NOT zero.) To account for compression and tension at both abutments, two Seismic Structural Analysis programs are required:

(Program # 1) Use full springs at all pile and soil springs, except set the backwall spring equal to zero at the FIRST abutment only, and

(Program # 2) Use springs at all pile and soil springs, except set the backwall spring equal to zero at the SECOND abutment only.

For analyzing and designing the structure, use the worst case forces from these two models. When these "full-zero" models are used, the resulting longitudinal abutment soil force does not require adjustment as it would in the "half-half" model.

#### "Half-Half" Abutment Stiffnesses

For skewed bridges, the "half-half" method should not be used. For the "half-half" stiffness approach, half of the backwall soil stiffness is used at each abutment, in addition to the full stiffnesses at all other abutment spring elements (piles, beams, wings, etc.). After the seismic analysis, the "half-half" method also requires doubling the backwall force.

#### Non-Integral Abutments

For non-integral abutments with restrainers, three separate Seismic Structural Analysis Programs are required:

- (1) With restrainer elements only on the first abutment: This model covers movement toward the last abutment.
- (2) With restrainer elements only on the last abutment: This model covers movement toward the first abutment.
- (3) Without restrainer elements: With no restrainers, the components of the springs that are longitudinal with respect to the bridge centerline will have no effect.

#### Point-of-Fixity Approximations for Piles

Avoid using the point-of-fixity formulas (U.S. Steel Design Handbook, 1965 & NHI Course No. 13063, 1996). Stiffnesses based on estimated points of fixity are not recommended, for several reasons:

- a) For standard integral pile cap END bents, there is DOUBLE-curvature bending in both directions. The point-of-fixity formulas were apparently derived for SINGLE-curvature bending, so the formulas should not be used for most standard integral end bents.
- b) For standard INTERMEDIATE bents, out-of-plane bending is usually single-curvature, and in-plane bending is usually double-curvature, and one fixity length cannot model the different bending cases in both directions at the same time. Therefore, the point-of-fixity formulas should not be used for most standard intermediate bents.
- c) The point-of-fixity formulas also assume homogeneous soil (no layers). When piles or drilled shafts penetrate through multiple varying soil layers, or when the water table is near the top of the pile head, use programs such as SPILE and COM624P because of their more accurate analyses and their more detailed soil layer geometries.
- d) It is virtually impossible to select a point of fixity such that both the maximum deflection and maximum bending both were computed correctly.

#### 2.6.2 - Abutment Stiffness, Wilson Equations

# Abutment Soil Types

Compacted Backfill: Wings, Backwall and possibly Beam

Call the district to determine the type of borrow soil that will most likely be used as abutment backfill. When estimating soil properties (see Section 6.2.4), consider that backfill is compacted to 95% maximum density, so assume dense or stiff conditions.

MO. Std. Specs. 203.3.4, 206.4.9

Natural (in-situ): possibly Beam

Use available boring data for estimating soil deposit properties.

# **Abutment Spring Types**

Spring Location	n Direction of Spring	Type of Soil @ Location
Backwall Beam Wings	Horizontal, normal to backwall Vertically downward Horizontal, normal to wing	Compacted backfill In-situ? or compacted? Compacted backfill

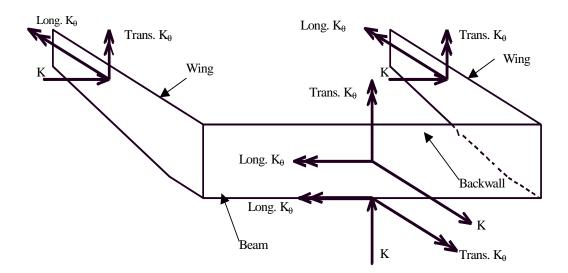


FIGURE 6.1.2.6.2-1: ABUTMENT SPRINGS Orientations of Wilson Equation Stiffnesses

# Wilson Equations (Wilson, 1988)

For translational and rotational stiffnesses on plate-like elements such as backwalls, wings and beams, use the Wilson equations:

#### Translation normal to the plane

$$K = \frac{E * L}{(1 - v^2) * I}, \text{ kip/ft.}$$

#### Rotation about the transverse axis (y-axis)

$$K_{\theta y} = \frac{K*L^2}{12}$$
 , kip\*ft./radian

#### Rotation about the longitudinal axis (x-axis)

$$K_{\alpha} = \frac{K * B^2}{12}$$
, kip\*ft./radian

The axis orientation for each element used to determine  $K_{\theta x}$  and  $K_{\theta y}$  is shown in Figure 6.1.2.6.2-2 below. If K is reduced as in Section 6.1.2.10, then  $K_{\theta}$  must also be reduced.

K = estimated equivalent linear stiffness for translation, kip/foot

 $K_{\theta}$  = estimated equivalent linear stiffness for rotation, kip\*foot/radian

E = Young's Modulus of soil at spring location, either for in-situ soil or for compacted backfill, ksf

L = length of item, feet

For backwall, L = length of backwall along skew, to inside wing face For wings, L = inside layout length of wing

For beams, L = skewed length of beam along cl. beam

v = Poisson's Ratio of soil at spring location, either natural or compacted

I = 1.2136 \* 
$$\log_{10} \left(\frac{L}{B}\right)$$
 + 0.84 = Shape factor for soil contact area

B = height or width of item, feet

For backwall, B = height from top of slab to bottom of beam

For wings, B = equivalent height of wing = (wing area)/(wing L) For beams, B = beam width normal to beam

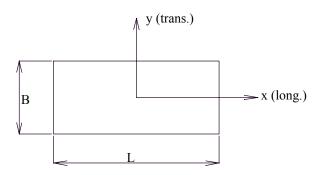


FIGURE 6.1.2.6.2-2 ELEMENT ORIENTATION

#### 2.6.3 – Pile Axial Stiffness

# General Procedure

- 1) From the boring data and the bridge profile plot, determine the SPT blowcounts along the pile length.
- 2) Determine the soil properties required for the SPILE computer program or any other computer programs based on the methods presented by Nordlund (1963,1979), Thompson (1964), Meyerhoff (1976), Cheney and Chassie (1982), and Tomlison (1979,1985). Assume that the groundwater table is at the design high water elevation.
- 3) Run the SPILE program (Urzua, 1993) or other programs using the methods described above to determine Q<sub>b</sub> and Q<sub>f</sub>.
- 4) Determine the axial pile stiffness, K, as described below for friction piles and bearing piles (Lam and Martin, 1986).

#### **Friction Piles**

Q<sub>u</sub>= the ultimate axial pile capacity, in kips (or tons)

Q<sub>f</sub> = the ultimate friction capacity from SPILE, in kips (or tons)

Q<sub>b</sub> = the ultimate bearing capacity from SPILE, in kips (or tons)

For steel HP friction piles, use the box perimeter for friction, but use the HP steel area for bearing.

In compression,

 $\begin{aligned} &Q_u = Q_f + Q_b \\ &Q_u = Q_f \end{aligned} \quad \text{because } Q_b = \text{zero}.$ In tension,

The typical pile resistance - displacement relationship is shown in Figure 6.1.2.6.3-1.

At a displacement, z, at which the pile capacity is less than the ultimate capacity (q < Q<sub>u</sub>), the partial capacity, q, is equal to the sum of the partial friction capacity, f, and the partial bearing capacity, b.

q = f + b, in kips

f = friction mobilized along a pile segment at a displacement, z≤z<sub>c</sub>

$$f=Q_f*\left[2*\sqrt{rac{z}{z_c}}-rac{z}{z_c}
ight], \, {
m kips}$$

 $z_c$  = the critical displacement of the pile segment at which  $Q_f$  is fully mobilized. Use  $z_c = 0.2$ ".

b = tip resistance mobilized at a displacement,  $z \le z'_c$ 

$$b = Q_b * \left(\frac{z}{z'_c}\right)^{1/3}, \text{ kips}$$

z'<sub>c</sub> = the critical pile displacement at which Q<sub>b</sub> is fully mobilized.

Use  $z'_c = 0.05*D$ , inches

D = least pile dimension (D = diameter for C.I.P. piles), inches

#### Friction Piles cont.

However, the pile itself will deform, also. This pile deformation or pile compliance,  $\delta$ , should be included in the pile resistance – displacement curve as shown in Figure 6.1.2.6.3-1.

$$\delta = \frac{qL}{AE}$$
 = pile compliance = pile deformation, inches

q = f + b = compressive axial load corresponding to a pile displacement z, kips

L = total friction length of the pile in the soil, inches

AE = For concrete C.I.P. piles, AE =  $A_cE_c+A_sE_s$ , kips. For steel HP piles, AE =  $A_sE_s$ , kips.

From Figure 6.1.2.6.3-1, it can be seen that the pile axial load-axial deformation curve is nonlinear. If response spectrum method is considered in the analysis, the secant modulus stiffness is used. The secant modulus stiffness,  $K_s$ , is defined as the slope between two points at which the axial

loads are equal to zero and  $\frac{Q_u}{2}$  . For regular highway bridge foundation

piles, typical levels of cyclic compression loading would be from 50 to 70% of  $Q_{\rm u}$ .

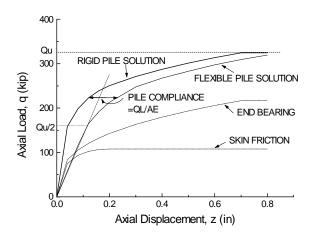


FIGURE 6.1.2.6.3-1 Pile Axial Stiffness Model

# Steel HP Bearing Piles

In compression,  $Q_f = 0$ , because bearing piles bear directly on rock.

In tension,  $Q_f$  = the ultimate friction capacity of the pile.

Q<sub>b</sub> = the ultimate bearing capacity, in kips (or tons)

$$Q_b = 0.25 * f_y * A_s$$
 (AASHTO 4.5.7.3), where:

 $A_s$  = the HP steel pile area, in square inches

 $f_y$  = yield stress of the pile steel, in ksi

In compression,  $Q_u = Q_b$ , because  $Q_f = zero$ .

In tension,  $Q_u = Q_f$ , because  $Q_b = zero$ .

The pile is more often in compression due to preloading from dead load, so the pile axial spring constant can be calculated as:

$$K_s = \frac{AE}{L}$$
,

where:

 $AE = A_sE_s$ , kips, using the HP steel area, square inches.

L = total length of pile between the pile cap and the point of bearing on rock, inches.

## Pile Group Effects

Design pile footings with a center to center spacing of more than or equal to 3 pile diameters.

- a) Pile group capacity in cohesionless soils: The ultimate group capacity for driven piles in cohesionless soils can be taken as the sum of the individual ultimate pile capacities.
- b) Pile group capacity in cohesive soils:
  - 1) For pile groups driven in clays with c ≤ 14 psi, a group efficiency of 0.7 (i.e. use 70% of the sum of the individual ultimate pile capacities) for center to center pile spacings of three times the pile diameter. If the center to center pile spacing is greater than 6 times the pile diameter, a group efficiency of 1.0 may be used. Linear interpolations should be used for intermediate center to center pile spacings.
  - 2) For pile groups driven in clays with c > 14 psi, a group efficiency of 1.0 may be used.

#### 2.6.4 - Pile Lateral and Rotational Stiffness, (p-y curves)

### Calculating Stiffnesses

The pile lateral translational spring constants are determined using estimated soil properties and the COM624P computer program (Wang and Reese, 1993) or any other programs that utilize non-linear p-y curves for either single piles or a pile group.

- 1) First, set up the soil depth profile at the pile location. Use the boring data and the bridge profile plot to determine the SPT blowcounts along the pile length.
- 2) For a given soil profile, the pile lateral force-lateral deflection curve at the top of pile (pile head) can be obtained by applying incremental lateral forces at the pile head, the program then calculates the corresponding lateral deflections at the pile head. The material non-linearity of the pile is also considered in the program. Similarly, pile moment-rotational curve at the top of pile can be obtained by the COM624P program.

Since the response spectrum method is based on linear analysis, the secant modulus stiffness is used to represent the equivalent linear stiffness. The secant modulus stiffness is defined as the slope between two points at which the lateral loads are equal to zero and  $P(M_u)/2$ , where  $M_u$  is the ultimate moment capacity of the pile;  $P(M_u)$  represents the lateral load at which  $M_u$  is developed in the pile. The ultimate moment capacity of CIP pile or composite concrete-steel shell pile is based on the limit state of concrete strain,  $\epsilon_c = 0.003$  and the steel shell strain,  $\epsilon_s = 0.015$ . The ultimate moment capacity of steel HP pile is equal to the plastic moment,  $M_p$ , of the pile under constant axial load due to superstructure and substructure loads.

3) It should be recognized that using the secant stiffness approach (including axial, lateral, and rotational stiffness) in the seismic analysis is an approximation method to simplify the time consuming non-linear dynamic analysis following the load-deformation relationship of the pile head. In general, using the secant stiffness approach in conjunction with the pile stress check described in section 6.1.2.10 gives reasonable solutions in the design process without conducting an iterative procedure.

**Example 6.1.2.6.4-1** Find the stiffness of an individual pile at the groundline level which represents the characteristics of the soil—pile interactions.

<u>Description</u>: A pile-cap bent with four steel HP12 x 53 piles is shown in Figure 6.1.2.6.4-1. The bent has skew of 54.5 degrees. For individual piles, the stiffnesses of pile-soil interaction are estimated using COM624P computer program, then these stiffnesses are used to form Point elements in the structural model as shown in Figure 6.1.2.6.4-2. The point elements are located at the ground level which represent the characteristics of the pile-soil interactions.

Revised: June 2000 D9835

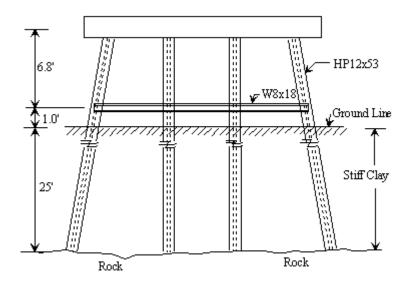
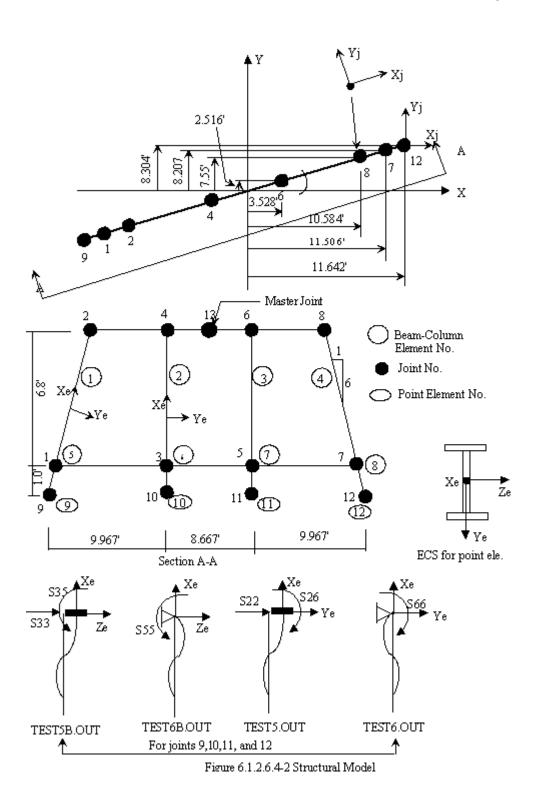


Figure 6.1.2.6.4-1 Intermediate Pile Bent

The soil is classified as stiff clay with c=2 ksf;  $\gamma=0.069$  pci;  $\epsilon_{50}=0.007$ ; and k =400 pci, where c is the undrained shear strength of clay;  $\gamma$  is effective unit weight;  $\epsilon_{50}$  is the strain corresponding to one-half the maximum principle stress difference; and k is the variation of soil modulus.

In order to formulate the stiffnesses of pile-soil interaction, the computer program COM624P is used to obtain the translational, rotational and rotational-translational coupling stiffnesses for joints 9, 10, 11, and 12 (see Figure 6.1.2.6.4-2). The COM624P output for fixed head and applied lateral forces in the  $y_e$  direction, hinge head and applied moment in the  $z_e$  direction, fixed head and applied lateral forces in the  $z_e$  direction, and hinge head and applied moments in the  $y_e$  direction are shown in the output files TEST5.OUT, TEST6.OUT, TEST5B.OUT, and TEST6B.OUT, respectively.



New: April 2000 SD001

### **TEST5.OUT**

```
EXAMPLE FOR DETERMINING PILE HEAD STIFFNESSES
     UNITS-ENGL
         PILE DEFLECTION, BENDING MOMENT, SHEAR SOIL RESISTANCE
                        INPUT INFORMATION
     THE LOADING IS STATIC
     PILE GEOMETRY AND PROPERTIES
          PILE LENGTH
                                                     300.00 IN
          MODULUS OF ELASTICITY OF PILE = .290E+05 KIP/IN**2
                       1 SECTION(S)
                                    DIAMETER MOMENT OF
                                      IN
                                                                     TN**2
                                                    TN**4
                     300.00
                                   11.780
                                                    .394E+03
                                                                     .156E+02
                    300.00
     SOILS INFORMATION
         X-COORDINATE AT THE GROUND SURFACE SLOPE ANGLE AT THE GROUND SURFACE
          1 LAYER(S) OF SOIL
          LAYER 1
          THE LAYER IS A STIFF CLAY ABOVE THE WATER TABLE
         X AT THE TOP OF THE LAYER = .00 IN
X AT THE BOTTOM OF THE LAYER = 360.00 IN
VARIATION OF SOIL MODULUS, k = .400E+03 LBS/IN**3
         DISTRIBUTION OF EFFECTIVE UNIT WEIGHT WITH DEPTH
                      2 POINTS
X,IN
                              WEIGHT, LBS/IN**3
                    .00
360.00
                                    .69E-01
                                     .69E-01
         DISTRIBUTION OF STRENGTH PARAMETERS WITH DEPTH
                            2 POINTS
                              C,LBS/IN**2
                      X,IN
                                                    PHI, DEGREES
                                  .140E+02
                    .00
                                                    .000
                                                                     .700E-02
                                  .140E+02
     FINITE DIFFERENCE PARAMETERS
         NUMBER OF PILE INCREMENTS
TOLERANCE ON DETERMINATION OF DEFLECTIONS
                                                                       = .100E-04 IN
          MAXIMUM NUMBER OF ITERATIONS ALLOWED FOR PILE ANALYSIS =
                                                                             .15E+03 IN
         MAXIMUM ALLOWABLE DEFLECTION
     INDIT CODES
         OUTPT =
          KCYCL =
         KBC
          KPYOP =
    EXAMPLE FOR DETERMINING PILE HEAD ROTATIONAL TRANS. STIFFNESSES
     UNITS-ENGL
                         OUTPUT INFORMATION
                              SUMMARY TABLE
 LATERAL
             BOUNDARY
   TIOAD
           CONDITION
                            LOAD
                                                                    MOMENT
                                                                                STRESS
  (KIP)
                           (KIP)
                                          (IN)
                                                      (IN/IN)
                                                                   (IN-KIP) (LBS/IN**2)
                                                      .000E+00 -.242E+03
.278E-17 -.630E+03
-.111E-16 -.110E+04
               .000E+00
   .100E+02
.200E+02
                           .124E+03
.124E+03
                                       .160E-01
.684E-01
                                                                               .116E+05
               .000E+00
   .300E+02
               .000E+00
                           .124E+03
                                        .159E+00
                                                     -.111E-16
                                                     -.111E-16 -.163E+04
.000E+00 -.222E+04
.000E+00 -.285E+04
.000E+00 -.351E+04
                           .124E+03
                                        .289E+00
   .400E+02
               .000E+00
                                                                               .324E+05
   .500E+02
               .000E+00
                           .124E+03
                                        .458E+00
   .600E+02
               .000E+00
                           .124E+03
                                        .667E+00
                                                                               .505E+05
               .000E+00
                           .124E+03
                                       .916E+00
                                                      .000E+00 -.422E+04
.000E+00 -.496E+04
.888E-16 -.573E+04
               .000E+00
                           .124E+03
.124E+03
                                       .121E+01
.154E+01
   .800E+02
                                                                               .710E+05
               .000E+00
                                                                               .820E+05
   .900E+02
   .100E+03
               .000E+00
                           .124E+03
                                       .192E+01
                                                                               .935E+05
```

Page 2.6.4-5

Seismic Analysis Model

## **TEST6.OUT**

```
EXAMPLE FOR DETERMINING PILE HEAD STIFFNESSES
UNITS - - ENGL
    PILE DEFLECTION, BENDING MOMENT, SHEAR SOIL RESISTANCE
                   I N P U T I N F O R M A T I O N *****************************
THE LOADING IS STATIC
 PILE GEOMETRY AND PROPERTIES
                                            300.00 IN
     PILE LENGTH
     MODULUS OF ELASTICITY OF PILE = .290E+05 KIP/IN**2
                 1 SECTION(S)
                        DIAMETER MOMENT OF
                                         INERTIA
                                          IN**4
              300.00
                            11.780
                                         .394E+03
                                                          .156E+02
              300.00
SOILS INFORMATION
    X-COORDINATE AT THE GROUND SURFACE = SLOPE ANGLE AT THE GROUND SURFACE =
     1 LAYER(S) OF SOIL
     LAYER 1
     THE LAYER IS A STIFF CLAY ABOVE THE WATER TABLE
    X AT THE TOP OF THE LAYER = .00 IN
X AT THE BOTTOM OF THE LAYER = 360.00 IN
                                   = .400E+03 LBS/IN**3
     VARIATION OF SOIL MODULUS, k
    DISTRIBUTION OF EFFECTIVE UNIT WEIGHT WITH DEPTH
                      2 POINTS
                       WEIGHT, LBS/IN**3
              .00
                             .69E-01
    DISTRIBUTION OF STRENGTH PARAMETERS WITH DEPTH
               2 POINTS
                                         PHI, DEGREES
                       C,LBS/IN**2
                           .140E+02
                                           .000
                                                          .700E-02
                           .140E+02
FINITE DIFFERENCE PARAMETERS
    NUMBER OF PILE INCREMENTS
TOLERANCE ON DETERMINATION OF DEFLECTIONS
                                                              .100E-04 IN
     MAXIMUM NUMBER OF ITERATIONS ALLOWED FOR PILE ANALYSIS =
                                                                 .15E+03 IN
    MAXIMUM ALLOWABLE DEFLECTION
 INPUT CODES
    OUTPT = 1
KCYCL = 1
     KBC
           = 4
EXAMPLE FOR DETERMINING PILE HEAD ROTATIONAL TRANS. STIFFNESSES
UNITS--ENGL
                  OUTPUT INFORMATION
PILE LOADING CONDITION
    LATERAL DEFLECTION AT PILE HEAD = .000E+00 IN
APPLIED MOMENT AT PILE HEAD = .140E+04 IN-KIP
AXIAL LOAD AT PILE HEAD = .124E+03 KIP
    X DEFLECTION MOMENT TOTAL
                                         SHEAR
                                                      SOIL
                                                                FLEXURAL
 STRESS
                                                      RESIST
```

```
.114E+08
     35 00
             - 442E-01
                          550E+03
                                       162E+05
                                                 - 206E+02
                                                              - 261E+03
     40.00
             -.437E-01
                          .451E+03
                                       .147E+05
                                                  -.192E+02
     45.00
             -.423E-01
                           358E+03
                                       .133E+05
                                                  -.178E+02
                                                              - 285E+03
                                                                            .114E+08
                          .272E+03
     50.00
             -.400E-01
                                       .120E+05
                                                  -.164E+02
                                                              -.294E+03
                                                                            .114E+08
                                                  -.149E+02
     55 00
             -.372E-01
                           .194E+03
                                       .108E+05
                                                              - 301E+03
                                                                            .114E+08
     60.00
             -.339E-01
                           .123E+03
                                       .978E+04
                                                  -.134E+02
                                                              -.307E+03
                                                                            .114E+08
             -.304E-01
                           .592E+02
                                       .883E+04
                                                  -.118E+02
                                                              -.311E+03
                                                                            .114E+08
     70.00
             -.267E-01
                           .350E+01
                                       800E+04
                                                  -.103E+02
                                                              -.312E+03
                                                                            .114E+08
             -.230E-01
                                       .861E+04
                           .444E+02
                                                  -.870E+01
                                                                            .114E+08
     75.00
                                                              -.312E+03
     80.00
               .194E-01
                          .844E+02
                                       921E+04
                                                    714E+01
                                                              -.310E+03
                                                                            .114E+08
     85.00
             -.160E-01
                                       .969E+04
                                                  -.560E+01
                                                              -.306E+03
                                                                            .114E+08
               .129E-01
                                       .101E+05
                                                    408E+01
                                                                299E+03
                                                                            .114E+08
     95.00
             -.100E-01
                           158E+03
                                       .103E+05
                                                  -.261E+01
                                                              -.290E+03
                                                                            .114E+08
               .754E-02
                                       .105E+05
                          -.168E+03
                                                  -.118E+01
                                                                            .114E+08
                                                   .178E+00
                                                                            .114E+08
    105 00
             -.541E-02
                          - 171E+03
                                       .105E+05
                                                              - 265E+03
             -.366E-02
                                       .104E+05
                                                              -.247E+03
    110.00
                         -.167E+03
                                                   .146E+01
                                                                            .114E+08
                                       .103E+05
                                                   .264E+01
    115.00
              .227E-02
                          .157E+03
                                                              -.226E+03
                                                                            .114E+08
             -.122E-02
                         -.141E+03
                                       .101E+05
                                                              -.199E+03
    120.00
                                                                            .114E+08
    125.00
              .483E-03
                                       .974E+04
                                                   .462E+01
                                                                            .114E+08
                           120E+03
                                                                .162E+03
    130.00
              .440E-05
                          .951E+02
                                       .937E+04
                                                   .524E+01
                                                               -.464E+02
                                                                            .114E+08
              .266E-03
                           .693E+02
                                       .899E+04
                                                   .484E+01
                                                               .141E+03
                                                                            .114E+08
    140.00
              384E-03
                         - 470E+02
                                       865E+04
                                                   409E+01
                                                               154E+03
                                                                            .114E+08
              .399E-03
                                       .837E+04
                                                   .332E+01
                                                               .156E+03
    145.00
                          .284E+02
                                                                            .114E+08
    150.00
              .351E-03
                          -.138E+02
                                       815E+04
                                                   .255E+01
                                                               .151E+03
                                                                            .114E+08
    155.00
              .273E-03
                         -.289E+01
                                       .799E+04
                                                   .181E+01
                                                               .141E+03
                                                                            .114E+08
                                       .802E+04
    165.00
               .112E-03
                           858E+01
                                       808E+04
                                                   .528E+00
                                                               .113E+03
                                                                            .114E+08
    170.00
                          .986E+01
                                                   .463E-02
              .540E-04
                                       .810E+04
                                                               .942E+02
                                                                            .114E+08
    175.00
              .177E-04
                           876E+01
                                       808E+04
                                                  -.415E+00
                                                                .712E+02
                                                                            .114E+08
                                       .804E+04
    180.00
              .252E-06
                          .588E+01
                                                  -.689E+00
                                                               .227E+02
                                                                            .114E+08
    185.00
              .442E-05
                           .253E+01
                                       .799E+04
                                                   .549E+00
                                                                .504E+02
                                                                            .114E+08
                                                  -.299E+00
    190.00
             -.339E-05
                          .420E+00
                                                              -.471E+02
                                                                            .114E+08
             -.127E-05
                           .506E+00
                                       .796E+04
                                                  -.832E-01
    200.00
             -.133E-06
                          -.490E+00
                                       .796E+04
                                                   .711E-01
                                                              -.204E+02
                                                                            .114E+08
             .135E-07
                         -.391E-01
                                       .795E+04
                                                   .528E-01
    205.00
                                                               .968E+01
                                                                            .114E+08
                                                                            .114E+08
    210.00
             -.374E-12
                          117E-03
                                       795E+04
                                                  - 488E-02
                                                               - 522E+00
              .313E-17
    215.00
                          -.101E-08
                                       .795E+04
                                                   .136E-06
                                                               .147E-04
                                                                            .114E+08
    220.00
              .261E-22
                           863E-14
                                       .795E+04
                                                   .114E-11
                                                               .123E-09
                                                                            .114E+08
    225.00
              .218E-27
                                       .795E+04
                                                               .102E-14
                          -.741E-19
                                                   .951E-17
                                                                            .114E+08
    230.00
             -.182E-32
                           .636E-24
                                       .795E+04
                                                  -.794E-22
                                                               -.855E-20
                                                                            .114E+08
    235.00
              .152E-37
                           .545E-29
                                       .795E+04
                                                  -.216E-29
                                                                .713E-25
                                                                            .114E+08
    240.00
             -.126E-42
                          .467E-34
                                       .795E+04
                                                   .185E-34
                                                               -.595E-30
                                                                            .114E+08
    245.00
               105E-47
                           400E-39
                                       .795E+04
                                                  -.158E-39
                                                                496E-35
                                                                            .114E+08
                                       .795E+04
    250.00
             -.880E-53
                           .342E-44
                                                   .136E-44
                                                               .414E-40
                                                                            .114E+08
    255.00
              .733E-58
                           .293E-49
                                       .795E+04
                                                   .116E-49
                                                                .345E-45
                                                                            .114E+08
                          .250E-54
                                       .795E+04
                                                               -.288E-50
    260.00
             -.611E-63
                                                   .993E-55
                                                                            .114E+08
                                       .795E+04
                                                                            .114E+08
    270 00
             - 425E-73
                          183E-64
                                       795E+04
                                                   725E-65
                                                               - 200E-60
             .354E-78
                                       .795E+04
    275.00
                         -.156E-69
                                                  -.619E-70
                                                               .166E-65
                                                                            .114E+08
                                                                            .114E+08
                          .133E-74
    280.00
             -.295E-83
                                       .795E+04
                                                   529E-75
                                                               - 139E-70
                                       .795E+04
    285.00
              .245E-88
                         -.114E-79
                                                  -.451E-80
                                                               .115E-75
                                                                            .114E+08
    290.00
              .204E-93
                          .970E-85
                                       .795E+04
                                                   .385E-85
                                                                961E-81
                                                                            .114E+08
                         -.827E-90
    295.00
              .170E-98
                                       .795E+04
                                                  -.328E-90
                                                               .800E-86
                                                                            .114E+08
               .284-103
                           .000E+00
                                       .795E+04
                                                   .000E+00
        COMPUTED LATERAL FORCE AT PILE HEAD
                                                            -.27244E+02 KIP
        NO. OF ITERATIONS
        MAXIMUM DEFLECTION ERROR
                                          .938E-05 IN
                            SUMMARY TABLE
LATERAL
            BOUNDARY
                          AXIAL
                                                                   MAX.
                                                                                MAX.
 LOAD
(KIP)
          CONDITION
                           LOAD
                                                                  MOMENT
                                                                               STRESS
                                                     (IN/IN)
                          (KIP)
                                         (IN)
                                                                  (IN-KIP)
                                                                            (LBS/IN**2)
              BC2
              .200E+03
                                       .000E+00
                                                    -.254E-03
                          .124E+03
                                                                  .200E+03
-.109E+02
              .400E+03
                          .124E+03
                                       .000E+00
                                                    -.608E-03
                                                                  .400E+03
                                                                              .139E+05
 -.146E+02
              .600E+03
                          .124E+03
                                       .000E+00
                                                    -.101E-02
                                                                  .600E+03
                                                                              .169E+05
-.180E+02
              .800E+03
                          .124E+03
                                       000E+00
                                                    - 146E-02
                                                                  .800E+03
                                                                              199E+05
 -.213E+02
              .100E+04
                          .124E+03
                                       .000E+00
                                                    -.193E-02
                                                                  .100E+04
                                                                              .229E+05
                                                    -.243E-02
-.295E-02
 -.243E+02
              .120E+04
                          .124E+03
                                       .000E+00
                                                                  .120E+04
                                                                              .259E+05
-.272E+02
              .140E+04
                          .124E+03
                                       .000E+00
                                                                  .140E+04
                                                                              .289E+05
 -.301E+02
              .160E+04
                          .124E+03
                                       .000E+00
                                                    -.349E-02
                                                                  .160E+04
                                                                              .319E+05
                                                                  .180E+04
              .180E+04
-.328E+02
                          .124E+03
                                       .000E+00
                                                    -.404E-02
                                                                              .349E+05
                                                    -.461E-02
                                                                 .200E+04
 -.355E+02
              .200E+04
                          .124E+03
                                       .000E+00
                                                                              .378E+05
```

### **TEST5B.OUT**

```
EXAMPLE FOR DETERMINING PILE HEAD STIFFNESSES
    UNITS - - ENGL
         PILE DEFLECTION, BENDING MOMENT, SHEAR SOIL RESISTANCE
                          I N P U T I N F O R M A T I O N *****************************
    THE LOADING IS STATIC
    PILE GEOMETRY AND PROPERTIES
                                                      300.00 IN
         PILE LENGTH
                        1 SECTION(S)
         MODULUS OF ELASTICITY OF PILE = .290E+05 KIP/IN**2
                                  DIAMETER MOMENT OF
                                                    INERTIA
                                                     IN**4
                    300.00
                                     12.046
                                                   .127E+03
                                                                       .156E+02
                    300.00
    SOILS INFORMATION
         X-COORDINATE AT THE GROUND SURFACE = SLOPE ANGLE AT THE GROUND SURFACE =
          1 LAYER(S) OF SOIL
         LAYER 1
         THE LAYER IS A STIFF CLAY ABOVE THE WATER TABLE
         X AT THE TOP OF THE LAYER = .00 IN
X AT THE BOTTOM OF THE LAYER = 360.00 IN
         VARIATION OF SOIL MODULUS, k
                                              = .400E+03 LBS/IN**3
         DISTRIBUTION OF EFFECTIVE UNIT WEIGHT WITH DEPTH
                             2 POINTS
                               WEIGHT, LBS/IN**3
                    .00
                                     .69E-01
         DISTRIBUTION OF STRENGTH PARAMETERS WITH DEPTH
                             2 POINTS
                                C,LBS/IN**2
                      X,IN
                                                      PHI, DEGREES
                                    .140E+02
                                                      .000
                         . 00
                                                                       .700E-02
                                    .140E+02
    FINITE DIFFERENCE PARAMETERS
         NUMBER OF PILE INCREMENTS
TOLERANCE ON DETERMINATION OF DEFLECTIONS
                                                                            .100E-04 IN
         MAXIMUM NUMBER OF ITERATIONS ALLOWED FOR PILE ANALYSIS =
                                                                                .15E+03 IN
         MAXIMUM ALLOWABLE DEFLECTION
    INPUT CODES
         OUTPT = 1
         KCYCL =
         KBC
                    2
         KPYOP =
   EXAMPLE FOR DETERMINING PILE HEAD ROTATIONAL TRANS. STIFFNESSES
    UNITS--ENGL
                         OUTPUT INFORMATION
                              S U M M A R Y T A B L E
LATERAL
                           AXIAL
          CONDITION
BC2
                                                                     MOMENT STRESS (IN-KIP) (LBS/IN**2)
  LOAD
                            LOAD
 (KIP)
                                                       (IN/IN)
                            (KIP)
                                           (IN)
                                                      (1N/1N) (1N-K1P)

.278E-17 - .209E+03

-.555E-17 - .548E+03

-.111E-16 - .961E+03

.000E+00 - .143E+04

.222E-16 - .195E+04
  .100E+02
               .000E+00
                            .124E+03
                                        .322E-01
                                        .140E+00
  .200E+02
               .000E+00
                            .124E+03
                                                                                  .339E+05
  .300E+02
               .000E+00
                            .124E+03
                                        .330E+00
  .400E+02
               .000E+00
                            .124E+03
                                        .604E+00
                                                                                  .759E+05
  .500E+02
               .000E+00
                            .124E+03
                                        .964E+00
                                                      .222E-16 -.195E+04

-.888E-16 -.252E+04

.000E+00 -.312E+04

-.888E-16 -.375E+04

.000E+00 -.442E+04

.000E+00 -.516E+04
  .600E+02
.700E+02
              .000E+00
                           .124E+03
.124E+03
                                        .141E+01
.195E+01
                                                                                  .127E+06
              .000E+00
  .800E+02
                           .124E+03
                                        .258E+01
                                                                                  .186E+06
  .900E+02
                            .124E+03
                                        .330E+01
                                                                                  .217E+06
  .100E+03
              .000E+00
                            .124E+03
```

New: April 2000

### **TEST6B.OUT**

```
EXAMPLE FOR DETERMINING PILE HEAD STIFFNESSES
  UNITS - - ENGL
           PILE DEFLECTION, BENDING MOMENT, SHEAR SOIL RESISTANCE
                                                I N P U T I N F O R M A T I O N *****************************
 THE LOADING IS STATIC
  PILE GEOMETRY AND PROPERTIES
                                                                                                          300.00 IN
            PILE LENGTH
            MODULUS OF ELASTICITY OF PILE = .290E+05 KIP/IN**2
                                          1 SECTION(S)
                                                            DIAMETER MOMENT OF
                                                                                                   INERTIA
                                                                                                        IN**4
                                   300.00
                                                                      12.046 .127E+03
                                                                                                                                             .156E+02
                                   300.00
 SOILS INFORMATION
           X-COORDINATE AT THE GROUND SURFACE = SLOPE ANGLE AT THE GROUND SURFACE =
             1 LAYER(S) OF SOIL
            LAYER 1
            THE LAYER IS A STIFF CLAY ABOVE THE WATER TABLE
           X AT THE TOP OF THE LAYER = .00 IN
X AT THE BOTTOM OF THE LAYER = 360.00 IN
            VARIATION OF SOIL MODULUS, k
                                                                                      = .400E+03 LBS/IN**3
           DISTRIBUTION OF EFFECTIVE UNIT WEIGHT WITH DEPTH
                                                     2 POINTS
                                                         WEIGHT, LBS/IN**3
                                   .00
                                                                       .69E-01
           DISTRIBUTION OF STRENGTH PARAMETERS WITH DEPTH
                                      2 POINTS
                                                                                                   PHI, DEGREES
                                                        C,LBS/IN**2
                                                                   .140E+02
                                                                                                         .000
                                                                                                                                             .700E-02
                                                                   .140E+02
  FINITE DIFFERENCE PARAMETERS
           NUMBER OF PILE INCREMENTS
TOLERANCE ON DETERMINATION OF DEFLECTIONS
                                                                                                                                                       .100E-04 IN
            MAXIMUM NUMBER OF ITERATIONS ALLOWED FOR PILE ANALYSIS =
                                                                                                                                                              .15E+03 IN
           MAXIMUM ALLOWABLE DEFLECTION
  INPUT CODES
           OUTPT = 1
KCYCL = 1
            KBC
                           = 4
EXAMPLE FOR DETERMINING PILE HEAD ROTATIONAL TRANS. STIFFNESSES
 UNITS--ENGL
                                             O U T P U T I N F O R M A T I O N
  PILE LOADING CONDITION
          LATERAL DEFLECTION AT PILE HEAD = .000E+00 IN
APPLIED MOMENT AT PILE HEAD = .600E+03 IN-KIP
AXIAL LOAD AT PILE HEAD = .124E+03 KIP
                                                                          TOTAL
          X DEFLECTION MOMENT
                                                                                                          SHEAR
                                                                                                                                   SOIL
   | STRESS | LBS/IN | L
                                                                               STRESS
                                                                                                                                   RESIST
                                                                                                                                                           RIGIDITY
                                                                                                                                                             .368E+07
                                                                                                                                                            .368E+07
                                                                                                                                                             .368E+07
                                                                                                                                                           .368E+07
```

# Seismic Design - Section 6.1

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### Seismic Analysis Model

```
30 00
        - 308E-01
                      183E+03
                                  166E+05
                                             - 110E+02
                                                         - 229E+03
                                                                       368E+07
 35.00
         -.291E-01
                      .131E+03
                                  .141E+05
                                             -.986E+01
                                                         -.238E+03
                                                                       .368E+07
                                                                       .368E+07
 40.00
         -.264E-01
                      .841E+02
                                  .119E+05
                                             -.865E+01
                                                          -.244E+03
         -.233E-01
                      .435E+02
                                  .100E+05
                                             -.742E+01
                                                          -.247E+03
 45.00
         -.198E-01
                       901E+01
                                   .838E+04
                                             -.618E+01
                                                          - 248E+03
                                                                       .368E+07
 55.00
         -.162E-01
                     -.192E+02
                                  .886E+04
                                             -.494E+01
                                                          -.247E+03
                                                                       .368E+07
 60.00
         -.128E-01
                     -.413E+02
                                  .991E+04
                                             -.372E+01
                                                          -.242E+03
                                                                       .368E+07
                                                                       .368E+07
 65.00
         -.967E-02
                     -.573E+02
                                  .107E+05
                                             -.253E+01
                                                          -.235E+03
         -.692E-02
                      .673E+02
                                  .111E+05
                                                          -.224E+03
                                             -.138E+01
                                                                       .368E+07
 70.00
 75.00
          .462E-02
                       717E+02
                                  .114E+05
                                               .287E+00
                                                          -.210E+03
                                                                       .368E+07
         -.280E-02
                      .708E+02
 80.00
                                  .113E+05
                                              .723E+00
                                                          -.192E+03
                                                                       .368E+07
          .147E-02
                       650E+02
                                  .110E+05
                                                           169E+03
                                                                       .368E+07
 90.00
         -.571E-03
                      .550E+02
                                  .106E+05
                                              .241E+01
                                                          -.138E+03
                                                                       .368E+07
         -.459E-04
                     -.414E+02
                                   .991E+04
                                              .298E+01
                                                           .740E+02
                                                                       .368E+07
                                              .271E+01
                                                                       .368E+07
100.00
          .199E-03
                     -.266E+02
                                   .921E+04
                                                           113E+03
                                  .864E+04
105.00
          .262E-03
                     -.145E+02
                                              .211E+01
                                                          .125E+03
                                                                       .368E+07
                     -.549E+01
.461E+00
                                  .821E+04
.797E+04
110.00
          .225E-03
                                              .149E+01
                                                           .124E+03
                                                                       .368E+07
          .149E-03
                                              .896E+00
                                                          .115E+03
                                                                       .368E+07
115.00
          .759E-04
                      .356E+01
                                   .812E+04
                                               .358E+00
                                                           .995E+02
                                                                       .368E+07
125.00
          .255E-04
                      .417E+01
                                  .815E+04
                                             -.891E-01
                                                           .777E+02
                                                                       .368E+07
130.00
          .256E-05
                      .284E+01
                                  .808E+04
                                             -.406E+00
                                                          .444E+02
                                                                       .368E+07
135.00
         -.160E-05
                      747E+00
                                  798E+04
                                             - 319E+00
                                                          - 388E+02
                                                                       .368E+07
                      .308E+00
                                  .796E+04
                                                          .159E+02
140.00
         -.233E-06
                                              -.447E-01
                                                                       .368E+07
145.00
          .408E-11
                      .507E-03
                                  .795E+04
                                              .276E-01
                                                           .661E+00
                                                                       .368E+07
150.00
         -.109E-16
                     -.132E-08
                                  .795E+04
                                             -.481E-06
                                                          -.125E-04
                                                                       .368E+07
                                  .795E+04
                                              .128E-11
160.00
          .775E-28
                      .901E-20
                                  .795E+04
                                              -.343E-17
                                                           .104E-15
                                                                       .368E+07
         .207E-33
                      .235E-25
                                  .795E+04
                                              .914E-23
                                                          .299E-21
165.00
                                                                       .368E+07
170.00
         -.551E-39
                       613E-31
                                   .795E+04
                                             -.248E-31
                                                           .851E-27
                                                                       .368E+07
                                  .795E+04
175.00
          .147E-44
                                              .645E-37
                                                                       .368E+07
                      .160E-36
                                                          .241E-32
180.00
          .392E-50
                      .416E-42
.108E-47
                                  .795E+04
                                              .168E-42
                                                           .682E-38
                                                                       .368E+07
          .105E-55
185.00
                                              .438E-48
                                                          .192E-43
                                                                       .368E+07
         -.279E-61
                     -.281E-53
                                  .795E+04
                                              -.114E-53
                                                          -.539E-49
195.00
          .744E-67
                      .732E-59
                                  .795E+04
                                              .296E-59
                                                          .151E-54
                                                                       .368E+07
200.00
         -.198E-72
                     -.190E-64
                                  .795E+04
                                              -.770E-65
                                                                       .368E+07
                                                          -.421E-60
                                                                       .368E+07
205 00
          .529E-78
                      494E-70
                                  795E+04
                                              200E-70
                                                          117E-65
                                  .795E+04
210.00
         -.141E-83
                     -.128E-75
                                             -.519E-76
                                                          -.326E-71
                                                                       .368E+07
                      .332E-81
         .376E-89
-.100E-94
                                  .795E+04
215.00
                                              .135E-81
                                                          .905E-77
                                                                       .368E+07
                                                          -.251E-82
220.00
                     -.860E-87
                                             -.349E-87
                                                                       .368E+07
          .267-100
225.00
                      .223E-92
                                  .795E+04
                                              .904E-93
                                                          .694E-88
                                                                       .368E+07
                                                                       .368E+07
                                  .795E+04
230.00
          .713-106
                     -.576E-98
                                             -.234E-98
                                                           .192E-93
235.00
         .190-111
                      .149-103
                                              .605-104
                                                          .529E-99
                                                                       .368E+07
                                  .795E+04
240.00
         -.507-117
                     -.384-109
                                             -.156-109
                                                          -.146-104
                                                                       .368E+07
          .135-122
245.00
                      .992-115
                                              .403-115
                                                          .401-110
                                                                       .368E+07
                                  .795E+04
250.00
          .360-128
                     -.256-120
                                             -.104-120
                                                          -.110-115
                                                                       .368E+07
          .960-134
255.00
                      .658-126
                                              .268-126
                                                          .302-121
                                                                       .368E+07
                                             -.688-132
                                                                       .368E+07
265 00
          .682-145
                      .434-137
                                  .795E+04
                                              .177-137
                                                          227-132
         -.182-150
                     -.111-142
                                  .795E+04
270.00
                                             -.453-143
                                                          -.623-138
                                                                       .368E+07
                                                          .170-143
                      .285-148
275.00
          .484-156
                                  .795E+04
                                              .116-148
                                                                       .368E+07
                                  .795E+04
                                             -.297-154
         -.129-161
                     -.727-154
280.00
                                                          -.466-149
                                                                       .368E+07
285.00
         .344-167
                      .186-159
                                  .795E+04
                                              .758-160
                                                          .127-154
                                                                       .368E+07
                                  .795E+04
                                                          -.347-160
290.00
         -.916-173
                     -.472-165
                                             -.193-165
                                                                       .368E+07
         .244-178
                      .120-170
                                  .795E+04
                                              .491-171
300.00
         -.130-183
                      .000E+00
                                  .795E+04
                                              .000E+00
                                                        -.511-171
                                                                       .368E+07
    COMPUTED LATERAL FORCE AT PILE HEAD
                                                   = -.16245E+02 KIP
    NO. OF ITERATIONS
MAXIMUM DEFLECTION ERROR
                                     .989E-05 IN
                        SUMMARY TABLE
```

LATERAL	BOUNDARY	AXIAL			MAX.	MAX.
LOAD	CONDITION	LOAD	YT	ST	MOMENT	STRESS
(KIP)	BC2	(KIP)	(IN)	(IN/IN)	(IN-KIP)	(LBS/IN**2)
728E+0	1 .200E+03	.124E+03	.000E+00	711E-03	.200E+03	.174E+05
121E+0	2 .400E+03	.124E+03	.000E+00	171E-02	.400E+03	.269E+05
162E+0	2 .600E+03	.124E+03	.000E+00	286E-02	.600E+03	.364E+05
201E+0	2 .800E+03	.124E+03	.000E+00	411E-02	.800E+03	.459E+05
236E+0	2 .100E+04	.124E+03	.000E+00	545E-02	.100E+04	.554E+05
270E+0	2 .120E+04	.124E+03	.000E+00	686E-02	.120E+04	.649E+05
303E+0	2 .140E+04	.124E+03	.000E+00	834E-02	.140E+04	.743E+05
334E+0	2 .160E+04	.124E+03	.000E+00	987E-02	.160E+04	.838E+05
364E+0	2 .180E+04	.124E+03	.000E+00	115E-01	.180E+04	.933E+05
- 394E+0	2 200E+04	124E+03	000E+00	- 131E-01	200E+04	103E+0

From the above output, the stiffnesses of point element  $S_{33}$  (or S(3,3)),  $S_{35}$  (or S(3,5)),  $S_{55}$ ,  $S_{22}$ ,  $S_{26}$ , and  $S_{66}$  can be calculated as follows:

a) For S<sub>33</sub>:

Plastic moment  $M_{pye} = 1159.2 \text{ k-in.}$ 

$$M = \frac{M_{pye}}{2} = 579.6$$
 k-in, which is close to M=548 k-in in the SUMMARY

TABLE of TEST5B.OUT

$$S_{33} = \frac{P}{\delta_{ze}} = \frac{20kip}{0.14in} = 142.9 \text{ k/in}$$

b) For S<sub>35</sub>:

$$S_{35} = \frac{M}{\delta_{ze}} = \frac{548}{0.14} = 3914$$
 (kip/rad); in which  $\delta$  is the lateral displacement at pile head.

c) For S<sub>55</sub>:

Since 579.6 k-in is close to 600 k-in,  $S_{55}$  can be obtained from TEST6B.OUT as

X	MOMENT	FLEXURAL	DEFLECTION
		RIGIDITY	
IN	IN-KIP	KIP-IN**2	IN
****	*****	*****	******
.00	.600E+03	.368E+07	0.0
5.00	.521E+03	.368E+07	-0.123E-01
10.00	.445E+03	.368E+07	-0.211E-01
15.00	.372E+03	.368E+07	•
20.00	.304E+03	.368E+07	_

Total rotation at top of the pile is  $\theta_{ye} = \frac{0.0123}{5} = 0.0025$  rad.

$$S_{55} = \frac{M}{\theta_{ve}} = \frac{600}{0.0025} = 240000 \text{(k-in/rad.)}$$

$$S_{53} = \frac{P}{\theta_{ve}} = \frac{16.2}{0.0025} = 6480 \text{(kip/rad.)}$$

Since the program performs structural analysis using symmetric stiffness matrix, use average number for  $S_{35}$  and  $S_{53}$  approximately:  $S_{35} = S_{53} = \frac{3914 + 6480}{2} = 5200$  (kip/rad.)

d) For S<sub>22</sub>:

Plastic moment M<sub>pze</sub>= 2664 kip-in.

M= 
$$\frac{M_{pze}}{2}$$
 = 1332 kip-in. (From TEST5.OUT SUMMARY TABLE, it is between 1100 k-in. and 1630 k-in.)

$$\frac{1332 - 1100}{1630 - 1100} = \frac{232}{530} = 0.438$$

$$S_{22} = \frac{P}{\delta_{ye}} = \frac{30 + (0.438)(10)}{0.159 + (0.438)(0.289 - .159)} = \frac{34.38}{0.216} = 159.2 \text{ (kip/in.)}$$

e) For S<sub>26</sub>:

$$S_{26} = \frac{M}{\delta_{ye}} = \frac{-1332}{0.216} = -6166$$
 (kip/rad.)

f) For S<sub>66</sub>:

Since 1332 k-in. is closer to 1400 k-in., the  $S_{\rm 66}$  can be obtained from TEST6.OUT as

X	MOMENT	FLEXURAL	DEFLECTION
		RIGIDITY	
IN	IN-KIP	KIP-IN**2	IN
****	******	******	******
.00	.140E+04	.114E+08	0.0
5.00	.127E+04	.114E+08	-0.132E-01
10.00	.114E+04	.114E+08	-0.237E-01
15.00	.101E+04	.114E+08	•
20.00	.886E+03	.114E+08	

Total rotation at top of the pile  $\theta_{ze} = \frac{0.0132}{5} = 0.0026$  rad.

$$S_{66} = \frac{M}{\theta_{ze}} = \frac{1400}{0.0026} = 538460 \text{ k-in./rad.}$$

$$S_{62} = \frac{-P}{\theta_{z_e}} = \frac{-27.2}{0.0026} = -10460 \text{ kip/rad.}$$

Since the program performs structural analysis using symmetric stiffness matrix, use average number for  $S_{62}$  and  $S_{26}$  approximately:  $S_{26} = S_{62} = \frac{-6166-10460}{2} = -8313$  (kip/rad.)

- g) For axial stiffness S<sub>11</sub>:  $\frac{AE}{L} = \frac{(15.5)(29000)}{(25)(12)} = 1498.33$  kip/in
- h) For torsional stiffness  $S_{44}$ :  $\frac{GJ}{L} = \frac{(11100)(1.12)}{(25)(12)} = 41.44$  kip-in/rad. Usually, the torsional effect of an individual pile is insignificant for the multiple-column bent

Therefore, the stiffness matrix of the pile at the groundline level corresponding to the pile element coordinate system  $(x_e, y_e, z_e)$  is:

$$\mathsf{K}_{\mathsf{pile}} = \begin{bmatrix} \mathsf{S}_{11} & 0 & 0 & 0 & 0 & 0 \\ & \mathsf{S}_{22} & 0 & 0 & 0 & \mathsf{S}_{26} \\ & & \mathsf{S}_{33} & 0 & \mathsf{S}_{35} & 0 \\ & & & \mathsf{S}_{44} & 0 & 0 \\ \mathsf{Symm} & & & \mathsf{S}_{55} & 0 \\ & & & \mathsf{S}_{66} \end{bmatrix}$$

$$= \begin{bmatrix} 1498.3 & 0 & 0 & 0 & 0 & 0 \\ & 159.2 & 0 & 0 & 0 & -8313 \\ & & 142.9 & 0 & 5200 & 0 \\ & & 41.44 & 0 & 0 \\ & & & 240000 & 0 \\ & & & 538460 \end{bmatrix}$$

## **Pile Group Effects:**

Design pile footings with a center to center spacing of more than or equal to 3 pile diameters.

For center to center pile spacing of 3 pile diameters, it is suggested that a p multiplier,  $P_m$ , value of 0.8 be used to modify the p-y curve of individual piles along the lead row, 0.4 for the second row, and 0.3 for the third and subsequent rows. For larger center to center spacings, these  $P_m$  values should be conservative. Alternatively, using a  $P_m = 0.5$  for all piles to represent the average adjustment factor is adequate in practical design for earthquake loadings. For center to center pile spacings of 6 pile diameters, the pile group effect can be neglected. For pile spacings between 3 and 6 pile diameters, us a linear interpolation between p multipliers of 0.5 and 1.0.

# p-y Curves for Liquefied Soil:

The p-multiplier of 0.1 can be used for liquefied soil (MCEER Report 98-0018, 1998). If p-multipliers are not used, the residual shear strength of the liquefied soil can be used in accordance with Section 6.1.2.5 where the soil type is determined from the residual shear strength and the corresponding soil parameters in Table 6.1.2.4-2 can be used for the p-y analysis.

#### 2.6.5 - Pile Lateral and Rotational Stiffness- Linear Subgrade Modulus Method

The lateral load-deflection characteristics of the pile-soil system are mildly nonlinear. The elastic pile usually dominates the nonlinear soil stiffness. Furthermore, the significant soil-pile interaction zone is usually confined to a depth at the upper 5 to 10 pile diameters. Therefore, simplified single-layer pile-head stiffness design charts are appropriate for lateral loading. The stiffness charts shown in figures 6.1.2.6.5-1 - 6.1.2.6.5-4 make use of a discrete Winkler spring soil model in which stiffness increases linearly with depth from zero at grade level where the location of the pile head is This linear subgrade stiffness model has been found to assumed. reasonably fit pile load test data for both sand and clay soil conditions. The coefficient f in these figures is used to define the subgrade modulus E<sub>s</sub> at depth z, representing the soil stiffness per unit pile length. Figures 6.1.2.6.5-5 and 6.1.2.6.5-6 show f values for piles embedded in sand and clay respectively (assuming elastic pile). For the purpose of selecting an appropriate f value, the soil condition at the upper 5 pile diameters should be used.

These stiffness charts are appropriate for piles with embedded length greater than 3 times the pile characteristic length,  $\lambda$ . The following equation can be used to obtain the characteristic length of pile-soil system:

$$\lambda = \sqrt[5]{\frac{EI_p}{f}} \tag{1}$$

### **Embedment Effect**

Soil resistance on the pile increases and the stiffness coefficients at the pile head increase with the depth of embedment due to additional overburden. Figures 6.1.2.6.5-7 – 6.1.2.6.5-9 present pile head stiffness coeficients for pile embedment depths of 5 and ten feet based on a subgrade modulus, which increases linearly with depth.

#### Pile Response and Load Distribution

The pile lateral and moment distribution can be estimated by the equations shown in the Figures 6.1.2.6.5-10 and 6.1.2.6.5-11 for non-embedded and embedded piles respectively. In the figures, the A and B shape functions are non-dimensional and can be used to solve for the pile deflections and moments along the pile including the fixed pile head condition. Tables 6.1.2.6.5-1-6.1.2.6.5-7 give the data of the shape functions.

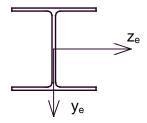
### Example 1:

Find the stiffness matrix of a vertical pile shown in Figure 6.1.2.6.4-1 at the groundline level.

Page 2.6.5-2

Seismic Analysis Model

#### Solution:



1) Calculate 
$$S_{33}$$
:  
 $El_y = 29000$ ksi x  $127$ in<sup>4</sup> =  $3.6$ x $10^9$  # - in<sup>4</sup>

From Figure 6.1.2.6.5-6: for clay with undrained shear strength of 2ksf, f = 32pci

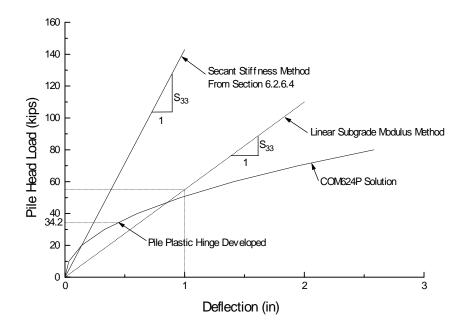
From Figure 6.1.2.6.5-1, using EI = 
$$3.6x10^9 \# - in^2$$
 and  $f = 32$  pci,  $S_{33} = 5.5x10^4 \text{ lb/in}$ 

- 2) Calculate  $S_{55}$ : From Figure 6.1.2.6.5-2, using the same EI and f as in 1),  $S_{55} = 1.2 \times 10^8$  lb-in/rad. = 120000 k-in/rad.
- 3) Calculated  $S_{35}$ : From Figure 6.1.2.6.5-3, using the same EI and f as 1),  $S_{35} = 2.2 \times 10^6$  lb/rad. = 2200 k/rad.
- 4) Calculate  $S_{22}$ :  $EI_z = 11397000 \text{ k-in}^2 = 1.1 \times 10^{10} \text{ #-in}^2$ From Figure 6.1.2.6.5-1, using new EI and the same f as above:  $S_{22} = 8.5 \times 10^4 \text{ lb/in}$
- 5) Calculate  $S_{66}$ : From Figure 6.1.2.6.5-2, using the same EI and f from 4):  $S_{66} = 2.7 \times 10^8$  lb-in/rad. = 270000 k-in/rad.
- 6) Calculate  $S_{26}$ : From Figure 6.1.2.6.5-3, using the same EI and f from 4):  $S_{26} = 4 \times 10^6$  lb/rad. = 4000 k/rad.
- 7)  $S_{11}$  and  $S_{44}$  are the same as calculated in Example 1 in Section 6.1.2.6.4.

The completed stiffness matrix is as follows:

$$\mathsf{K}_{\mathsf{pile}} = \begin{bmatrix} \mathsf{S}_{11} & 0 & 0 & 0 & 0 & 0 \\ & \mathsf{S}_{22} & 0 & 0 & 0 & \mathsf{S}_{26} \\ & & \mathsf{S}_{33} & 0 & \mathsf{S}_{35} & 0 \\ & & & \mathsf{S}_{44} & 0 & 0 \\ \mathsf{Symm}. & & & \mathsf{S}_{55} & 0 \\ & & & & \mathsf{S}_{66} \end{bmatrix} = \begin{bmatrix} 1498.33 & 0 & 0 & 0 & 0 & 0 & 0 \\ & 85 & 0 & 0 & 0 & -4000 \\ & & & 550 & 0 & 2200 & 0 \\ & & & & 41.44 & 0 & 0 \\ \mathsf{Symm}. & & & 120000 & 0 \\ & & & & 270000 \end{bmatrix}$$

In comparison with the stiffness matrix calculated in Example 1 from Section 6.1.2.6.4, there are some discrepancies between the two matrices. The reason for the discrepancies is because the linear subgrade modulus method (Lam, et al, 1991) is originally derived using a 1 inch deflection of the pile head in clay as shown on the figure below.



From the above figure, it is recommended using the secant stiffness approach for the pile stiffness estimation as described in Section 6.1.2.6.4. If a p-y curve based computer program is not available, the linear subgrade modulus method may be used to estimate pile stiffness and moment distribution along a pile. However, using the linear subgrade modulus method may result in a significant underestimation of pile stiffness when a dynamic structural analysis shows that pile deflection is much less than 1 inch.

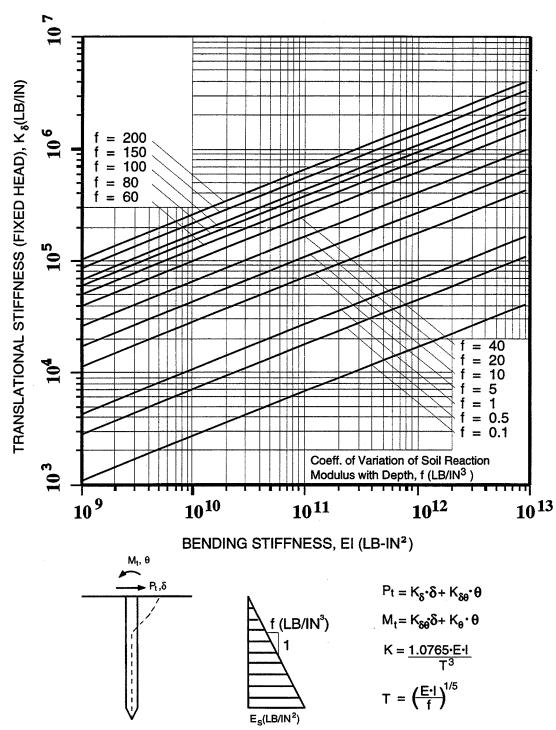


Figure 6.1.2.6.5-1 Lateral Pile Head Stiffness (Fixed -Head Condition)

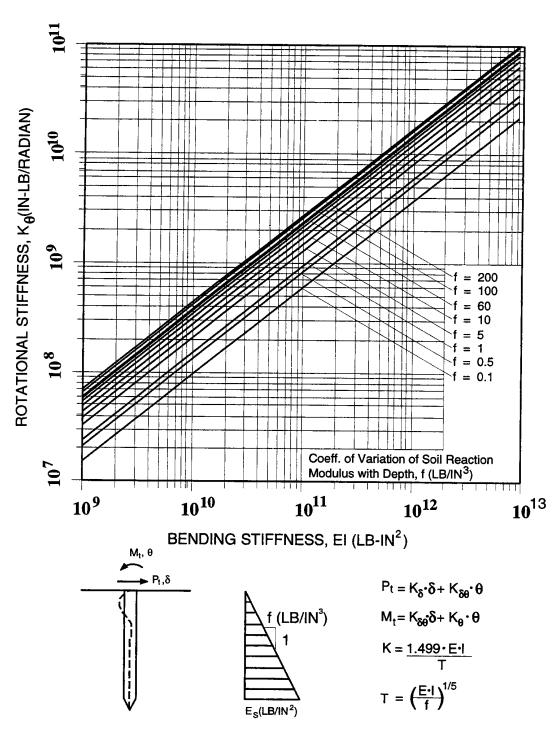


Figure 6.1.2.6.5-2 Rotational Pile-Head Stiffness

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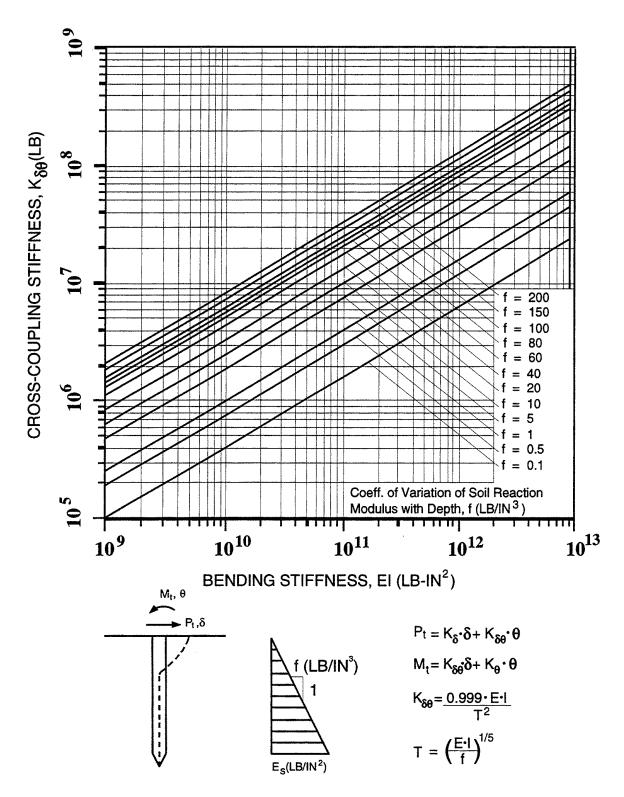


Figure 6.1.2.6.5-3 Cross-Coupling Pile-Head Stiffness

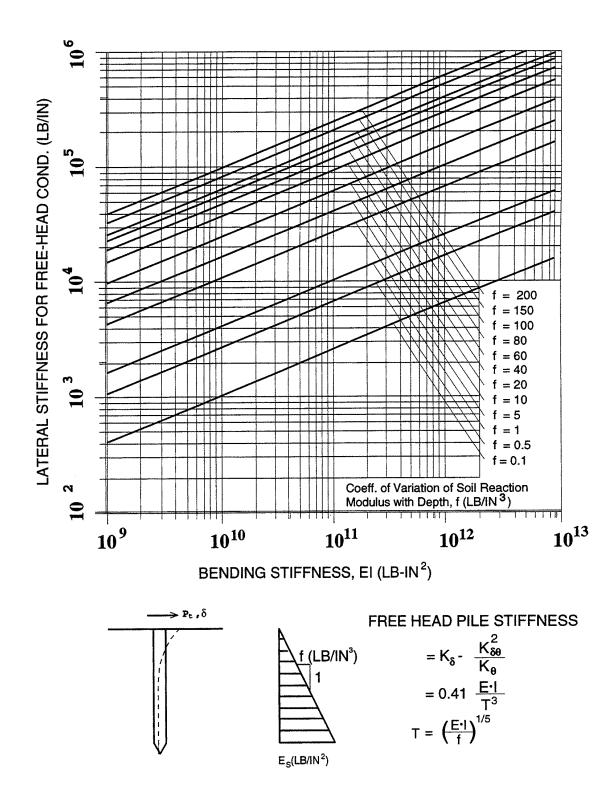


Figure 6.1.2.6.5-4 Lateral Pile-Head Stiffness (Free-Head Condition)

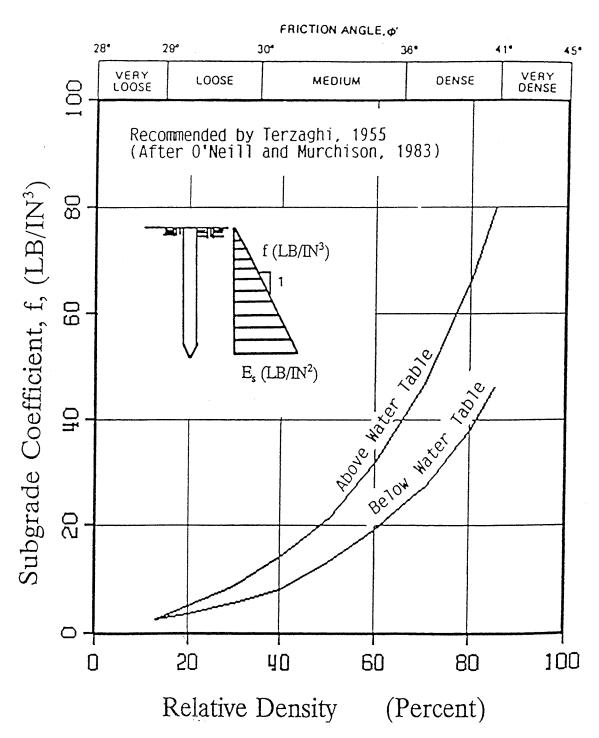


Figure 6.1.2.6.5-5 Recommended Coefficient f of Variation in Subgrade Modulus with Depth for Sand

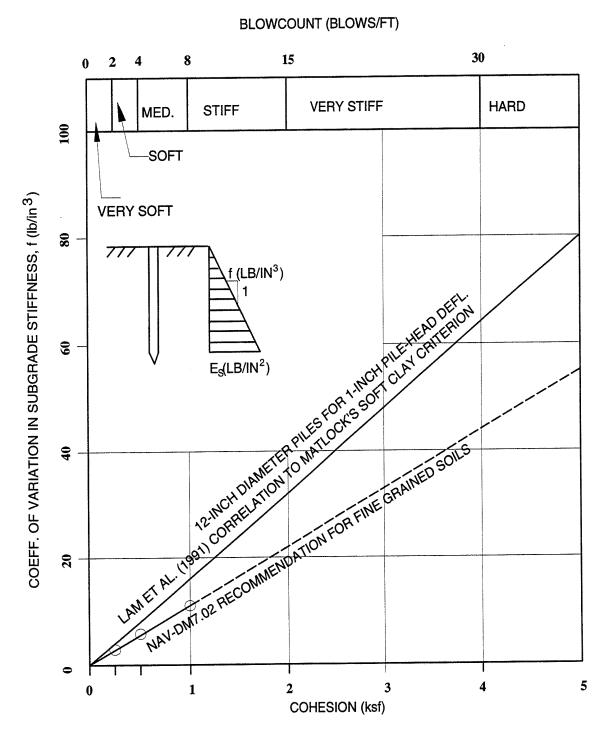
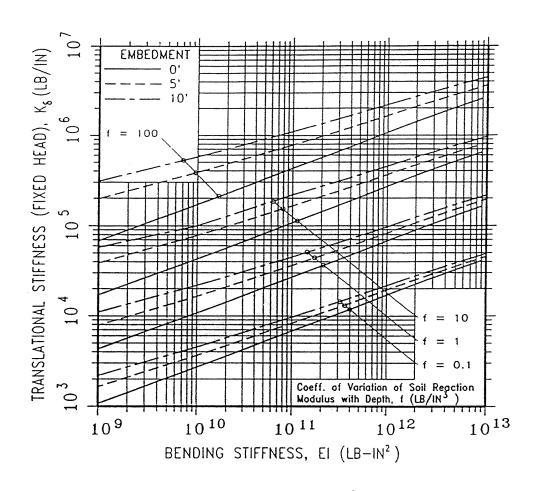
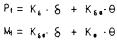


Figure 6.1.2.6.5-6 Recommended Coefficient f of Variation in Subgrade Modulus with Depth for Clay





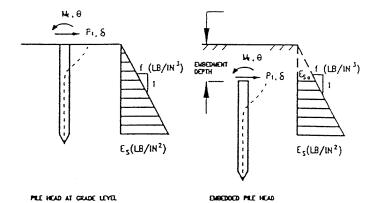
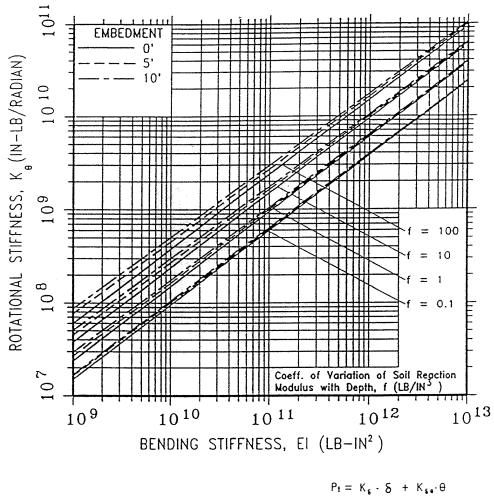
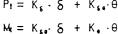


Figure 6.1.2.6.5-7 Lateral Embedded Pile-Head Stiffness





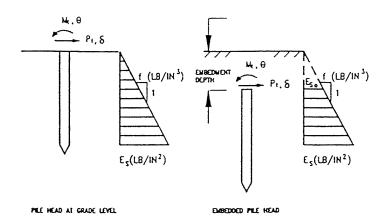


Figure 6.1.2.6.5-8 Embedded Pile-Head Rotational Stiffness

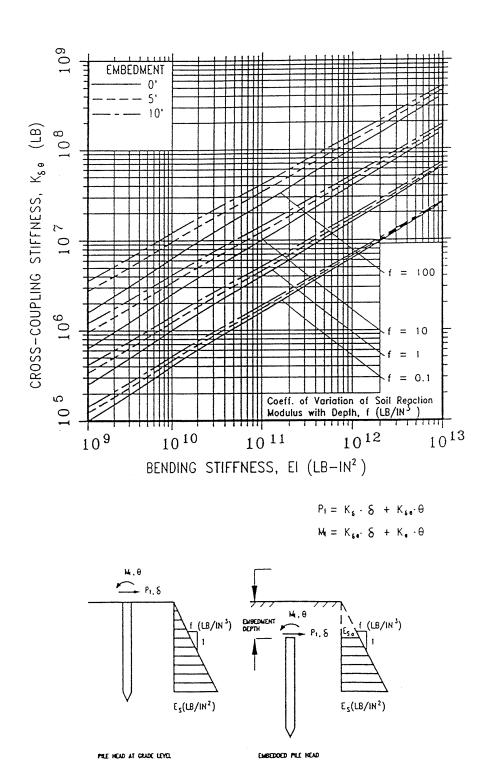
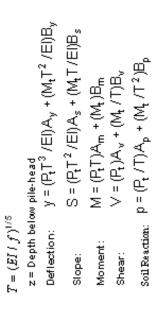
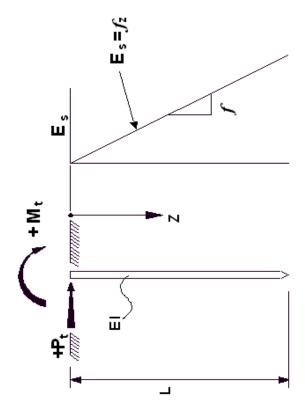


Figure 6.1.2.6.5-9 Embedded Pile Cross-Coupling Pile-Head Stiffness





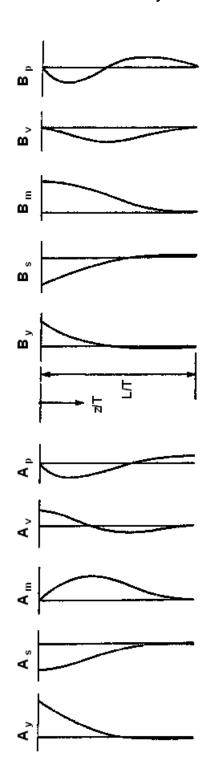
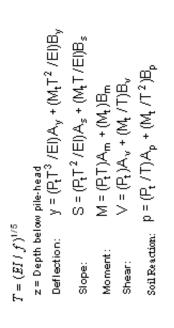
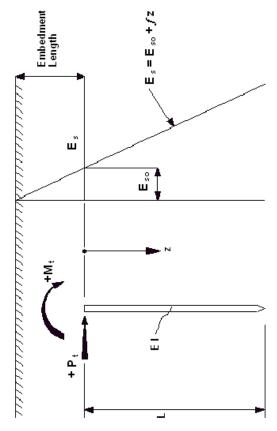


Figure 6.1.2.6.5-10 Linear Pile Solution for Pile-Head at Groundline (see Table 6.1.2.6.5-1)





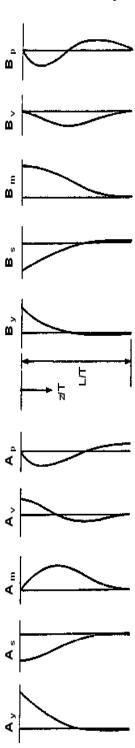


Figure 6.1.2.6.5-11 Linear Pile Solution for Embedded Piles (see Tables 6.1.2.6.5-2 through 7)

z/T	A <sub>y</sub>	As	A <sub>m</sub>	$A_{v}$	Ap	B <sub>y</sub>	B <sub>s</sub>	$B_{m}$	B <sub>v</sub>	$B_p$	z/T
0.0	2.435	-1.623	0.000	1.000	0.000	1.623	-1.749	1.000	0.000	0.000	0.0
0.1	2.273	-1.618	0.100	0.988	-0.227	1.453	-1.649	1.000	-0.007	-0.145	0.1
0.2	2.112	-1.603	0.198	0.956	-0.422	1.293	-1.549	0.999	-0.028	-0.259	0.2
0.3	1.952	-1.578	0.291	0.906	-0.586	1.143	-1.450	0.994	-0.058	-0.343	0.3
0.4	1.796	-1.545	0.379	0.840	-0.718	1.003	-1.351	0.987	-0.095	-0.401	0.4
0.5	1.643	-1.503	0.459	0.763	-0.822	0.873	-1.253	0.976	-0.137	-0.436	0.5
0.6	1.495	-1.453	0.531	0.677	-0.897	0.752	-1.156	0.960	-0.181	-0.451	0.6
0.7	1.353	-1.397	0.595	0.585	-0.947	0.641	-1.061	0.939	-0.226	-0.449	0.7
0.8	1.216	-1.335	0.649	0.489	-0.973	0.540	-0.968	0.914	-0.270	-0.432	0.8
0.9	1.086	-1.268	0.693	0.392	-0.977	0.448	-0.878	0.885	-0.312	-0.403	0.9
1.0	0.962	-1.197	0.727	0.295	-0.962	0.364	-0.791	0.852	-0.350	-0.364	1.0
1.2	0.738	-1.047	0.767	0.109	-0.885	0.223	-0.628	0.775	-0.414	-0.267	1.2
1.4	0.544	-0.893	0.772	-0.056	-0.761	0.112	-0.482	0.688	-0.456	-0.157	1.4
1.6	0.381	-0.741	0.746	-0.193	-0.609	0.029	-0.354	0.594	-0.477	-0.046	1.6
1.8	0.247	-0.596	0.696	-0.299	-0.445	-0.030	-0.245	0.498	-0.476	0.055	1.8
2.0	0.141	-0.464	0.628	-0.371	-0.283	-0.070	-0.155	0.404	-0.456	0.140	2.0
2.5	-0.020	-0.200	0.422	-0.424	0.049	-0.105	-0.006	0.200	-0.350	0.263	2.5
3.0	-0.075	-0.040	0.225	-0.349	0.226	-0.089	0.057	0.059	-0.213	0.268	3.0
3.5	-0.074	0.034	0.081	-0.223	0.257	-0.057	0.065	-0.016	-0.095	0.200	3.5
4.0	-0.050	0.052	0.000	-0.106	0.201	-0.028	0.049	-0.042	-0.017	0.113	4.0
4.5	-0.026	0.042	-0.032	-0.027	0.117	-0.009	0.028	-0.039	0.021	0.041	4.5
5.0	-0.009	0.025	-0.033	0.013	0.046	0.000	0.011	-0.026	0.029	0.002	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Table 6.1.2.6.5-1 Linear Elastic Pile Solution,  $E_s = f z$ 

z/T	A <sub>y</sub>	As	$A_{m}$	A <sub>v</sub>	Ap	B <sub>y</sub>	Bs	B <sub>m</sub>	B <sub>v</sub>	B <sub>p</sub>	z/T
0.0	2.151	-1.468	0.000	1.000	-0.215	1.468	-1.660	1.000	0.000	-0.147	0.0
0.1	2.004	-1.463	0.099	0.969	-0.401	1.307	-1.560	0.999	-0.021	-0.261	0.1
0.2	1.858	-1.449	0.194	0.921	-0.557	1.156	-1.460	0.996	-0.051	-0.347	0.2
0.3	1.714	-1.425	0.283	0.859	-0.686	1.015	-1.361	0.989	-0.089	-0.406	0.3
0.4	1.573	-1.393	0.366	0.786	-0.786	0.884	-1.263	0.978	-0.131	-0.442	0.4
0.5	1.435	-1.352	0.440	0.703	-0.861	0.763	-1.166	0.963	-0.176	-0.458	0.5
0.6	1.302	-1.305	0.506	0.615	-0.912	0.651	-1.070	0.943	-0.222	-0.456	0.6
0.7	1.174	-1.251	0.563	0.522	-0.940	0.549	-0.977	0.919	-0.266	-0.439	0.7
0.8	1.052	-1.193	0.611	0.428	-0.947	0.456	-0.887	0.890	-0.309	-0.410	0.8
0.9	0.936	-1.130	0.649	0.333	-0.936	0.371	-0.800	0.857	-0.348	-0.371	0.9
1.0	0.826	-1.063	0.677	0.241	-0.909	0.296	-0.716	0.820	-0.383	-0.325	1.0
1.2	0.627	-0.925	0.708	0.068	-0.815	0.168	-0.560	0.738	-0.437	-0.219	1.2
1.4	0.456	-0.783	0.706	-0.082	-0.685	0.071	-0.421	0.646	-0.470	-0.106	1.4
1.6	0.314	-0.644	0.676	-0.204	-0.534	-0.001	-0.302	0.551	-0.480	0.002	1.6
1.8	0.198	-0.514	0.626	-0.295	-0.377	-0.051	-0.201	0.455	-0.470	0.097	1.8
2.0	0.108	-0.395	0.560	-0.355	-0.226	-0.082	-0.119	0.364	-0.443	0.173	2.0
2.5	-0.027	-0.163	0.367	-0.389	0.071	-0.105	0.012	0.169	-0.326	0.273	2.5
3.0	-0.071	-0.026	0.189	-0.310	0.219	-0.084	0.061	0.041	-0.189	0.260	3.0
3.5	-0.065	0.035	0.063	-0.192	0.235	-0.051	0.063	-0.024	-0.077	0.184	3.5
4.0	-0.043	0.047	-0.006	-0.087	0.177	-0.024	0.045	-0.043	-0.007	0.097	4.0
4.5	-0.022	0.037	-0.030	-0.018	0.099	-0.007	0.024	-0.037	0.024	0.030	4.5
5.0	-0.007	0.021	-0.030	0.015	0.036	0.001	0.009	-0.023	0.029	-0.007	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Table 6.1.2.6.5-2 Linear Elastic Solution,  $E_s = E_{so} + f z$  where  $E_{so}/(f T) = 0.1$ 

	_	_	_		_	_		_			
z/T	$A_{y}$	As	$A_{m}$	$A_{v}$	$A_p$	$B_{y}$	B <sub>s</sub>	$B_{m}$	$B_v$	$B_p$	z/T
0.0	1.930	-1.348	0.000	1.000	-0.386	1.348	-1.589	1.000	0.000	-0.270	0.0
0.1	1.796	-1.343	0.098	0.954	-0.539	1.194	-1.489	0.999	-0.031	-0.358	0.1
0.2	1.662	-1.329	0.191	0.894	-0.665	1.050	-1.390	0.994	-0.070	-0.420	0.2
0.3	1.530	-1.305	0.277	0.822	-0.765	0.916	-1.291	0.985	-0.114	-0.458	0.3
0.4	1.401	-1.274	0.355	0.742	-0.840	0.792	-1.193	0.971	-0.161	-0.475	0.4
0.5	1.275	-1.235	0.425	0.655	-0.893	0.678	-1.097	0.952	-0.208	-0.474	0.5
0.6	1.154	-1.189	0.486	0.565	-0.923	0.573	-1.003	0.929	-0.255	-0.458	0.6
0.7	1.037	-1.138	0.538	0.472	-0.933	0.477	-0.911	0.902	-0.299	-0.430	0.7
0.8	0.926	-1.082	0.581	0.379	-0.926	0.391	-0.823	0.869	-0.340	-0.391	8.0
0.9	0.821	-1.022	0.614	0.287	-0.903	0.313	-0.737	0.833	-0.377	-0.344	0.9
1.0	0.722	-0.960	0.638	0.199	-0.866	0.243	-0.656	0.794	-0.409	-0.292	1.0
1.2	0.543	-0.829	0.661	0.036	-0.760	0.127	-0.506	0.707	-0.456	-0.178	1.2
1.4	0.390	-0.698	0.654	-0.103	-0.624	0.040	-0.374	0.613	-0.480	-0.064	1.4
1.6	0.263	-0.570	0.621	-0.213	-0.474	-0.023	-0.261	0.516	-0.482	0.042	1.6
1.8	0.162	-0.450	0.570	-0.292	-0.323	-0.065	-0.167	0.421	-0.465	0.131	1.8
2.0	0.083	-0.343	0.506	-0.343	-0.182	-0.091	-0.092	0.331	-0.431	0.200	2.0
2.5	-0.033	-0.135	0.324	-0.360	0.088	-0.104	0.024	0.145	-0.306	0.280	2.5
3.0	-0.066	-0.015	0.161	-0.279	0.213	-0.079	0.064	0.026	-0.170	0.253	3.0
3.5	-0.059	0.036	0.049	-0.168	0.217	-0.046	0.061	-0.030	-0.063	0.171	3.5
4.0	-0.038	0.044	-0.009	-0.073	0.158	-0.020	0.042	-0.044	0.001	0.085	4.0
4.5	-0.018	0.033	-0.029	-0.012	0.085	-0.005	0.021	-0.035	0.026	0.022	4.5
5.0	-0.005	0.018	-0.027	0.015	0.029	0.002	0.007	-0.021	0.028	-0.011	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Table 6.1.2.6.5-3 Linear Elastic Pile Solution,  $E_s = E_{so} + f z$  where  $E_{so}/(f T) = 0.2$ 

-											
z/T	$A_{y}$	As	$A_{m}$	$A_{v}$	$A_p$	B <sub>y</sub>	B <sub>s</sub>	$B_{m}$	$B_v$	$B_p$	z/T
0.0	1.490	-1.104	0.000	1.000	-0.745	1.104	-1.439	1.000	0.000	-0.552	0.0
0.1	1.380	-1.099	0.096	0.921	-0.828	0.965	-1.339	0.997	-0.057	-0.579	0.1
0.2	1.270	-1.085	0.184	0.836	-0.889	0.836	-1.240	0.989	-0.115	-0.585	0.2
0.3	1.163	-1.063	0.263	0.745	-0.930	0.717	-1.142	0.974	-0.173	-0.574	0.3
0.4	1.058	-1.033	0.333	0.651	-0.952	0.608	-1.046	0.954	-0.229	-0.547	0.4
0.5	0.956	-0.997	0.394	0.555	-0.956	0.508	-0.951	0.929	-0.281	-0.508	0.5
0.6	0.858	-0.955	0.444	0.460	-0.944	0.417	-0.860	0.898	-0.330	-0459	0.6
0.7	0.765	-0.908	0.486	0.367	-0.918	0.336	-0.772	0.863	-0.373	-0.403	0.7
0.8	0.677	-0.858	0.518	0.277	-0.880	0.263	-0.688	0.823	-0.410	-0.342	8.0
0.9	0.593	-0.805	0.541	0.192	-0.831	0.198	-0.608	0.781	-0.441	-0.278	0.9
1.0	0.516	-0.750	0.556	0.112	-0.773	0.141	-0.532	0.735	-0.466	-0.212	1.0
1.2	0.377	-0.638	0.564	-0.030	-0.640	0.049	-0.394	0.638	-0.495	-0.084	1.2
1.4	0.260	-0.527	0.545	-0.144	-0.495	-0.017	-0.277	0.538	-0.500	0.033	1.4
1.6	0.166	-0.421	0.508	-0.228	-0.348	-0.062	-0.179	0.439	-0.483	0.131	1.6
1.8	0.091	-0.325	0.456	-0.284	-0.210	-0.090	-0.100	0.346	-0.449	0.207	1.8
2.0	0.035	-0.240	0.395	-0.313	-0.088	-0.103	-0.040	0.260	-0.403	0.259	2.0
2.5	-0.041	-0.082	0.238	-0.298	0.124	-0.098	0.046	0.094	-0.259	0.295	2.5
3.0	-0.058	0.003	0.108	-0.212	0.203	-0.068	0.066	0.000	-0.124	0.238	3.0
3.5	-0.047	0.035	0.027	-0.126	0.187	-0.037	0.055	-0.037	-0.040	0.147	3.5
4.0	-0.028	0.036	-0.015	-0.048	0.125	-0.014	0.035	-0.042	0.012	0.064	4.0
4.5	-0.012	0.025	-0.026	-0.002	0.061	-0.002	0.016	-0.031	0.029	0.009	4.5
5.0	-0.003	0.013	-0.022	0.016	0.015	0.003	0.004	-0.017	0.026	-0.016	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Table 6.1.2.6.5-4 Linear Elastic Pile Solution,  $E_s = E_{so} + f z$  where  $E_{so}/(fT) = 0.5$ 

z/T	A <sub>y</sub>	As	A <sub>m</sub>	$A_{v}$	Ap	B <sub>y</sub>	B <sub>s</sub>	B <sub>m</sub>	B <sub>v</sub>	B <sub>p</sub>	z/T
0.0	1.097	-0.879	0.000	1.000	-1.097	0.879	-1.290	1.000	0.000	-0.879	0.0
0.1	1.010	-0.874	0.095	0.890	-1.111	0.755	-1.190	0.996	-0.086	-0.830	0.1
0.2	0.923	-0.861	0.178	0.779	-1.107	0.641	-1.091	0.983	-0.165	-0.769	0.2
0.3	0.837	-0.839	0.250	0.669	-1.089	0.537	-0.994	0.963	-0.239	-0.698	0.3
0.4	0.755	-0.811	0.312	0.562	-1.057	0.442	-0.899	0.935	-0.305	-0.619	0.4
0.5	0.675	-0.777	0.363	0.458	-1.013	0.357	-0.807	0.902	-0.362	-0.535	0.5
0.6	0.599	-0.739	0.403	0.360	-0.959	0.281	-0.719	0.863	-0.411	-0.449	0.6
0.7	0.527	-0.697	0.435	0.267	-0.897	0.213	-0.635	0.819	-0.452	-0.362	0.7
0.8	0.460	-0.653	0.457	0.181	-0.828	0.153	-0.556	0.772	-0.484	-0.276	0.8
0.9	0.397	-0.606	0.471	0.102	-0.754	0.102	-0.481	0.723	-0.507	-0.193	0.9
1.0	0.339	-0.559	0.477	0.030	-0.677	0.057	-0.411	0.671	-0.523	-0.115	1.0
1.2	0.236	-0.464	0.470	-0.090	-0.520	-0.012	-0.288	0.565	-0.531	0.026	1.2
1.4	0.153	-0.372	0.443	-0.178	-0.367	-0.059	-0.185	0.460	-0.514	0.141	1.4
1.6	0.087	-0.288	0.400	-0.238	-0.227	-0.087	-0.103	0.360	-0.477	0.226	1.6
1.8	0.037	-0.213	0.349	-0.270	-0.105	-0.101	-0.040	0.269	-0.426	0.283	1.8
2.0	0.001	-0.149	0.293	-0.281	-0.004	-0.104	-0.005	0.190	-0.366	0.312	2.0
2.5	-0.042	-0.036	0.160	-0.240	0.146	-0.084	0.061	0.047	-0.210	0.295	2.5
3.0	-0.044	0.017	0.060	-0.156	0.177	-0.051	0.064	-0.025	-0.083	0.205	3.0
3.5	-0.031	0.031	0.003	-0.075	0.139	-0.023	0.045	-0.045	-0.006	0.105	3.5
4.0	-0.016	0.026	-0.019	-0.020	0.081	-0.006	0.024	-0.038	0.026	0.031	4.0
4.5	-0.006	0.016	-0.021	0.008	0.031	0.002	0.009	-0.023	0.030	-0.009	4.5
5.0	0.000	0.007	-0.014	0.015	0.002	0.004	0.000	-0.010	0.022	-0.022	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Figure 6.1.2.6.5-5 Linear Elastic Pile Solution,  $E_s = E_{so} + f z$  where  $E_{so}/(f T) = 1.0$ 

	1	1					1				
z/T	$A_{y}$	$A_s$	$A_{m}$	$A_{v}$	$A_p$	$B_{y}$	B <sub>s</sub>	$B_{m}$	$B_v$	$B_p$	z/T
0.0	0.742	-0.663	0.000	1.000	-1.483	0.663	-1.130	1.000	0.000	-1.327	0.0
0.1	0.675	-0.659	0.093	0.855	-1.418	0.555	-1.030	0.993	-0.125	-1.166	0.1
0.2	0.610	-0.646	0.171	0.717	-1.342	0.457	-0.932	0.975	-0.233	-1.006	0.2
0.3	0.546	-0.625	0.236	0.587	-1.256	0.369	-0.836	0.947	-0.326	-0.849	0.3
0.4	0.485	-0.599	0.288	0.466	-1.163	0.290	-0.743	0.910	-0.403	-0.697	0.4
0.5	0.426	-0.568	0.329	0.355	-1.066	0.220	-0.654	0.866	-0.466	-0.551	0.5
0.6	0.371	-0.534	0.359	0.253	-0.965	0.159	-0.570	0.817	-0.514	-0.414	0.6
0.7	0.320	-0.497	0.380	0.162	-0.863	0.107	-0.491	0.763	-0.549	-0.288	0.7
0.8	0.272	-0.458	0.392	0.080	-0.761	0.061	-0.417	0.707	-0.572	-0.171	8.0
0.9	0.228	-0.419	0.396	0.009	-0.661	0.023	-0.350	0.649	-0.584	-0.067	0.9
1.0	0.188	-0.379	0.394	-0.052	-0.564	-0.009	-0.288	0.590	-0.586	0.026	1.0
1.2	0.120	-0.302	0.373	-0.146	-0.384	-0.055	-0.181	0.474	-0.565	0.176	1.2
1.4	0.067	-0.231	0.337	-0.207	-0.227	-0.082	-0.097	0.365	-0.519	0.280	1.4
1.6	0.027	-0.169	0.291	-0.239	-0.097	-0.095	-0.034	0.267	-0.456	0.342	1.6
1.8	-0.001	-0.115	0.242	-0.248	0.004	-0.097	0.011	0.183	-0.385	0.369	1.8
2.0	-0.020	-0.072	0.193	-0.240	0.078	-0.092	0.040	0.114	-0.311	0.366	2.0
2.5	-0.036	-0.003	0.087	-0.175	0.161	-0.063	0.065	0.001	-0.146	0.282	2.5
3.0	-0.029	0.022	0.020	-0.095	0.147	-0.032	0.053	-0.041	-0.035	0.160	3.0
3.5	-0.017	0.024	-0.011	-0.034	0.095	-0.011	0.031	-0.043	0.018	0.060	3.5
4.0	-0.007	0.016	-0.018	0.000	0.043	0.000	0.013	-0.029	0.032	0.001	4.0
4.5	-0.001	0.008	-0.014	0.012	0.009	0.003	0.002	-0.014	0.026	-0.021	4.5
5.0	0.001	0.002	-0.008	0.012	-0.007	0.003	-0.002	-0.004	0.014	-0.022	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

Figure 6.1.2.6.5-6 Linear Elastic Pile Solution,  $E_s = E_{so} + f z$  where  $E_{so}/(f T) = 1.0$ 

	_	_						_	_		
z/T	$A_{y}$	$A_s$	A <sub>m</sub>	$A_{v}$	$A_p$	B <sub>y</sub>	B <sub>s</sub>	$B_{m}$	$B_v$	B <sub>p</sub>	z/T
0.0	0.404	-0435	0.000	1.000	-2.019	0.435	-0.925	1.000	0.000	-2.177	0.0
0.1	0.360	-0.431	0.090	0.807	-1.837	0.348	-0.825	0.989	-0.198	-1.775	0.1
0.2	0.318	-0.418	0.161	0.633	-1.651	0.270	-0.728	0.960	-0.357	-1.406	0.2
0.3	0.277	-0.399	0.216	0.477	-1.465	0.202	-0.634	0.918	-0.481	-1.073	0.3
0.4	0.238	-0.376	0.257	0.340	-1.283	0.144	-0.545	0.864	-0.573	-0.775	0.4
0.5	0.201	-0.349	0.284	0.220	-1.107	0.093	-0.461	0.803	-0.637	-0.514	0.5
0.6	0.168	-0.319	0.301	0.118	-0.940	0.051	-0.384	0.737	-0.677	-0.287	0.6
0.7	0.137	-0.289	0.308	0.031	-0.783	0.017	-0.314	0.668	-0.697	-0.094	0.7
8.0	0.110	-0.258	0.307	-0.040	-0.638	-0.012	-0.251	0.598	-0.698	0.067	8.0
0.9	0.086	-0.228	0.300	-0.097	-0.506	-0.034	-0.195	0.528	-0.685	0.198	0.9
1.0	0.064	-0.199	0.288	-0.142	-0.387	-0.050	-0.145	0.461	-0.660	0.303	1.0
1.2	0.030	-0.144	0.253	-0.198	-0.188	-0.071	-0.066	0.336	-0.584	0.440	1.2
1.4	0.006	-0.098	0.210	-0.221	-0.041	-0.078	-0.010	0.228	-0.490	0.499	1.4
1.6	-0.009	-0.060	0.166	-0.218	0.061	-0.076	0.027	0.140	-0.389	0.500	1.6
1.8	-0.018	-0.032	0.124	-0.199	0.124	-0.068	0.048	0.072	-0.293	0.462	1.8
2.0	-0.022	-0.011	0.086	-0.171	0.156	-0.057	0.057	0.022	-0.206	0.401	2.0
2.5	-0.020	0.015	0.021	-0.091	0.149	-0.029	0.050	-0.038	-0.051	0.218	2.5
3.0	-0.011	0.017	-0.008	-0.030	0.091	-0.009	0.029	-0.043	0.019	0.074	3.0
3.5	-0.004	0.011	-0.014	0.001	0.037	0.000	0.011	-0.028	0.034	-0.002	3.5
4.0	-0.001	0.005	-0.010	0.010	0.005	0.003	0.001	-0.012	0.026	-0.026	4.0
4.5	0.001	0.001	-0.005	0.009	-0.007	0.002	-0.002	-0.002	0.013	-0.023	4.5
5.0	0.001	-0.001	-0.001	0.005	-0.008	0.001	-0.002	0.001	0.004	-0.013	5.0
10.0	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	10.0

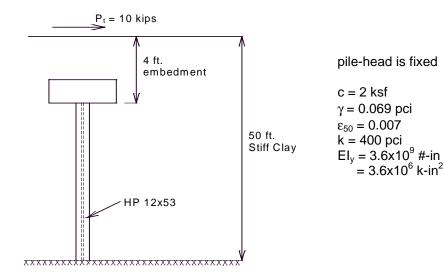
Table 6.1.2.6.5-7 Linear Elastic Pile Solution,  $E_s = E_{s0} + f z$  where  $E_{so}/(f T) = 5.0$ 

Note: For the following example,  $\lambda$  = T from Figures 6.1.2.6.5-10 & 11 and Tables 6.1.2.6.5-1 through 7.

### Example 2:

Find: a) the lateral stiffness of the embedded pile-head, S<sub>33</sub> shown below.

b) the moment distribution and lateral deflection along the pile using the linear subgrade modulus method.



#### Solve:

- a) Using Figure 6.1.2.6.5-6 with c = 2 ksf, f = 32 pci Using Figure 6.1.2.6.5-7 with El<sub>y</sub> = 3.6x10<sup>9</sup> #-in<sup>2</sup> and f = 32pci,  $S_{33}\approx 1.05x10^5$  #/in = 105 k/in
- b) From eq (1), the characteristic length  $\lambda = \sqrt[5]{\frac{EI_y}{f}} = \sqrt[5]{\frac{3.6x10^9 \# in^2}{32\,pci}}$  = 40.76 in

$$E_{so} = f x 4ft = (32pci) (4x12) = 1536 psi$$

$$\frac{\mathsf{E}_{\mathsf{so}}}{f*\lambda} = \frac{1536}{32*40.76} = 1.178 \text{ use Table 6.1.2.6.5-5 } (\frac{\mathsf{E}_{\mathsf{so}}}{f*\lambda} \approx 1.0)$$

from Figure 6.1.2.6.5-11:

Slope, 
$$S = \left(\frac{P_t \lambda^2}{EI}\right) A_s + \left(\frac{M_t \lambda}{EI}\right) B_s$$
 (a)

Deflection, 
$$y = \left(\frac{P_t \lambda^3}{EI}\right) A_y + \left(\frac{M_t \lambda^2}{EI}\right) B_y$$
 (b)

Moment, 
$$M = (P_t \lambda)A_m + M_t B_m$$
 (c)

For a fixed-head pile: S=0

Substituting S=0 into eq (a)

$$S = 0 = \left(\frac{P_t \lambda^2}{EI}\right) A_s + \left(\frac{M_t \lambda}{EI}\right) B_s, \text{ Where } A_s \text{ and } B_s \text{ are coefficients at the pile-}$$

head

$$= \lambda A_s + \frac{M_t}{P_t} B_s$$

$$\therefore \frac{M_t}{P_t} = -\lambda \frac{A_s}{B_s} \quad \text{(d)} \quad \text{Where } \lambda = 40.76 \text{in}.$$

From Table 6.1.2.6.5-5: 
$$A_s = -0.879$$
 and  $B_s = -1.290$   $\therefore \frac{A_s}{B_s} = 0.681$ 

Substituting eq (d) into eq (c)

Moment 
$$M = (P_t \lambda) A_m + M_t B_m$$
  

$$= P_t \lambda \left( A_m + \frac{M_t}{P_t \lambda} * B_m \right)$$

$$= P_t \lambda \left( A_m - \frac{A_s}{B_s} * B_m \right)$$

$$= (10 \text{kips} * 40.76 \text{in}) (A_m - 0.681 B_m)$$

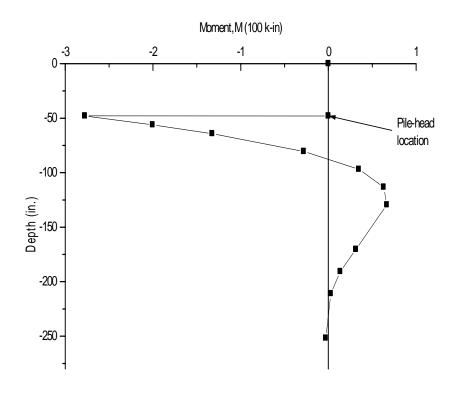
$$= 407.6 (A_m - 0.681 B_m) \text{ kip-in}$$
 (e)

Using Table 6.1.2.6.5-5, the following table is created.

Seismic Analysis Model

<u>Z</u>	Depth (z)	Coefficients		Moment	
λ	ln	$A_{m}$	$B_m$	From eq (e)	
0.0	0.00	0.000	1.000	-277.58	k-in
0.2	8.15	0.178	0.983	-200.30	k-in
0.4	16.30	0.312	0.935	-132.36	k-in
0.8	32.60	0.457	0.772	-28.02	k-in
1.2	48.91	0.470	0.565	34.74	k-in
1.6	65.22	0.400	0.360	63.11	k-in
2.0	81.52	0.293	0.190	66.69	k-in
3.0	122.3	0.060	-0.025	31.40	k-in
3.5	142.7	0.003	-0.045	13.71	k-in
4.0	163.0	-0.019	-0.038	2.80	k-in
5.0	203.8	-0.014	-0.010	-2.93	k-in

The moment distribution of the pile is shown below:



Substituting eq (d) into eq (b)

$$y = \left(\frac{P_t \lambda^3}{EI}\right) A_y + \left(\frac{M_t \lambda^2}{EI}\right) B_y$$

$$= \frac{P_t \lambda^3}{EI} \left(A_y + \frac{M_t}{P_t \lambda} B_y\right)$$

$$= \frac{P_t \lambda^3}{EI} \left(A_y - \frac{A_s}{B_s} B_y\right)$$

$$= \frac{10 * (40.76)^3}{3.6 \times 10^6} \left(A_y - 0.681 B_y\right)$$

$$= 0.188 (A_y - 0.681 B_y) \qquad (f)$$

Using Table 6.1.2.6.5-5, the following table is created.

<u>Z</u>	Depth (z)	Coefficients		Deflection	
λ	In	$A_{y}$	$B_y$	From eq (f)	
0.0	0.00	1.097	0.879	0.0937	in
0.2	8.15	0.923	0.641	0.0915	in
0.4	16.30	0.755	0.442	0.0854	in
0.8	32.60	0.460	0.153	0.0669	in
1.2	48.91	0.236	-0.012	0.0459	in
1.6	65.22	0.087	-0.087	0.0275	in
2.0	81.52	0.001	-0.104	0.0135	in
3.0	122.3	-0.044	-0.051	-0.0017	in
3.5	142.7	-0.031	-0.023	-0.0029	in
4.0	163.0	-0.016	-0.006	-0.0022	in
5.0	203.8	0.000	0.004	-0.0005	in

Check the pile stiffness:  $S_{33} = 10 \text{kips}/0.0937 \text{in} = 107 \text{ k/in}$  which is very close to the value calculated in a) using Figure 6.1.2.6.5-7.

# Seismic Design - Section 6.1

Page 2.6.6-1

Seismic Analysis Model

## 2.6.6 - Drilled Shaft Lateral and Rotational Stiffnesses

The diameter of the drilled shaft is usually much bigger than the typical piles used by MoDOT and the aspect ratio (length to diameter) is usually smaller for drilled shafts. Due to a smaller aspect ratio, the magnitude of rotation of the shaft can be more significant than for a pile. Therefore, the rotational resistance along the length and at the tip of the shaft, which is neglected for a typical pile, could be very significant. For simplicity, the procedure of using p-y curves for piles is recommended for drilled shafts. However, a scaling factor (larger than unity) shall be applied to either the linear subgrade modulus,  $E_{\rm s}$ , or the resistance value (p) of the p-y curves for shaft diameters greater than 24 inches. The scaling factor is the ratio of the shaft diameter to a 24 inch diameter shaft (Lam 1998).

#### 2.6.7 - Spread Footing Stiffness, Equivalent Circular Footing Method

Volume II of report #FHWA/RD-86/102, sections 5.0-5.8

For spread footings and caps of pile footings, the general form of stiffness matrix is summarized in Figure 6.1.2.6.7-1 (Lam and Martin, 1986).

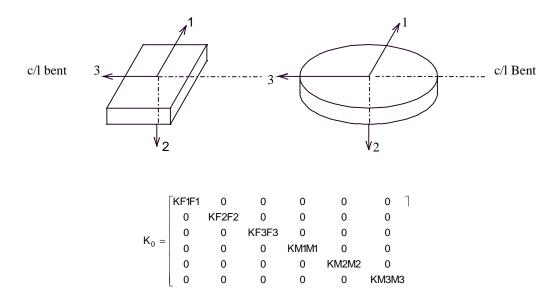


Figure 6.1.2.6.7-1 Spread Footing Foundation Matrix, [K<sub>0</sub>]

For spread footings, this is the master joint stiffness matrix located at the center of gravity of the footing. For pile footings, this stiffness matrix should be combined with the pile stiffness matrices using rigid body transformation. In general, the off-diagonal (cross-coupling) terms can be neglected, for two reasons: 1) the values of the off-diagonal terms are small, especially for shallow footings, and 2) they are difficult to compute. However, for some unusual deeply-embedded footings where the ratio of embedment depth to equivalent diameter is greater than five, the contribution of stiffness from the cross-coupling terms may need to be included (see Development Section).

#### Stiffness Matrix

The stifness matric[K], of an embedded footing can be express as:

 $[K]=\alpha*\beta*[K_0]$  where

 $[K_0]$  = the stiffness matrix of an equivalent circular surface footing from Figure 6.1.2.6.7-1.

 $\alpha$  = the foundation shape correction factor using L/B from Figure 6.1.2.6.7-4 and:

2L = the longer of the footing length or width in feet.

2B = the shorter of the footing length or width in feet.

 $\beta$  = the foundation embedment factor using D/R from Figure 6.1.2.6.7-5 and:

D = footing thickness in feet

R = equivalent footing radius as defined in Figure 6.1.2.6.7-2 in feet. Note that R is different for different modes of displacement.

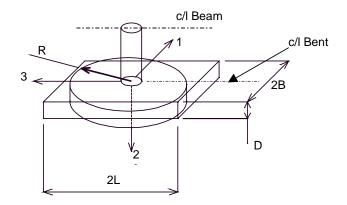


Figure 6.1.2.6.7-2 Equivalent Radius of Rectangular Footings

# **Equivalent Radius**

Translational: 
$$R = \sqrt{\frac{4BL}{\pi}} \text{ (Translation about any axis)}$$
 Rotational: 
$$R_1 = \left[\frac{(2B)(2L)^3}{3\pi}\right]^{1/4} \text{ (Rocking about the 1-axis)}$$
 
$$R_3 = \left[\frac{(2B)^3(2L)}{3\pi}\right]^{1/4} \text{ (Rocking about the 3-axis)}$$
 Torsional: 
$$R_2 = \left[\frac{4BL(4B^2 + 4L^2)}{6\pi}\right]^{1/4} \text{ (Torsion about the 2-axis)}$$

# Stiffness Coefficients

Horizontal translation (KF1F1) = 
$$\frac{8GR}{2-\nu}$$
  
Vertical translation (KF2F2) =  $\frac{4GR}{1-\nu}$   
Horizontal translation (KF3F3) =  $\frac{8GR}{2-\nu}$   
Rocking rotation (KM1M1) =  $\frac{8GR^3}{3(1-\nu)}$ 

New: April 2000

Torsional rotation (KM2M2) = 
$$\frac{16GR_2^3}{3}$$

Rocking rotation (KM1M1) = 
$$\frac{8GR_3^3}{3(1-\nu)}$$

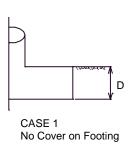
Where:

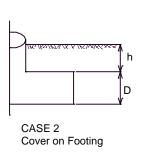
G = Shear modulus for the soil directly beneath the footing, ksf

= 
$$\frac{\mathsf{E}}{2(1+v)}$$
, where E and v are from Section 6.1.2.4

v = Poisson's Ratio for the soil directly beneath the footing

Three idealized embedment conditions are represented in Figure 6.1.2.6.7-3. To consider all of the cases of embedment effects,  $\beta$  would normally be a function of R, D and h. However, report # FHWA/RD-86/102 (Volume II) shows that the effects of ground cover and excavations can be ignored, and the situation depicted in Case 1 can be used to approximate the conditions in Case 2 and 3. Therefore,  $\beta$  can be determined based solely on D/R from Figure 6.1.2.6.7-5 for all three of the above cases.





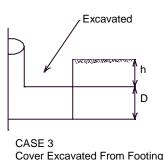


Figure 6.1.2.6.7-3 Embedment Cases

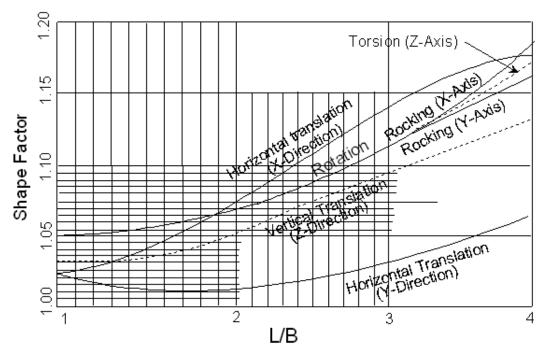


Figure 6.1.2.6.7-4 Shape Factor,  $\alpha$  (Lam and Martin 1986)

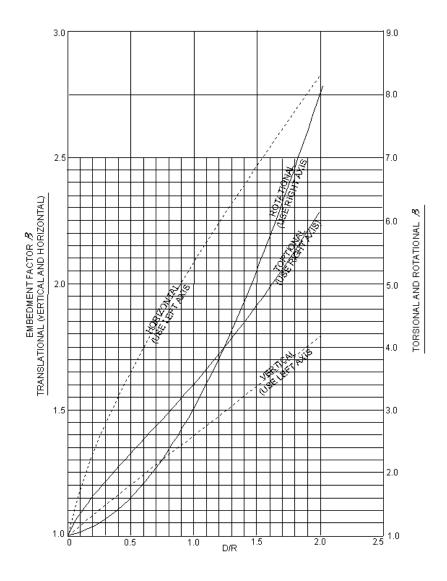


Figure 6.1.2.6.7-5 Embedment Factor,  $\beta$ 

# 2.7 - Rigid Body Transformation

An abutment consists of many translational and rotational springs which represent the interaction between soil and backwall, beam, wings, pile caps and piles as shown in Figure 6.1.2.7-1. To reduce the total number of degrees-of-freedom in the analysis and to take into account the geometric relationships among the spring constants, it is attractive to lump all the stiffnesses of these springs from "slave" joints to a "master" joint through a rigid body transformation. Any two joints on the rigid body (e.g. abutment) are constrained such that the deformation of one joint (the slave joint) can be represented by the deformation of the other joint (the master joint). Thus the degrees-of-freedom for the slave joint are transferred to the master joint, and the number of degrees-of-freedom in an abutment is reduced. Figure 6.1.2.7-2 depicts the typical joints "j" and "m" for slave and master joints, respectively. For integral abutments, usually the center of gravity of the superstructure is chosen as the "master" joint as shown in Figure 6.1.2.7-1. RBT can also be applied to the pile footing by transforming all the pile springs and pile cap springs to an assigned master joint. Usually the master joint is placed at the center of gravity of the pile cap. The RBT takes into account the coupling effects between translational and rotational responses of skewed abutments.

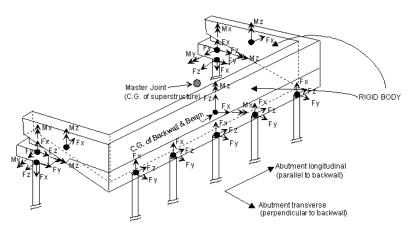


Figure 6.1.2.7-1 Abutment Spring Constants Considered

#### 1) RBT for Stiffness

Before a seismic structural analysis computer program is run, RBT is used to sum up the stiffness effects of many individual springs (at different "slave joint" locations and in different local element directions) into one equivalent 6 X 6 stiffness matrix (at the "master joint" and in its joint coordinate system).

#### 2) RBT for Force

After the seismic structural analysis program has been run, RBT uses the master joint's forces to back-solve for individual forces and displacements at the slave joints. Usually, the master joint's displacements are not used

because the displacements are very small and are more difficult to back-calculate.

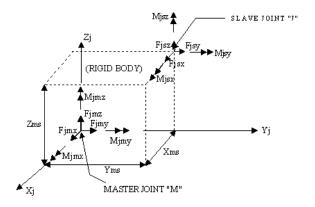


Figure 6.1.2.7-2 Master Joint and Slave Joint Relationship

#### Iteration of RBT for Stiffness and Force

# A) Abutments

Sometimes during Iterative Abutment Analysis (see Section 6.1.2.10), it becomes necessary to reduce spring constants at slave joints. If individual stiffnesses are reduced, then (1) and (2) above must be repeated to recompute the master joint stiffness matrix and to recompute the local slave element forces for each new iteration.

#### B) Pile Footings

If pile footing design significantly changes the assumed size and pile geometry of a pile footing, then (1) and (2) above must be repeated to recompute the master joint stiffness matrix and to recompute the local slave element forces for each new iteration. The distribution of seismic forces to bents is by stiffness, relative to each other, so a change in stiffness at one bent affects the force distribution to all bents, particularly the distribution between intermediate bents.

In order to perform rigid body transformation, several procedures are needed and defined in the following sections.

#### 2.7.1 - Joint Definition and Degrees of Freedom

A joint is defined as the point where one or more springs are connected. The assemblage of all springs becomes a structural model. The structural model is built by first defining the location and orientation of each joint.

- 1.) Global Coordinate System. The global coordinate system (GCS) defines the location of a structure. The GCS is a cartesian coordinate system, with three perpendicular axes  $x_g$ ,  $y_g$ , and  $z_g$ . The  $z_g$  axis is defined as  $x_g$  cross  $y_g$  (right hand rule), as shown in Figure 6.1.2.7.1-1. The location of the GCS's origin is arbitrary, and usually taken at the base of the structure.
- 2.) <u>Joint Coordinate System.</u> The location of a joint is defined by its  $x_g$ ,  $y_g$ ,  $z_g$  coordinates in the GCS. Each joint is assumed to have six degrees of freedom (dof). The first three dof are translational, and correspond to the joint's  $x_j$ ,  $y_j$ , and  $z_j$  axes. The remaining three dof are rotational, about the joint's  $x_i$ ,  $y_j$ , and  $z_j$  axes as shown in Figure 6.1.2.7-1-1. The  $x_j$ ,  $y_j$ , and  $z_j$  axis define a joint coordinate system (JCS) for a given joint. The JCS may not be parallel to the GCS, and the JCS may vary for different joints. Thus, the orientation of the JCS for a given joint is defined by two vectors  $\overrightarrow{V}_{xj}$  and  $\overrightarrow{V}_{yj}$ . The origin of the JCS is at the joint. A third vector is then  $\overrightarrow{V}_{zj} = \overrightarrow{V}_{xj} \times \overrightarrow{V}_{yj}$ . The three vectors are written in matrix form as:

$$\{V_{j}\} = \begin{bmatrix} \overrightarrow{V_{xj}} \\ \overrightarrow{V_{yj}} \\ \overrightarrow{V_{zj}} \end{bmatrix} = \begin{bmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{bmatrix} \begin{bmatrix} \overrightarrow{i} \\ \overrightarrow{j} \\ \overrightarrow{k} \end{bmatrix} = \begin{bmatrix} c_{j} \end{bmatrix} \begin{bmatrix} \overrightarrow{i} \\ \overrightarrow{j} \\ \overrightarrow{k} \end{bmatrix}$$
(1)
$$\uparrow \qquad \qquad \uparrow \qquad \qquad \uparrow$$

$$JCS \qquad \qquad GCS$$

where  $\vec{i}$ ,  $\vec{j}$ , and  $\vec{k}$  are unit vectors parallel to the  $x_g$ ,  $y_g$ , and  $z_g$  axes. Note that the orientation of the JCS determines the orientation of the global degrees of freedom.

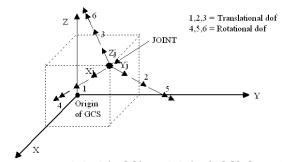


Figure 6.1.2.7.1-1 Global (GCS) and Joint(JCS) Coordinate System

## 2.7.2 - Rigid Body Constraints

As shown if Figure 6.1.2.7-2, summing the forces acting on the slave joint "j" about the master joint "m" in three dimensions, yields the force transformation matrix for a 3D rigid body as follows:

$$\begin{bmatrix} F_{jmx} \\ F_{jmy} \\ F_{jmz} \\ M_{jmx} \\ M_{jmy} \\ M_{jmz} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & -Z_{ms} & Y_{ms} & 1 & 0 & 0 \\ Z_{ms} & 0 & -X_{ms} & 0 & 1 & 0 \\ -Y_{ms} & X_{ms} & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} F_{jsx} \\ F_{jsy} \\ F_{jsz} \\ M_{jsx} \\ M_{jsy} \\ M_{jsz} \end{bmatrix}$$
 (2)

where  $\{F_m\}_j$  represents the force vector acting on the master joint "m", and  $\{F_s\}_j$  represents the force vector acting on the slave joint "j" . A similar transformation for displacements can be derived as

$$\{\delta_{s}\}_{j} = \left[\mathsf{T}_{ms}\right]_{j}^{\mathsf{T}} \{\delta_{m}\}_{j} \tag{4}$$

where  $\{\delta_m\}_j$  represents the displacement vector of the master joint, and  $\{\delta_s\}_j$  represents the displacement vector of the slave joint.

## 2.7.3 - Spring Element Coordinate System (ECS)

Each structural component of an abutment or pile footing such as piles, pile caps, backwalls or wings contain several spring constants in the element coordinate directions. The direction of the individual ECS is defined by the designer. Figure 6.1.2.7.3-1 shows some typical ECS for piles, pile caps, backwalls and wings.

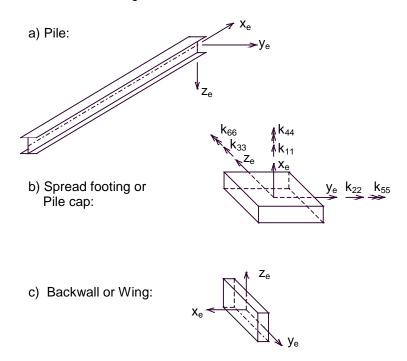


Figure 6.1.2.7.3-1 Spring Element Coordinate System

For example, in Figure 6.1.2.7.3-1 (b), there are three translational springs  $K_{11}$ ,  $K_{22}$ ,  $K_{33}$  in the ECS'  $x_e$ ,  $y_e$ , and  $z_e$  directions, respectively, and 3 rotational springs  $K_{44}$ ,  $K_{55}$ , and  $K_{66}$  in the ECS'  $x_e$ ,  $y_e$ ,  $z_e$  directions, respectively.

## 2.7.4 - Transferring Element Force Matrices

# Transferring Spring Element Force Matrix From ECS to GCS.

Let the element coordinate system be denoted  $x_e$ ,  $y_e$ ,  $z_e$  at a joint. The three vectors that define the orientation of the ECS can be written in matrix form as:

$$\begin{cases}
\overrightarrow{V}_{e} \\
\overrightarrow{V}_{e}
\end{cases} = \begin{bmatrix}
\overrightarrow{V}_{xe} \\
\overrightarrow{V}_{ye} \\
\overrightarrow{V}_{ze}
\end{bmatrix} = \begin{bmatrix}
c_{11} & c_{12} & c_{13} \\
c_{21} & c_{22} & c_{23} \\
c_{31} & c_{32} & c_{33}
\end{bmatrix} \begin{bmatrix}
\overrightarrow{i} \\
\overrightarrow{j} \\
\overrightarrow{k}
\end{bmatrix} = \begin{bmatrix}
c_{e}
\end{bmatrix} \begin{bmatrix}
\overrightarrow{i} \\
\overrightarrow{j} \\
\overrightarrow{k}
\end{bmatrix}$$
(5)

ECS

GCS

where [ce] is the direction cosine matrix for the element's ECS.

$$\left\{ \begin{matrix} F_{G} \end{matrix} \right\}_{i} = \left[ \begin{matrix} C_{e} \end{matrix} \right]_{i}^{T} \left\{ \begin{matrix} F_{e} \end{matrix} \right\}_{i}$$

$$ECS$$
(6)

where  $\{F_G\}_i$  = element forces at joint i in the GCS direction  $\{F_e\}_i$  = element forces at joint i in the ECS direction

# Transferring Element Force Matrix From GCS to JCS.

 $\begin{aligned} \{F_s\}_i &= [C_j]_i \{F_g\}_i & \text{where } \{F_s\}_i \text{ element forces at joint i in the JCS direction} \\ &= [C_j]_i \Big( [C_e]_i^T \{F_e\}_i \Big) \\ &= [C_{je}]_i \{F_e\}_i \end{aligned} \tag{7}$ 

So: 
$$\{\delta_e\}_i = [c_{je}]_i^T \{\delta_s\}_i$$
 (8)

# 2.7.5 – Transferring the Element Stiffness Matrix at Slave Joint "i" in its ECS to Master Joint in the JCS Direction

From eqns. (3), (4), (7) and (8):

$$\begin{aligned} \{F_{m}\}_{i} &= [T_{ms}]_{i} \{F_{s}\}_{i} \\ &= [T_{ms}]_{i} [c_{je}]_{i} \{F_{e}\}_{i} \\ &= [T_{ms}]_{i} [c_{je}]_{i} ([k_{e}]_{i} \{\delta_{e}\}_{i}) \\ &= [T_{ms}]_{i} [c_{je}]_{i} [k_{e}]_{i} [c_{je}]_{i}^{T} \{\delta_{s}\}_{i} \\ &= [T_{ms}]_{i} [c_{je}]_{i} [k_{e}]_{i} [c_{je}]_{i}^{T} [T_{ms}]_{i}^{T} \{\delta_{m}\}_{i} \\ &= ([A]_{i} [k_{e}]_{i} [A]_{i}^{T}) \{\delta_{m}\}_{i} = [k_{m}]_{i} \{\delta_{m}\}_{i} \end{aligned}$$
(9)

Stacking up all the stiffness from slave joints to the master joint gives:

$$\{F_{m}\} = \prod_{i=1}^{n} \{F_{m}\}_{i} = [K_{m}]\{\delta_{m}\}$$
 (10)

and

$$[k_m] = \prod_{i=1}^n [k_m]_i$$

where n =the total number of slave joints.

From the seismic analysis, the force vector,  $\{F_m\}$ , or the displacement vector,  $\{\delta_m\}$ , at the master joint can be obtained. Then the spring deformations and spring forces for each element can be obtained by:

$$\{\delta_{e}\}_{i} = [A]_{i}^{\mathsf{T}} \{\delta_{m}\} \tag{11}$$

$$\{F_{e}\}_{i} = [k_{e}]_{i} \{\delta_{e}\}_{i}$$
 (12)

#### Example:

Transfer the pile-head stiffness matrix of pile no.2 as shown in Figure 6.1.2.7.5-1 to the master joint at joint 17. In the figure, the pile footing consists of 16 piles and a rigid pile cap. The GCS (x, y, z) and ECS (xe, ye, ze) of the individual piles are also shown in the figure. Let all the joints JCS be in the same direction as the GCS and assume all the slave joints (at pile-head locations) have the same elevations as that of the master joint. The individual pile-head matrix corresponding to the pile ECS is:

It is assumed that the rotation and lateral movements at the pile-heads are small. Therefore, the rotational stiffnesses at the pile-head are neglected in this example.

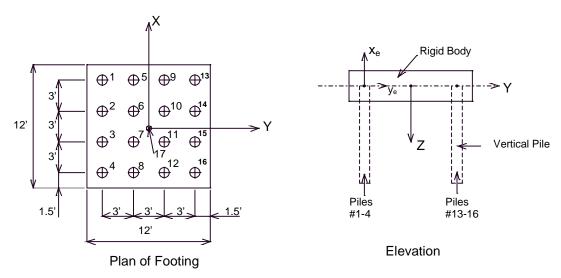


Figure 6.1.2.7.5-1 Pile Footing

Solve:

For Pile #2:

From eq. (1):  $[C_j]_{6x6}$  = unity matrix

From eq. (2): 
$$Z_{ms} = 0$$
";  $Y_{ms} = -4.5$ ' = -54";  $X_{ms} = 18$ "

$$[T_{ms}] = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & -Z_{ms} & Y_{ms} & 1 & 0 & 0 \\ Z_{ms} & 0 & -X_{ms} & 0 & 1 & 0 \\ -Y_{ms} & X_{ms} & 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -54 & 1 & 0 & 0 \\ 0 & 0 & -18 & 0 & 1 & 0 \\ 54 & 18 & 0 & 0 & 0 & 1 \end{bmatrix}$$

From eq. (5):

$$[c_e] = \begin{bmatrix} \overrightarrow{V}_{xe} \\ \overrightarrow{V}_{ye} \\ \overrightarrow{V}_{ze} \end{bmatrix} = \begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \therefore [c_e]_{6x6} \begin{bmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

From eq. (7):

From eq. (9)

$$[A] = [T_{ms}][c_{je}] = \begin{bmatrix} 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ -1 & 0 & 0 & 0 & 0 & 0 \\ 54 & 0 & 0 & 0 & 0 & 1 \\ 18 & 0 & 0 & 0 & 1 & 0 \\ 0 & 18 & 54 & -1 & 0 & 0 \end{bmatrix}_{6x6}$$

... The stiffness matrix at the Master Joint due to pile no. 2,  $[K_m]$ , is

$$[K_{m}] = [A][K_{e}][A]^{T} = \begin{bmatrix} 5.5 & 0 & 0 & 0 & 0 & 297 \ 0 & 5.5 & 0 & 0 & 0 & 99 \ 0 & 0 & 76 & -4104 & -1368 & 0 \ 0 & 0 & -4104 & 221616 & 73872 & 0 \ 0 & 0 & -1368 & 73872 & 24624 & 0 \ 297 & 99 & 0 & 0 & 0 & 17820 \end{bmatrix} \times 10^{4}$$

# 2.8 - Modeling of Intermediate Pile Cap and Drilled Shaft Bents

#### 2.8.1 - Coupled Foundation Stiffness Method- a Rigorous Method

A rigorous procedure to develop a linear 6x6 pile stiffness matrix at groundline has been described in Example 6.1.2.6.4-1 in Section 6.1.2.6.4. Figure 6.1.2.8.1-1 illustrates the structural model used by this approach.

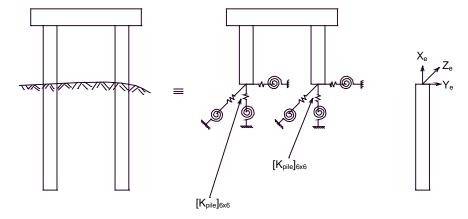


Figure 6.1.2.8.1-1 Structural Model for Pile Cap and Drilled Shaft Intermediate Bents

The common form of the stiffness matrix in the local pile coordinate system  $(x_e, y_e, z_e)$  is given in eq. (1) in which the diagonal terms  $K_x$ ,  $K_y$ ,  $K_z$ ,  $K_{\theta x}$ ,  $K_{\theta y}$ ,  $K_{\theta z}$  are stiffnesses corresponding to translational and rotational degrees of freedom associated with  $x_e$ ,  $y_e$ , and  $z_e$  axes, respectively. The off-diagonal terms represent coupling between two degrees of freedom. These stiffness coefficients can be calculated from the solutions presented in Section 6.1.2.6.

$$[K_{\text{pile}}]_{6x6} = \begin{bmatrix} K_x & 0 & 0 & 0 & 0 & 0 \\ & K_y & 0 & 0 & 0 & -K_{y\theta z} \\ & & K_z & 0 & K_{z\theta y} & 0 \\ & & & K_{\theta x} & 0 & 0 \\ & & & & K_{\theta y} & 0 \\ & & & & & K_{\theta z} \end{bmatrix}$$
 (1)

#### 2.8.2 - Equivalent Cantilever Column Method- a Simplied Approach

In the equivalent cantilever method, the foundation is replaced by a cantilever column that has stiffness approximately equivalent to those of the pile and surrounding soil. This is represented in Figure 6.1.2.8.2-1. This

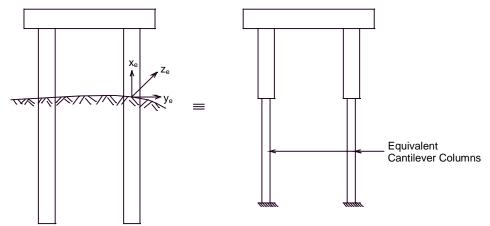


Figure 6.1.2.8.2-1 Structural Model for Pile Cap and Drilled Shaft Intermediate Bents

simplified approach may be used if a seismic analysis computer program is not capable of providing user input of a 6x6 stiffness matrix to represent the foundation stiffness at ground level. The stiffness matrix of a equivalent cantilever column can be expressed as

$$[K]_{equiv} = \begin{bmatrix} \frac{AE}{L} & 0 & 0 & 0 & 0 & 0 \\ & \frac{12EI_z}{L^3} & 0 & 0 & 0 & -\frac{6EI_z}{L^2} \\ & & \frac{12EI_y}{L^3} & 0 & \frac{6EI_y}{L^2} & 0 \\ & & \frac{GJ}{L} & 0 & 0 \\ symm. & & \frac{4EI_y}{L} & 0 \\ & & & \frac{4EI_z}{L} \end{bmatrix}$$
 (2)

where L is the equivalent cantilever length.

AE is the equivalent cantilever's axial rigidity.

 $\mathsf{El}_\mathsf{y}$  is the equivalent cantilever's flexural rigidity about the  $\mathsf{y}_\mathsf{e}$  direction.

 $\mathsf{EI}_\mathsf{z}$  is the equivalent cantilever's flexural rigidity about the  $\mathsf{z}_\mathsf{e}$  direction.

G is the equivalent cantilever's shear modulus.

J is the equivalent cantilever's torsional moment of inertia about the axial  $x_{\rm e}$  direction.

For translational and rotational stiffnesses, it is obvious that only three cantilever model parameters (i.e.  $El_y$ ,  $El_z$ , and L) are not sufficient to satisfy all six stiffness coefficients ( four diagonal stiffnesses,  $K_y$ ,  $K_z$ ,  $K_{\theta y}$ ,  $K_{\theta z}$ , and two cross-coupling stiffness,  $K_{y\theta z}$ ,  $K_{z\theta y}$ ) in equation (1) of section 6.1.2.8.1.

However, the general approach is to match the diagonal stiffness terms  $K_y$ ,  $K_z$ , and  $K_{\theta z}$ . From eqs. (1) and (2):

$$K_{y} = \frac{12EI_{z}}{L^{3}}$$
 (3)

$$K_z = \frac{12EI_y}{L^3} \tag{4}$$

$$K_{\theta z} = \frac{4EI_{z}}{I} \tag{5}$$

From eqs. (3), (4) and (5), solve for El<sub>v</sub>, El<sub>z</sub> and L

$$\mathsf{EI}_{\mathsf{z}} = \frac{\mathsf{K}_{\mathsf{\theta}\mathsf{z}}}{4} \left( \frac{3\mathsf{K}_{\mathsf{\theta}\mathsf{z}}}{\mathsf{K}_{\mathsf{y}}} \right)^{\frac{1}{2}} \tag{6}$$

$$L = \left(\frac{3K_{\theta z}}{K_{y}}\right)^{\frac{1}{2}} \tag{7}$$

$$\mathsf{EI}_{\mathsf{y}} = \frac{\mathsf{K}_{\mathsf{z}}\mathsf{L}^{\mathsf{3}}}{12} \tag{8}$$

Once the equivalent cantilever length is determined from eq. (7), the equivalent AE and GJ can be estimated by:

$$AE = K_x^*L \tag{9}$$

$$GJ = K_{\theta x}^* L \tag{10}$$

#### Example 6.1.2.8.2-1:

Find the equivalent cantilever column's L,  $\text{EI}_{y}$ ,  $\text{EI}_{z}$ , EA and GJ in example 6.1.2.6.4-1.

Solve: From Example 6.1.2.6.4-1,

$$K_x = S_{11} = 1498.3 \text{ k/in}$$

$$K_v = S_{22} = 159.2 \text{ k/in}$$

$$K_z = S_{33} = 142.9 \text{ k/in}$$

$$K_{\theta x} = S_{44} = 41.44 \text{ k-in/rad.}$$

 $K_{\theta v} = S_{55} = 240000 \text{ k-in/rad.}$ 

 $K_{\theta z} = S_{66} = 538460 \text{ k-in/rad.}$ 

 $K_{y\theta z} = S_{26} = -8313 \text{ kip/rad.}$ 

 $K_{z\theta y} = S_{35} = 5200 \text{ kip/rad.}$ 

From eq. (7): L = 
$$\left(\frac{3K_{\theta z}}{K_{y}}\right)^{\frac{1}{2}} = \left(\frac{3 \times 538469}{159.2}\right)^{\frac{1}{2}} = 100.7$$
 in

From eq. (6): 
$$\text{EI}_z = \frac{\text{K}_{\theta z}}{4} \left( \frac{3\text{K}_{\theta z}}{\text{K}_y} \right)^{\frac{1}{2}} = \frac{538460}{4} \times 100.7 = 13559987 \text{k-in}^2$$
 From eq. (8):  $\text{EI}_y = \frac{\text{K}_z \text{L}^3}{12} = \frac{142.9 \times (100.7)^3}{12} = 12160162.9 \text{ k-in}^2$  From eq. (9):  $\text{AE} = \text{K}_x^* \text{L} = 1498.3 \times 100.7 = 150878.8 kips}$  From eq. (10):  $\text{GJ} = \text{K}_{\theta x}^* \text{L} = 41.44 \times 100.7 = 4173.0 kip-in}^2$ 

The stiffness matrix is:

$$[K]_{6\times 6} = \begin{bmatrix} \frac{AE}{L} & 0 & 0 & 0 & 0 & 0 & 0 \\ & \frac{12EI_z}{L^3} & 0 & 0 & 0 & -\frac{6EI_z}{L^2} \\ & & \frac{12EI_y}{L^3} & 0 & \frac{6EI_y}{L^2} & 0 \\ & & \frac{GJ}{L} & 0 & 0 \\ symm & & \frac{4EI_y}{L} & 0 \\ & & & \frac{4EI_z}{Li} \end{bmatrix} = \begin{bmatrix} 1498.3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ & 159.2 & 0 & 0 & 0 & 0 & -8023.3 \\ & & 149.2 & 0 & 7195 & 0 \\ & & & 41.44 & 0 & 0 & 0 \\ symm & & & 483025 & 0 \\ & & & & 538629 \end{bmatrix}$$

# 2.9 - Modeling of Pile (Drilled Shaft) Footings

# 2.9.1 - Coupled Foundation Stiffness Method - Rigorous Approach

A rigorous approach to develop a linear 6x6 pile stiffness matrix at the bottom of the foundation cap has been described in Example 6.1.2.6.4-1 in Section 6.1.2.6.4. Figure 6.1.2.9.1-1 illustrates the structural model used by this approach.

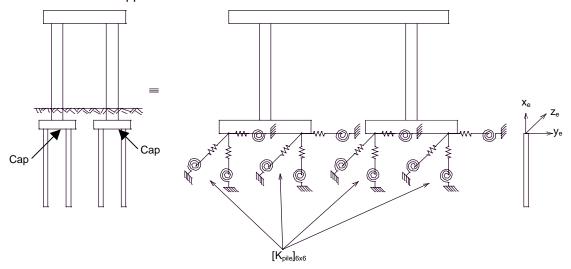


Figure 6.1.2.9.1-1 Structural Model for Pile (and Drilled Shaft) Footing Bents

The common form of the stiffness matrix in the local pile (or shaft) coordinate system  $(x_e, y_e, z_e)$  is given in eq. (1) in Section 6.1.2.8.1.

#### 2.9.2 – Axial and Translational Stiffness Method- Simplified Approach

For a pile footing type configuration shown in Figure 6.1.2.9.1-1, the rotational stiffness of the pile group tends to be dominated by the axial pile stiffness as compared to the stiffness contribution from the bending stiffness of individual piles. Therefore, a simplified fixed pile-head model can be used in the seismic analysis. Figure 6.1.2.9.2-1 illustrates the pile footing model based on this approach. Only pile axial and two horizontal translational stiffnesses are considered in the analysis.

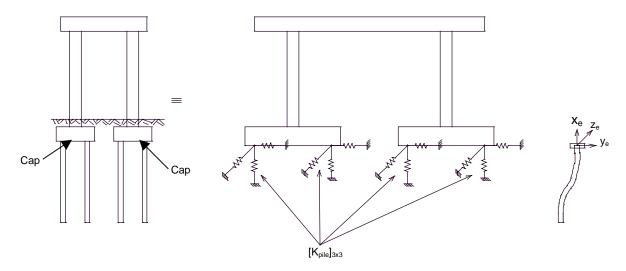


Figure 6.1.2.9.2-1 Structural Model for Pile (and Drilled Shaft) Footing Bents

The stiffness matrix of a pile can be expressed as:

$$[K_{pile}]_{3x3} = \begin{bmatrix} K_x & 0 & 0 \\ 0 & K_y & 0 \\ 0 & 0 & K_z \end{bmatrix}$$

in which the diagonal terms  $K_x$ ,  $K_y$ , and  $K_z$  are stiffnesses corresponding to translational degrees of freedom associated with  $x_e$ ,  $y_e$ , and  $z_e$  axes, respectively. Except for a special case, the simplified approach shall be considered sufficient in the seismic analysis.

# 2.10 - Iterative Abutment Analysis

# Soil Stiffness Nonlinearity

During an earthquake, ground motion causes the bridge abutments to impact against the soil, which deforms the soil. So, soil stiffness varies nonlinearly during seismic motion.

# Linear Approximations of Nonlinear Soil Stiffnesses

By using response spectrum methods, an equivalent linear soil stiffness is required for proper modeling. Spring "constants" are not really constant, but instead they are changeable modeling tools. Equivalent linear springs are used to approximate nonlinear structure/soil interaction, similar to the "secant modulus" approximation for other nonlinear materials.

# Reducing Stiffnesses

The flowchart of Figure 6.1.2.10-1 is slightly altered from the AASHTO flowchart because of limits on reducing pile stiffnesses as described below. Equivalent linear stiffnesses are valid only if they predict achievable soil forces. The passive force applied on the backwall will never exceed the passive force capacity of the soil, because the soil would fail before this could happen. If the seismic analysis program model is outputting an abutment force which exceeds the soil pressure capacity, then the model is predicting something impossible, and the spring constants must be reduced before accepting the model. According to AASHTO Div. I-A 1998 C4.5.2, this force-limiting should apply to all spring locations, including: 1) soil at backwall, 2) soil at wings, 3) piles, etc. Pile stiffness reduction is limited, as described below.

The starting values for springs should be based on the best available soil information as described in Sections 6.1.2.6.4 and 6.1.2.6.5, and it is better to slightly overestimate the stiffness than to underestimate it. Overestimated stiffnesses may be reduced to satisfy the displacement demand through iterative abutment analysis, usually iterative abutment analysis does not increase underestimated stiffnesses in order to save computing time.

# Redesigning the Abutment for Force or Displacement

As indicated in the flowchart (Figure 6.1.2.10-1) and the discussion of this section, the abutment may require redesigning if force or displacement limitations are exceeded. See Sections 6.1.2.10.1, 6.1.2.10.2, or 6.1.2.10.3 for discussion of intermediate wings, squared-off wings, deepened beams, and other remedial actions.

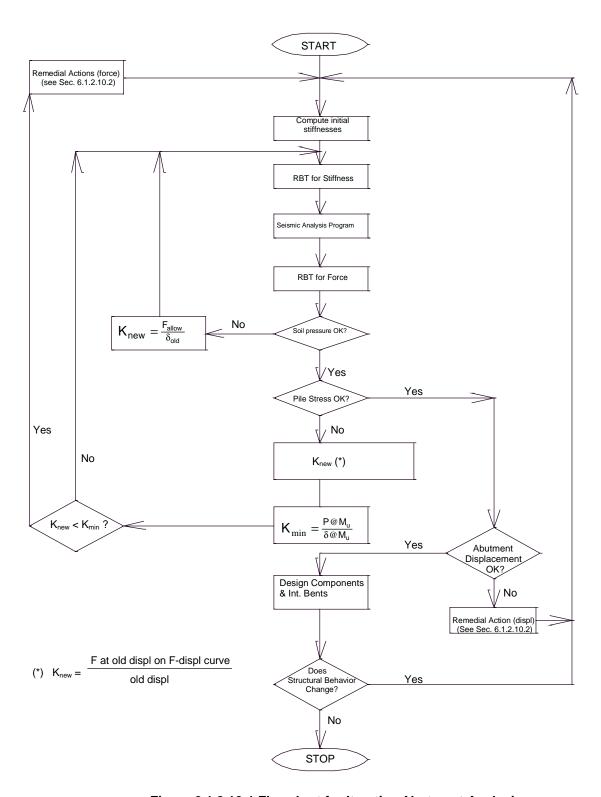


Figure 6.1.2.10-1 Flowchart for Iterative Abutment Analysis

# **General Procedure**

# Iterative Abutment Analysis

Note: Each different bridge model will require its own Iterative Abutment Analysis. For example, a model without liquefaction will require a completely independent analysis from a model with liquefaction.

#### 1) Stiffness:

Compute the initial stiffness estimates as described in Section 6.1.2.6.

## 2) RBT for Stiffness:

Combine the stiffnesses at the master joints using RBT as described in Section 6.1.2.7.

#### 3) Seismic Analysis:

Run the Seismic Structural Analysis Program as described in Section 6.1.2.8.

#### 4) RBT for Forces:

Redistribute the master joint forces using RBT for force as described in Section 6.1.2.7.

#### 5) Soil Pressures:

Compute the soil pressure (see Section 6.1.2.10.1) on the backwall and the pressure on the wings. If the pressure is greater than the allowable pressure, then reduce the corresponding stiffness accordingly and go to Step 2. If the pressures are less than the allowable, then go to Step 6.

#### 6) Pile Stresses:

a) Check shear stress and resultant moment (see Section 6.1.2.10.2). If pile stress or moment is greater than the allowable, for simplicity, reduce the stiffnesses in each direction accordingly, corresponding to the pile-head displacement calculated in that direction. However, in order to keep R=1 for pile foundations, do not reduce the stiffness below the minimum stiffness. The minimum stiffness is defined as the translational stiffness at which the ultimate moment, Mu, for concrete piles or plastic moment, Mp, for steel piles occurred along the pile as shown in Figure 6.1.2-10-2.

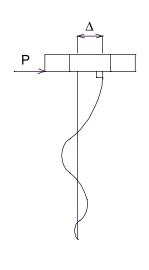
If the new stiffness is greater than the minimum stiffness, then go to Step 2.

If the new stiffness is less than the minimum stiffness, then go to Step 6 (b).

If the stress and moment are OK, then go to Step 7.

- b) If pile stiffness has been reduced to the minimum, then the designer must do one of the following before going to Step 2:
  - i) For excessive transverse force, first add an intermediate wing (a maximum of two) and/or square off the exterior wings.
  - ii) For excessive longitudinal force, first try deepening the abutment beam by 6" min. 12" max.

- iii) If (i) and (ii) does't fix the problem, then try using a larger size pile or more piles and go to Step 2.
- iv) As a last resort, if the abutment is still overloaded, try stiffening the intermediate bents by using larger columns or larger piles or more piles at the intermediate bents.



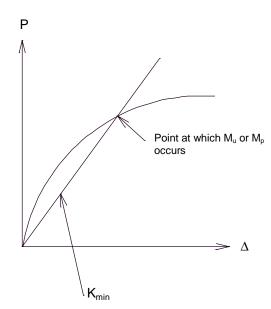


Figure 6.1.2.10-2 Definition of K<sub>min</sub>

# 7) Abutment Displacements:

Check the displacements at the master joint (see Section 6.1.2.10.3). If the abutment displacements are less than the allowable, then go to Step 8. If the abutment displacements are greater than the allowable, then the designer must do one of the following before going to Step 2:

- i) Add abutment piles.
- ii) Use larger size abutment piles.
- iii) For excessive transverse displacement, add an intermediate wing (a maximum of two) and/or square off the exterior wings.
- iv) For excessive longitudinal displacement, deepen the abutment beam by 6" min. 12" max.
- v) If the abutment is still overloaded, try stiffening the intermediate bents by using larger columns or larger piles or more piles at the intermediate bents.
- vi) As a last resort, see the Structural Design Engineer about specifying the backfill soil properties.

#### 8) Complete the Seismic Design:

Return to the checklist and/or flowchart in Section 6.1.2.2, then design abutment components, connections and intermediate bents as described in Section 6.1.3. If the seismic response of the bridge changes as a result of the design being different from the model assumed, then return to Step 2.

## 2.10.1 - Soil Pressures, Backwall and Wings

# Compacted Backfill Soil at Abutments

Ultimate soil capacities should be used for seismic design.

#### AASHTO Division I-A Sections 6.4.2(B) and 7.4.2(B)

It is not necessary to check resultant soil pressures. The longitudinal failure state of an abutment is taken to be when the ultimate soil pressure acts on the entire backwall, causing global failure of the sliding wedge of soil behind the backwall. The transverse failure state is taken to be when the ultimate soil pressure acts on the entire wing area, causing global failure of the sliding wedge of soil behind the wings. The actual distribution of stresses in compacted abutment fill is too complex to compute for cyclical seismic loads, and it is the global failure rather that a local failure that controls the ultimate capacity of the abutment soil. Therefore, check the backwall pressure normal to its plane, then check the wing pressure normal to its plane, considering them to be independent of each other.

$$p = \frac{F}{A} \le p_A$$

p = pressure on the planar surface of the backwall or wing, ksf

F = Force on element obtained from Rigid Body Transformation (see Section 6.1.2.7), kips. Check all seismic loading cases including both abutments and both load combinations:

Case I = 
$$1.0*L+0.3*T$$
  
Case II =  $0.3*L+1.0*T$ 

A = Area of the backwall or wing, square feet

 $p_A$  (for integral and non-integral abutments) = 7.7ksf = the maximum (ultimate) dynamic soil passive pressure, ksf. The maximum dynamic soil passive pressure,  $p_A$ , shall be reduced for backwall heights less than 8 feet. For example:  $p_A$  for a backwall height of 6 feet.  $p_A$  = 7.7\*(6/8) = 5.8 ksf.

If  $p > p_A$ , then reduce the stiffness as described below and iterate until the pressure is just barely less than the allowable.

$$K_{i+1} = \frac{A^*p_A}{\delta_i}$$
 = trial stiffness for the i+1 run, kips/foot

 $\delta_{\text{i}}$  = displacement of backwall or wing from the i run, feet

Return to the checklist and/or flowchart in Section 6.1.2.10.

#### 2.10.2 - Abutment Pile Stresses

#### Abutment Pile Stresses

The allowable pile stress is the ultimate pile strength.

AASHTO Division I-A Sections 6.4.2(C) and 7.4.2(C)

In order for the estimated pile stiffnesses to be valid, the pile stresses must be below the ultimate pile stress (i.e. R=1).

AASHTO Division I-A, 1992 Commentary C5.4.2

Non-Integral Abutments:

Consider non-integral abutment piles as "foundation" piles in AASHTO Div. I-A, 7.2.1(B), with R=1, and do not allow plastic hinging.

Integral Abutments:

Use R=1 for ALL end bent piles, including those on integral end bents.

#### **Concrete CIP Piles**

- 1) Before running a seismic analysis program such as SEISAB, run one p-y curve program such as COM624P to obtain the stiffness and the lateral load-lateral displacement relationships as described in Section 6.1.2.6.4.
- 2) After SEISAB & RBT have been run, rerun COM624P to obtain the moment demand ( $M_R$ ) due to the resultant applied lateral pile load,  $P_R$ .
- 3) From the same or other COM624P programs, the resultant ultimate moment capacity, ( $M_u$ ) can be obtained at the demand axial loads  $P = DL \pm EQ$ . For seismic load Case I and Case II, check the following criteria:

 $M_R \le M_u$ , where:

 $M_R$  = maximum resultant moment demand at the demand axial load, P=DL  $\pm$  EQ, and at the demand resultant lateral load,  $P_R$ , ft.\*kips

$$P_R = \sqrt{P_x^2 + P_y^2}$$
, resultant applied lateral load, kips

 $P_x$  or  $P_y$  = applied lateral load at the pile-head from the RBT, in the longitudinal and transverse directions respectively, kips

 $M_u$  = ultimate moment capacity at the demand axial load, at P = DL  $\pm$  EQ, and at a limit state of  $\epsilon_c$ = 0.003 (concrete) or  $\epsilon_s$ = 0.015 (steel).

If  $M_R > M_u$ , then reduce the pile stiffnesses in both the long. and trans. directions according to the following equation:

$$K_{\text{new}} = \frac{P_x^{'}}{H_x} \text{ or } \frac{P_y^{'}}{H_y}$$
, where:

 $K_{\text{new}}$  = stiffness for new trial run, kips/foot, in the strong or weak directions.

 $P_x$ ' and  $P_y$ ' = pile-head lateral force on pile lateral load - lateral displacement curve as described is Section 6.1.2.6.4 in the long. and trans. directions, respectively.

 $H_{x}$  and  $H_{y}$  = pile-head lateral displacements in the long. and trans. direction, respectively, from RBT.

Return to the checklist or flowchart of Section 6.1.2.10.

#### Steel HP Piles

- Before running a seismic analysis program such as SEISAB, run two p-y curve programs such as COM624P: one for the strong direction, and one for the weak direction to obtain pile lateral load – lateral displacement curves in the strong and weak directions.
- 2) After SEISAB & RBT have been run, rerun COM624P to obtain the maximum demand moments along the pile in the strong direction  $(M_x)$  and weak direction  $(M_y)$ . To obtain  $M_x$ , run COM624P with the pile demand axial load, P=DL  $\pm$  EQ and the pile lateral load in the strong direction  $(P_x)$ . To obtain  $M_y$ , run another COM624P with the pile demand axial load, P=DL  $\pm$  EQ, and the pile lateral load in the weak direction  $(P_y)$ . These two COM624P programs will have different pile section properties. Run both programs for load case I and load case II.
- 3) All piles must meet the following equation:

$$\frac{P}{0.85A_{s}F_{y}} + \frac{M_{x}}{M_{px}} + \frac{M_{y}}{M_{py}} \le 1.0$$
 (1)

**AASHTO 10.54.2** 

where:

P = applied axial load (DL  $\pm$  EQ), kips

 $M_x$  and  $M_y$  = maximum moment demand at the above axial load, P, at the corresponding lateral load,  $P_x$  or  $P_v$ .

 $A_s$  = steel area, square inches

 $F_y$  = yield stress of steel, usually 36 ksi or 50 ksi. The difference in price is small, so 50 ksi should be used when steel stresses are high.

 $M_{\rm p}=Z^*F_y,$  where Z = plastic section modulus in the strong (x) or weak (y) direction, inch\*kips

4) If eq. (1) can not be satisfied, then reduce the pile stiffness in both the strong and weak directions according to the following equation:

$$K_{\text{new}} = \frac{P_x^{'}}{H_x} \text{ or } \frac{P_y^{'}}{H_y}$$
, where:

 $K_{\text{new}}$  = stiffness for new trial run, kips/foot, in the strong or weak directions.

 $P_x$ ' and  $P_y$ ' = pile-head lateral force on pile lateral load - lateral displacement curve as described is Section 6.1.2.6.4 in the long. and trans. directions, respectively.

 $H_x$  and  $H_y$  = pile-head lateral displacements in the long. and trans. direction, respectively, from RBT.

5) Return to the checklist or flowchart of Section 6.1.2.10.

#### 2.10.3 - Abutment Deflection Iteration

In Iterative Abutment Analysis (see Figure 6.1.2.10-1), after the abutment forces are OK, the resultant abutment displacement must also be acceptable before finishing the seismic analysis of the bridge.

AASHTO Division I-A, 1998 Commentary, C4.5.2

 $\delta_R \leq \delta_{\text{allowable}}$  where:

 $\delta_{\text{R}}$  = resultant displacement of the master joint from the seismic analysis, feet

$$\begin{split} &\delta_{R3} = \sqrt{\delta_L^2 + (\delta_{0.3T})^2} \text{ , for Case I = L+0.3T} \\ &\delta_{R4} = \sqrt{(\delta_{0.3L})^2 + \delta_T^2} \text{ , for Case II = 0.3L+T} \end{split}$$

 $\delta_R$  is at the master joint (see Figure 6.1.2.10.3-1), using either CQC or SRSS.

 $\delta_{\text{allowable}}$  = 0.3 feet, for integral abutments and non-integral abutments with restrainers engaged.

 $\delta_{\text{allowable}} = 10^*\text{A}$ , inches, for non-integral abutments under active Mononobe - Okabe pressure, where A = Acceleration Coefficient in g's.

AASHTO Division I-A, 1998 Commentary

If the displacement exceeds the allowable value, then the abutment must be structurally altered as described in the flowchart description of Section 6.1.2.10. If the structural behavior is different as a result of these changes, it will be necessary to redesign the bridge and the abutment for Group I-VI loads and for Seismic loads.

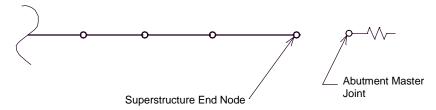


Figure 6.1.2.10.3-1 Abutment Master Joint

# 3.1 - Connection Design

#### Seismic Performance Categories A, B, C, D

Seismic design forces can be considered either service loads or factored loads with a factor of 1.0. Load Factor Design (LFD) is to be used wherever possible. However, Allowable Stress Design (ASD) is still allowed when LFD would be difficult to apply. Connections must be designed for seismic forces in all four Seismic Performance Categories (A, B, C and D). For design of some typical seismic connections, see the Section Numbers below:

- a) Anchor bolts (6.1.3.1.1)
- b) Dowel rods (6.1.3.1.2)
- c) Restrainer rods (6.1.3.1.3)
- d) Concrete shear blocks (6.1.3.1.4)
- e) Concrete end diaphragms (6.1.3.1.5)
- f) Seismic isolation systems (6.1.3.1.6)
- g) Joints (Beam/Column or Column/Footing) (6.1.3.1.7)

# Seismic Performance Category A

Minimum horizontal design force in each restrained direction for connections in SPC A is as described in AASHTO Division I-A, Section 5.2.

#### AASHTO Division I-A, Section 5.2

A seismic analysis is not required in SPC A, so do not use R=0.8 in SPC A. Use R=1 instead.

AASHTO Division I-A, Sections 5.4, 5.5 and 5.6

# Seismic Performance Categories B, C and D

For design of connections in SPC B, C and D, see AASHTO Division I-A, Sections 6.2.1 and 7.2.1(A). For design of column joint connections in SPC C and D, see AASHTO Division I-A, Section 7.6.4 and Bridge Manual Section 6.1.3.1.7.

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## 3.1.1 - Anchor Bolts

#### **Anchor Bolts**

Anchor bolts are used on bearings with sole plates. Design anchor bolts for flexure, shear and axial forces. Design forces are specified in AASHTO Div. I-A, Sections 3.6, 3.7, 5.2, 6.2 or 7.2. Design strengths are from AASHTO Table 10.56A, LFD, for ASTM A325 bolts, unless otherwise noted.

#### Flexural Stress

For flexural stress, design the bolt diameter to satisfy the allowable stress as shown below. Limit the number of bolts per bearing to four by adding concrete shear blocks when required.

$$f_b = \frac{M}{S} \le F_b$$

$$M = \frac{PL}{2}$$
 = maximum moment per bolt, inch\*kips

L = moment arm from center of sole plate to top of the beam cap, inches

$$P = \frac{F_H}{n_b N_g R} = \text{Horizontal seismic design force per bolt, kips}$$

$$F_{\scriptscriptstyle H}$$
 = Horizontal seismic force as shown below, kips.=  $\sqrt{(F_{\scriptscriptstyle T})^2+(F_{\scriptscriptstyle L})^2}$ 

#### F<sub>H</sub> in Seismic Performance Category A

For expansion bearings, transverse  $F_T$  = 0.2(DL) & longitudinal  $F_L$  = 0. Where DL = maximum dead load girder reaction at the bent, kips. For fixed bearings, Transverse  $F_T$  = 0.2(DL)

Longitudinal  $F_L$  = (0.2)(segment weight)/(# of girders).

Segment weight should be distributed appropriately among fixed bents. See also Bridge Manual section 3.31, page 2.8-2 & AASHTO Division I-A, Section 5.2

#### F<sub>H</sub> in Seismic Performance Categories B, C and D

At intermediate bents, 
$$F_{H} = \sqrt{\left(\sum V_{L}\right)^{2} + \left(\sum V_{T}\right)^{2}}$$
 , where:

 $\Sigma V_L$ = summation of top of column longitudinal shears at all columns  $\Sigma V_T$ = summation of top of column transverse shears at all columns At end bents, use the same formula as above, except substitute the abutment shears in place of the top of column shears.

n<sub>b</sub>= the number of bolts per girder

N<sub>G</sub>= the number of girders at the bent

R = 1.0 for Seismic Performance Category A,

0.8 for Seismic Performance Categories B, C and D

S = Section modulus for the bolt =  $\frac{\pi D^3}{32}$ , cubic inches.

D = bolt diameter, inches. The gross bolt diameter may be used because the bolt is unthreaded in the flexural zone.

 $F_b$  = (overstress factor=1.5)\*0.55\*( $F_v$ =50 ksi) = 41.25 ksi

#### **Shear Stress**

For shear stress, design the bolt diameter to satisfy the allowable stress as shown below ( $f_v < F_v$ ). Limit the number of bolts per bearing to four by adding concrete shear blocks when required.

$$f_v = \frac{P}{A} \le F_v$$

f<sub>v</sub> = actual shear stress on the bolt, ksi

P = the design shear force per bolt, kips/bolt = 
$$\frac{F}{n_b N_g R}$$
,

where the definitions are the same as in the flexural stress section.

 $F_v$ = allowable shear stress per bolt, ksi = (28.5 ksi)\*(f1)\*(f2)\*(f3)

where:

28.5 ksi = 1.5x19 ksi, where 19 ksi is from AASHTO Table 10.32.3B

f1 = 0.875 for bolts > 1" diameter, 1.0 for bolt diameters ≤ 1"

f2 = 1.25 for threads not in the shear plane (use)

f2 = 1.0 for threads in the shear plane (don't use)

f3 = 0.8 when distance between outermost bolts > 50" (rare)

f3 = 1.0 when distance between outermost bolts < 50" (usual case).

For most anchor bolts,  $F_v = 28.5*0.875*1.25 = 31.17$  ksi.

$$A = \frac{\pi D^2}{4}$$
 = Area of bolt, square inches

D = The gross bolt diameter, because bolt is unthreaded in the shear zone.

#### **Axial Stress**

For axial stress, design the bolt diameter to satisfy the allowable tensile stress as shown below. For further information about vertical restrainers (hold-down devices), see Section 6.1.3.1.3.

$$f_t = \frac{T}{A_t} \le F_t$$

where

f<sub>t</sub> = applied tensile stress, ksi

T = the maximum seismic tensile (uplift) force (DL  $\pm$  EQ) per girder from the seismic analysis, kips. If (DL+EQ) and (DL-EQ) are both compressive, then there is no need to design the bolts for axial stress.

A<sub>t</sub> = tensile area of bolt =

1.41 sq. in. for 1-1/2" diam. bolt

2.50 sq. in. for 2" diam. bolt

4.00 sq. in. for 2-1/2" diam. bolt

F<sub>t</sub> = allowable tensile stress = 68 ksi

#### 3.1.2 - Dowel Rods

## **Dowel Rods**

Dowel rods connect standard concrete diaphragms and beams on concrete girder bridges (standard fixed diaphragms are those with beam stirrups NOT extending up into the diaphragm). Dowel rods are standard rebars designed using Allowable Stress Design and an allowable overstress of 33%. Design forces are as specified in AASHTO Div. I-A, Sections 3.6, 3.7, 5.2, 6.2 or 7.2. The length of dowel bars is determined by development length into the beam and development length into the diaphragm.

#### Shear Stress

For shear stress, design the size and number of dowel rods to satisfy the allowable stress as shown below ( $f_v < F_v$ ). The number of dowels must also fit into the space available on the key:

min. bar size = #6 max. bar size = #11 min. spacing = 6" max. spacing = 18"

min. end distance=3" max. end distance=9" ( $\leq$  half the spacing)

$$f_v = \frac{P}{A} \le F_v$$

 $f_v$  = actual shear stress on the dowel, ksi

P = the design shear force per dowel, kips/dowel =  $\frac{F_H}{n_d R}$ , where:

 $F_{H}$  = Horizontal seismic force as shown below, kips =  $\sqrt{\left(F_{T}\right)^{2}+\left(F_{L}\right)^{2}}$ 

#### F<sub>H</sub> in Seismic Performance Category A

#### AASHTO Div. I-A, 5.2

Transverse  $F_T = 0.2(DL)$ 

where: DL = the summation of dead load reactions at the bent, kips Longitudinal  $F_L$  =0.2[(segment wt.)/(# of girders)] where segment weight should be distributed appropriately among fixed bents.

## F<sub>H</sub> in Seismic Performance Categories B, C and D

$$F_H = \sqrt{\left(\sum V_L\right)^2 + \left(\sum V_T\right)^2} ,$$

where:  $\Sigma V_L$  = summation of top of column longitudinal shears at all columns  $\Sigma V_T$  = summation of top of column transverse shears at all columns If columns are designed for plastic hinging, use the plastic hinging shear.

n<sub>d</sub> = the number of dowels at the bent

R =1.0 for Seismic Performance Category A,

0.8 for Seismic Performance Categories B, C and D

A = the cross-sectional area of the bar, sq. inches

 $F_v$  = allowable shear stress per dowel = 1.33\*0.4\* $f_v$  = 31.9 ksi / dowel

f<sub>y</sub> = yield stress of the rebar, ksi

### **Axial Stress**

For axial stress, design the total area of bars to satisfy the tensile stress as shown below.

 $f_t = T / (n_d A_d) \le F_t$ 

where:

f<sub>t</sub> = applied tensile stress, ksi / dowel

T = seismic tensile (uplift) force (DL  $\pm$  EQ) at bent, kips. If both (DL+EQ) and (DL-EQ) are compressive, then there is no need to design the dowels for axial stress.

 $n_d$  = the number of dowels at the bent

 $A_d^{\text{d}}$  = cross-sectional area of one bar, sq. inches  $F_t$  = allowable tensile stress per dowel = 1.33\*0.55\* $f_y$  = 43.9 ksi / dowel

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### 3.1.3 Restrainers

Most restrainer rods are low-carbon steel (ASTM A307,  $F_u$ =60ksi,  $F_y$ 36ksi) threaded rods at expansion gaps and hinges. They can be either longitudinal, transverse or vertical restrainers, depending on their axis of orientation. Restrainers are designed to remain elastic. Design forces are as specified in AASHTO Div. I-A, Sections 3.6, 3.7, 5.2, 6.2 or 7.2. Design tensile strengths are from AASHTO Table 10.56A for ASTM A307 rods. Allowable tensile stress  $F_t$  = 30 ksi on the tensile stress area of the rod. Tensile stress areas of available threaded rod sizes are in the AISC manual and in the ASTM A307 specification.

### Longitudinal Restrainers

Longitudinal restrainers may be added at expansion gaps when predicted seismic displacements exceed the available support length. Restrainers should be added at all hinges with expansion gaps. Restrainers may also be added in other situations as discussed in a retrofit strategy meeting. Omit restrainers on exterior faces of exterior girders. Locate the restrainer group as close as possible to the center of gravity (c.g.) of the superstructure (see Figure 6.1.3.1.3-3). Orient the restrainers parallel to the centerline of the superstructure, except for expansion joints on bridges with skew > 30 degrees and all curved bridges, then consider orienting the restrainers normal to the joint. If the restrainer is connected to the bent cap, a higher force may be directed to the columns than otherwise expected, and the bent should be designed to withstand the restrainer force. See Figures 6.1.3.1.3-3 - 6.1.3.1.3-9 at the end of this section for the details for Longitudinal Earthquake Restrainers for the different superstructure types.

### Restrainer Rod Design:

### **Restrainer Capacity**

 $F_{cap}$  = force capacity of restrainer in kips, the smaller of these forces:

a)  $A_t * F_t$  where:

A<sub>t</sub> = tensile stress area of threaded rod from AISC manual

 $F_t = 30 \text{ ksi} = \text{allowable tensile stress}$ , from AASHTO Table 10.56A

b) 0.35\*DS/n where:

DS = dead load of the entire superstructure unit, kips. When two segments are tied together, use the weight of the heavier segment.

n = the number of restrainers at the expansion gap

### **Restrainer Demand**

F<sub>dem</sub>= demand force in kips, taken to be the larger of these forces:

 a) force from seismic analysis divided by the response factor, R, where:

R = 1.0 for Seismic Performance Category A

R = 0.8 for Seismic Performance Categories B, C and D

b) 0.2\*DS/n where:

DS = dead load of the entire superstructure unit, kips. When two segments are tied together, use the weight of the heavier segment.

n = the number of restrainers at the expansion gap

c) A\*DL/n where:

A = Acceleration coefficient in g's

DL = the weight of the lighter of the two adjoining superstructure segments n = the number of restrainers at the expansion gap

### Example 6.1.3.1.3-1:

The accumulated dead load weight of a prestressed bridge segment with six girders is 1100 kips. The bridge is located in Seismic Performance Category C with A=0.25. There are  $2-1\frac{3}{8}$  inch diameter restrainers for each girder at the end bent. From the seismic analysis, the total longitudinal force at the expansion gap is 300 kips. Check the suitability of the restrainers.

### Solution:

Demand Force: 1) 0.2\*DS/n = 0.2x1110/(2x6) = 18.5 kips 2) A\*DS/n = 0.25x1110/(2x6) = 23.1 kips 3) (F/R)/n = (300/0.8)/12 = 31.25 kips  $\leftarrow$  **Controls** 

Design Capacity: 1)  $0.35xDS/n = 0.35x1110/(2x6) = 32.37 \text{ kips} \leftarrow \textbf{Controls}$ 2)  $A_t * F_t = 1.16 \text{in}^2 x 30 \text{ksi} = 34.8 \text{ kips}$ 

32.37 kips > 31,25 kips Capacity is O.K.

 $\therefore$  Two -1 $\frac{3}{8}$  diameter rods for each girder are satisfactory.

Note: Usually, restrainers should be omitted on the exterior face of exterior girders. For exterior girders, the two restrainers should be located on the interior face of the girder.

### **Anchor Stud Design**

Anchor studs shall be designed using ultimate strength design and concrete shear cone failure theory. The standard stud size is  $7/8" \phi \times 7"$  stud. Use a response modification factor for connections of 0.8.

Locate the studs on the concrete backwall or diaphragm using the minimum spacing, 2R, and the minimum edge distance, R, where R is the major radius of the concrete shear cone as shown in Figure 6.1.3.1.3-1. If the minimum spacing or minimum edge distance cannot be met, then see manufacturer's catalog for computation of partial cone strength reductions. If possible, center the stud group around the restrainer rod.

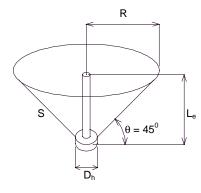


Figure 6.1.3.1.3-1 Concrete Shear Cone for Anchor Stud

### Anchor Plate Design

The area of the steel anchor plate shall be sized by the number of anchor studs required for tensile pullout and by the stud spacing (2R above) and edge distance on the plate. Locate the studs on the backwall or diaphragm using the minimum spacing, 2R, and the minimum edge distance, R. If the minimum spacing or minimum edge distance cannot be met, then consider the partial cone strength reductions. If possible, center the stud group around the restrainer rod. The thickness of the plate shall be sized by:

(a) Flexural stress on the plate considering the plate as a beam continuousover-simple-supports with an allowable stress of 0.55F<sub>v</sub> and a 33% allowable overstress in Seismic Performance Categories B, C and D,

AASHTO Division I-A, Sections 6.2.1 & 7.2.1 and AASHTO Table 10.32.1A

(b) Bearing stress on concrete (to account for the possibilities of local crushing at the expansion gap and/or restrainer deflection greater than 1/2"

and/or backwall knockoff) of 0.3\*f 'c, with a multiplier,  $\sqrt{\frac{A_2}{A_1}}$ , (where A<sub>1</sub> is the

loaded area and A2 is the maximum area of the portion of the supporting surface that is geometrically similar and concentric with the loaded area), plus a 33% allowable overstress in Seismic Performance Categories B, C and D. or

AASHTO Division I-A, Sections 6.2.1 & 7.2.1 and AASHTO 8.15.2.1.3

(c) minimum plate thickness = 3/8"

The backwall should be designed for flexure and shear as specified for abutment components in Section 6.1.3.2.

### Transverse Restrainers

Transverse restrainers are mainly used to keep the superstructure from sliding off the bearings. This type of restrainer is used either in place of, or along with, concrete shear blocks. The design procedure for transverse restrainers is the same as the design procedure for longitudinal restrainers with the exception that the demand force, F<sub>dem</sub>, is only part a) of the longitudinal restrainer demand force design.

### Vertical Restrainers (Hold-down Devices)

Vertical restrainers are only required in Seismic Performance Categories C and D (AASHTO Div. I-A, 7.2.5(B)), but they may also be used on important structures in SPC B. Vertical restrainers shall be used at all supports or hinges in continuous structures when the vertical seismic force (EQ) exceeds 50% of the dead load reaction (DR).

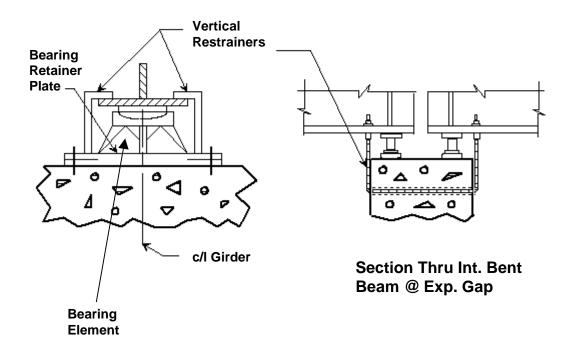
When 0.5(DR) < EQ < 1.0(DR), then the minimum net uplift force = 10% of the dead load downward force that would be exerted if the span were simply supported.

When EQ > 1.0(DR), then the net uplift force = 1.2\*(EQ-DR), but not less than 10% of the dead load downward force that would be exerted if the span were simply supported.

Vertical restrainers can take several forms: (a) using existing anchor bolts, (b) adding threaded rods, (c) adding vertical restraining plates, or (d) adding prestressing strands. If vertical restrainers are required, see the Structural

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Project Manager to determine which vertical restrainer system should be used.

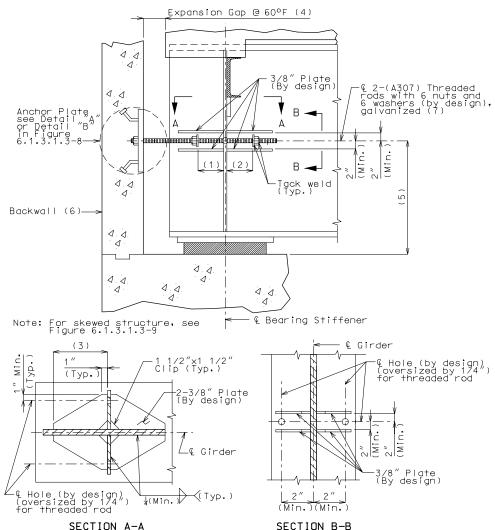


**End Section Thru Girder** 

Section 6.1.3.1.3-2 Examples of Vertical Restrainers

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Seismic Design Procedure



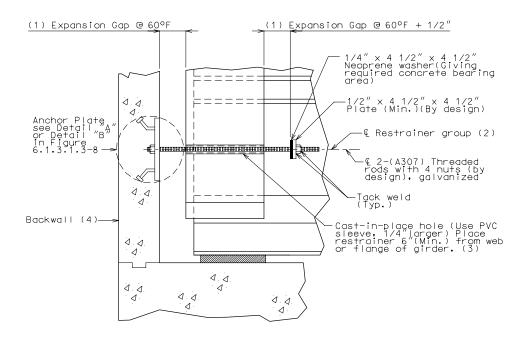
- (1) (Expansion Gap @  $60^{\circ}$  F) + 1/2''.
- (2) Expansion Gap @ 60° F.
- (3) Design length as required for the weld to develop the seismic force.
- (4) On skewed structures, adjust this distance parallel to the C/L of roadway.
- (5) Locate the restrainer as close as possible to the neutral axis of the superstructure and as close as possible to the bottom of the diaphragm.
- (6) End bent backwalls are to be designed for active seismic soil pressure as described in Section 6.1.3.2.
- (7) Omit restrainers on exterior faces of exterior girders.

FIGURE 6.1.3.1.3-3 LONGITUDINAL RESTRAINERS (END BENTS-STEEL GIRDERS)

New: April 2000

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Seismic Design Procedure



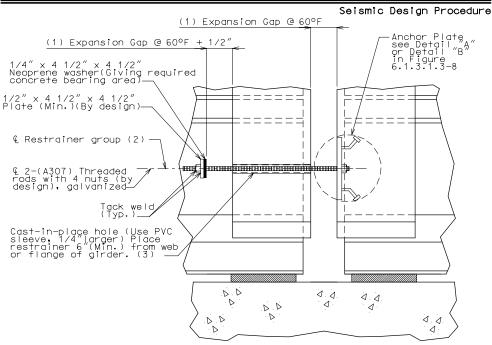
Note: For skewed structure, see Figure 6.1.3.1.3-9

- (1) On skewed structures, adjust this distance parallel to the C/L of roadway.
- (2) Locate at the center of gravity of the superstructure, using the spacing between girders. If different beam depths are used, locate the restrainers at the neutral axis of the smaller beam. May adjust for clearance.
- (3) Omit restrainers on exterior faces of exterior girders.
- (4) End bent backwalls are to be designed for active seismic soil pressure as described in Section 6.1.3.2.

FIGURE 6.1.3.1.3-4 LONGITUDINAL RESTRAINERS (END BENTS-CONCRETE GIRDERS)

### Seismic Design - Section 6.1

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Note: For skewed structure, see Figure 6.1.3.1.3-9

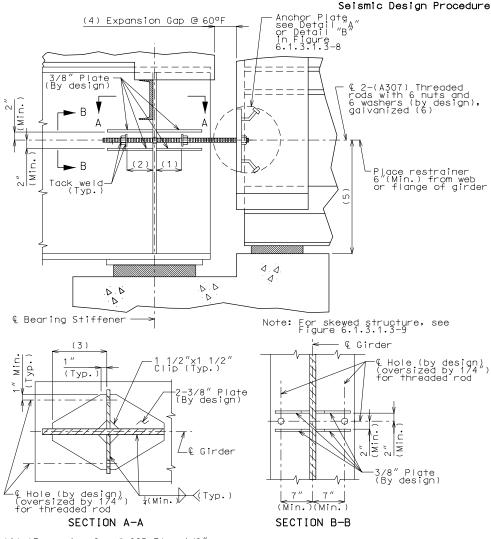
Y₀ = GRAVITY NEUTRAL AXIS OF PRESTRESSED I-GIRDERS (**)					
ROADWAY	GIRDER SPACING	GIRDER TYPE			
		III	ΙV	VI	VII
26′-0″	7′-6″	32.7	36.5	41.1	54.2
28′-0″	8'-2"	33.2	37.0	41.6	54.9
30′-0″	8′-8″	33.6	37.5	42.1	55.5
32′-0″	9′-2″	33.9	37.9	42.6	56.1
36′-0″	8′-2″	33.2	37.1	41.7	55.0
38′-0″	8′-8″	33.5	37.4	42.1	55.5
40′-0″	9′-0″	33.8	37.8	42.5	55.9
44′-0″	9′-9″	34.4	38.4	43.2	56.8

 $*Y_b = Inches from bottom of beam, based on an 8 1/2" slab.$ 

- (1) On skewed structures, adjust this distance parallel to the C/L of roadway.
- (2) Locate at the center of gravity of the superstructure. Use the gravity neutral axis of the composite section, using the spacing between girders. If different beam depths are used, locate the restrainers at the neutral axis of the smaller beam. May adjust for clearance.
- (3) Omit restrainers on exterior faces of exterior girders.

FIGURE 6.1.3.1.3-5 LONGITUDINAL RESTRAINERS (INTERMEDIATE BENTS-CONCRETE GIRDERS)

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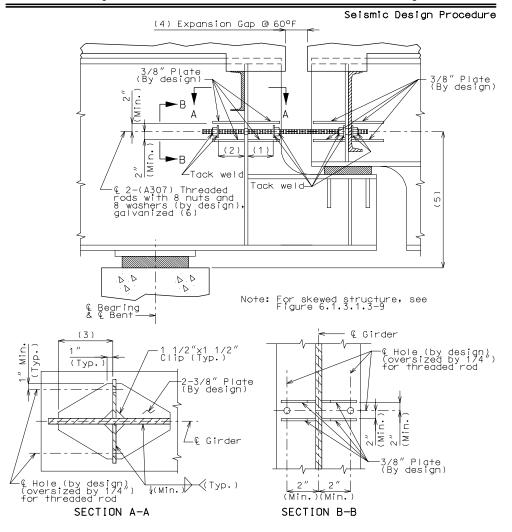


- (1) (Expansion Gap @  $60^{\circ}$  F) + 1/2''.
- (2) Expansion Gap @ 60° F.
- (3) Design length as required for the weld to develop the seismic force.
- (4) Dn skewed structures, adjust this distance parallel to the C/L of roadway.
- (5) Locate the restrainer as close as possible to the neutral axis of the superstructure. Use the gravity neutral axis of the composite section, using the spacing between girders. It different beam depths are used, locate the restrainers at the neutral axis of the smaller beam. Adjust the restrainer to clear channel and shop weld. Larger bracing is required for P/S to Steel beam restrainers.
- (6) Omit restrainers on exterior faces of exterior girders.

FIGURE 6.1.3.1.3-6 LONGITUDINAL RESTRAINERS (INTERMEDIATE BENTS-STEEL TO CONCRETE GIRDERS)

### Seismic Design - Section 6.1

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- (1) (Expansion Gap @  $60^{\circ}$  F) + 1/2''.
- (2) Expansion Gap @ 60° F.
- (3) Design length as required for the weld to develop the seismic force.
- (4) On skewed structures, adjust this distance parallel to the C/L of roadway.
- (5) Locate the restrainer as close as possible to the neutral axis of the superstructure and as close as possible to the bottom of the diaphragm. Use the gravity neutral axis of the girder, using the spacing between girders. If different beam depths are used, locate the restrainers at the neutral axis of the smaller beam. Adjust the restrainer to clear channel and shop weld.
- (6) Dmit restrainers on exterior faces of exterior girders.

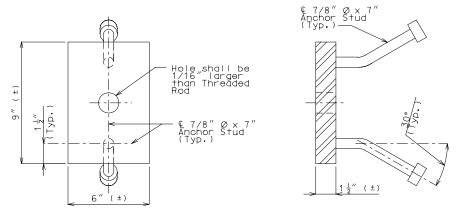
FIGURE 6.1.3.1.3-7 LONGITUDINAL RESTRAINERS (HINGED CONNECTION)

### Seismic Design - Section 6.1

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Seismic Design Procedure

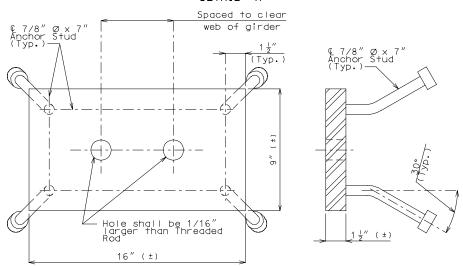
Note: Use Detail "A" for P/S I-Girder Structures at End and Int. Bents and also for all exterior girders on inside face.



ELEVATION OF ANCHOR PLATE

SECTION THRU ANCHOR PLATE

### DETAIL "A"



ELEVATION OF ANCHOR PLATE

SECTION THRU ANCHOR PLATE

DETAIL "B"

Note: Use Detail "B" for Steel Structures at End Bents or P/S I-Girders to Steel Structures at Int. Bents or whenever more than two restrainers occupy one anchor plate.

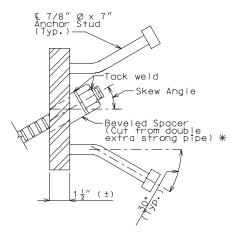
Pull-out 32K per stud. Working stress load 16K per stud. (See TRW Nelson Division Catalog.)

FIGURE 6.1.3.1.3-8
DETAILS "A" AND "B" FOR ANCHOR PLATES

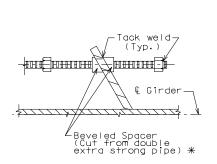
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Seismic Design Procedure

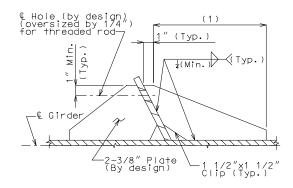
\* For Dimension and Properties of Pipe, see AISC Steel Construction Manual Part 1.



SKEWED ANCHOR PLATE DETAIL



BEVELED SPACER DETAIL (SKEWED STEEL GIRDERS)



CONNECTION PLATE DETAIL (SKEWED STEEL GIRDERS)

(1) Design length as required for the weld to develop the seismic force.

FIGURE 6.1.3.1.3-9
DETAILS FOR LONGITUDINAL
RESTRAINERS ON SKEWED STRUCTURES

### 3.1.4 – Concrete Shear Blocks

Concrete shear blocks are used when 4 anchor bolts per bearing are insufficient, or for preventing loss of support on beams and stub bent footings. Design shear keys as specified in AASHTO 8.16.6.4. Design forces are as specified in AASHTO Div. I-A, Sections 3.6, 3.7, 5.2, 6.2 or 7.2. The following dimensions and sizes are for rough guidelines only and may be altered to fit specific situations:

Concrete block dimensions:

L = Length shall extend all the way across the beam (for ease of forming), oriented parallel to centerline of roadway.

W = Width is as required for concrete area. Allow about 1/2" (typical) clearance between the edge of the sole plate and the edge of the block to allow engaging of anchor bolts.

H = Height of shear block shall extend to about an inch (+/-) above the top of the sole plate.

Steel reinforcement:

Bar size = #4 min. to # 6 max. hairpins placed parallel to the centerline of the beam, with #4 horizontal straight bars at the top of the hairpin to ensure proper alignment.

Spacing = Spacing of hairpin shear bars as required to provide the required steel area, with 6" minimum to 12" maximum. The maximum edge distance in the direction of the spacing = half of reinforcement spacing.

$$V_{\text{dem.}} = \frac{F_T}{R*\phi*N_B} = \text{demand shear per block, kips/block where:}$$

 $F_{\text{T}}=$  transverse component of total horizontal seismic force demand at the bent, normal to the centerline of the roadway, kips. Both seismic load cases, Case 1=L+0.3T and Case 2=0.3L+T, must be satisfied.

R = 1.0 for Seismic Performance Category A 0.8 for Seismic Performance Categories B, C and D

 $\phi = 0.85$  for shear

 $N_B$  = the number of blocks resisting the seismic force. The designer should consider using a value of  $N_B$  that is less than the total number of blocks, because all blocks may not resist equal amounts of force.

 $V_{cap} = A_{vf}^* f_v^* \mu = nominal shear capacity of concrete shear block, kips/block$ 

$$\begin{split} &V_{cap} \leq 0.2*f_{c}^{'}*A_{cv}\text{ , kips} \\ &V_{cap} \leq 0.8*A_{cv}\text{ , kips} \end{split}$$

 $A_{vf}$  = cross-sectional area of reinforcing bars at the shear plane, sq. inches  $f_v$  = yield strength of reinforcing bars, ksi

 $\mu = 1.0$  for retrofits (bushhammering > 1/4", in MO.Std.Spec.703.3.21)

 $\mu = 1.4$  for new structures (monolithic construction)

f 'c = final compressive strength of concrete at 28-day cure, ksi

A<sub>cv</sub> = area of concrete block at the shear plane, sq. inches

**Example:** An example of a shear block design can be found in the Bridge Manual Section 3.55.4.1-2.

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Seismic Design Procedure

### 3.1.5 - Concrete End Diaphragms

### Restrainers at Expansion Gaps, Concrete Girders

Design the concrete diaphragm thickness on P/S-I girder bridges with longitudinal restrainers at expansion gaps at abutments or intermediate bents. Check punching shear by Load Factor Design, as per AASHTO 8.16.6.6. Design force is the restrainer force used to size the rods in Section 6.1.3.1.3. In tension, the failure surface is d/2 outside the outermost anchor studs.

# Seismic Design - Section 6.1

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Seismic Design Procedure

### 3.1.6 - Seismic Isolation Bearings

## Isolation Bearings

Seismic isolation bearings shall conform to AASHTO Guide Specifications for Seismic Isolation Design, 1999. Isolation bearings should only be used when specified on the design layout or when required for special retrofit projects. See the Structural Project Manager for approval and for the design specifications for the specific proprietary system to be used.

### 3.1.7 - T- Joint Connections

### Principal Tension and Compression Stresses in Beam-Column Joints

The connections where columns and beams join, or where columns and footings join, should be based on the capacity design for shear and diagonal tension. For most locations, this is a "T"-shaped joint. For the analysis of "knee joints", see Priestley and Seible, 1996.

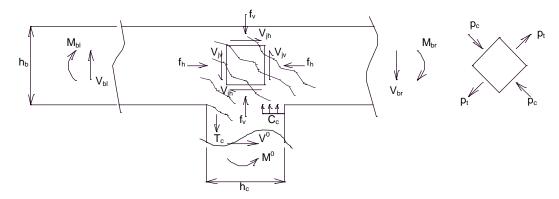


Figure 6.1.3.1.7-1 Joint Shear Stresses in a T-Joint

In the capacity design of connection joints, the column moment,  $M^0$ , will be the moment that is known and which will correspond to flexural overstrength of the column plastic hinges, i.e.  $M^0 = 1.3 M_p$  of the column. If the columns are designed based on plastic hinging, the beam and footings shall be designed with capacities greater than or equal to  $1.3 M_p$ .

At each joint, the principal tension and compression stresses are defined and checked as follows:

$$V_{jh} = \frac{M^0}{h_b} \tag{1}$$

$$v_{jh} = \frac{V_{jh}}{b_{ie}(h_c)} \tag{2}$$

$$b_{je} = \begin{cases} \sqrt{2} D & \text{(circluar column)} \\ h_{c} + b_{c} & \text{(rectangular column)} \end{cases}$$
 (3)

$$V_{jv} = \frac{V_{jh}h_b}{h_c} \tag{4}$$

$$v_{jv} = v_{jh} = \frac{V_{jv}}{b_{je}(h_b)}$$
 (5)

$$f_{v} = \frac{P_{c}}{b_{ie}(h_{c} + h_{b})}$$
 (6)

$$p_{c} = \frac{f_{v} + f_{h}}{2} + \sqrt{\left(\frac{f_{v} - f_{h}}{2}\right)^{2} + v_{jh}^{2}}$$
 (7)

$$p_{t} = \frac{f_{v} + f_{h}}{2} - \sqrt{\left(\frac{f_{v} - f_{h}}{2}\right)^{2} + v_{jh}^{2}}$$
 (8)

in which:

 $V_{jh}$  = Average horizontal shear force within a joint.

 $V_{iv}$  = Average vertical shear force within a joint.

v<sub>ih</sub> = Average horizontal shear stress within a joint.

 $v_{iv}$  = Average vertical shear stress within a joint.

h<sub>b</sub> = Beam depth.

h<sub>c</sub> = Column diameter or rectangular column cross-section height.

b<sub>ie</sub> = The effective width of a joint, defined in Figure 6.1.3.1.7-2.

D = Round column diameter.

 $f_{\nu} =$  Average vertical axial stress due to column axial force  $P_{c}$ , including the seismic component.

 $P_c$  = Column axial force.

f<sub>h</sub> = Average horizontal axial stress at the center of the joint.

pc = Nominal principal compression stress in a joint. (positive)

p<sub>t</sub> = Nominal principal tensile stress in a joint. (negative)

 $b_b = Beam width$ 

b<sub>c</sub> = Column cross-section width

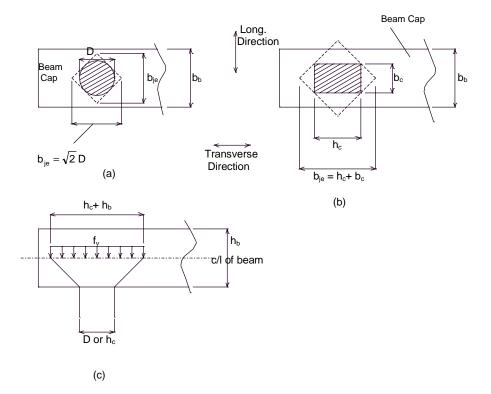


Figure 6.1.3.1.7-2 Effective Joint Width for Joint Shear Stress Calculations

New: April 2000

In Figure 6.1.3.1.7-2(c), the effective width is taken at the center of the column section, allowing a  $45^{\circ}$  spread from boundaries of the column section into the beam cap. In the transverse direction, the effective width will be the smaller of the value given by eq. (3) and the beam cap width  $b_b$ . Experimental evidence indicates that diagonal cracking is initiated in the joint region when  $p_t \geq 3.5 \sqrt{f_c}$  psi. The principal compression stress  $p_c$  shall be limited to  $p_c \leq 0.3 f_c$ .

### Design of Reinforcement for Beam-Column Joints

When the principal tension stress,  $p_t$ , exceeds  $3.5\sqrt{f_c}$  psi, joint cracking occurs and the following reinforcement shall be provided:

a) Vertical beam stirrup reinforcement shall be placed throughout the distance of h<sub>b</sub>/2 from the column face on each side of the column. The required amount of vertical beam stirrup reinforcement, A<sub>iv</sub>, is:

$$A_{jv} = 0.125 A_{sc} \frac{f_{yc}^{o}}{f_{yv}}$$
 (9)

Where:

 $A_{sc}$  = The total area of longitudinal steel

 $f_{vc}^{o}$  = overstrength stress in the column reinforcement use

$$f_{yc}^{o} = 1.1 f_{y}$$

f<sub>vv</sub> = yield stress of vertical stirrup reinforcement.

b) Vertical beam stirrup reinforcement within the joint,  $A_{vi}$ , is  $A_{vi} = 0.0625 A_{sc} \frac{f_{yc}^{o}}{f_{vv}} \tag{10}$ 

c) The additional beam bottom longitudinal reinforcement required is

$$A_{sb} = 0.0625A_{sc} \frac{f_{yc}^{0}}{f_{vb}}$$
 (11)

where  $f_{yb}$  = the yield stress of the beam bottom longitudinal reinforcement. This additional reinforcement must be carried a sufficient distance to develop its yield strength a distance  $h_b/2$  from the column face.

d) The horizontal hoop reinforcement within a joint requires

$$\rho_s = \frac{3.3}{Df_{gh}L_a} \left( \frac{0.09A_{sc}f_{yc}^{o}D}{L_a} - F \right)$$
 (12)

which for F=0 simplifies to

$$\rho_{s} = \frac{0.3A_{sc}f_{yc}^{o}}{L_{a}^{2}f_{yh}}$$
 (13)

Where

F =The beam cap prestress force.

 $f_{vh}$  = The yield stress of the horizontal hoops.

 $L_a$  = The Anchorage length in the joint. The minimum amount of horizontal hoop reinforcement shall be

$$\rho_{s,min} = \frac{3.5\sqrt{f_c'}}{f_{yh}} \tag{14}$$

The spacing of the horizontal hoop can be based on:

$$S = \frac{4A_s}{D'\rho_s}$$
 (15)

Where  $A_s$  = The cross-sectional area of the hoop bar. D' = The hoop diameter.

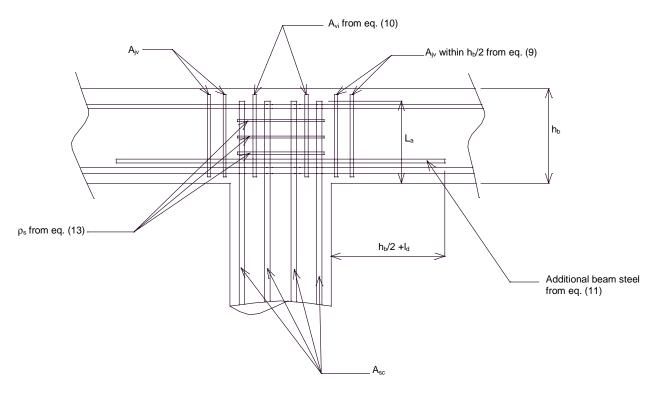


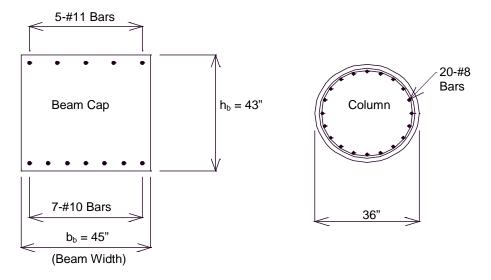
Figure 6.1.3.1.7-3 Beam Cap Joint Reinforcement

When the principal tension stress,  $p_t$ , does not exceed  $3.5\sqrt{f_c}$  psi, no joint cracking is expected. However, the following minimum reinforcement shall be provided:

- a) Vertical beam stirrup reinforcement within the joint based on eq.
- b) Minimum horizontal hoop reinforcement based on eq. (14)

Note that the bending of any hooked reinforcement outward, away from the column core, shall not be used because it directs the anchorage force away from the joint. Inward bending of the column reinforcement is allowed. However, it is likely to cause a congestion problem. The use of straight column reinforcement embedded into the beam-column joint is recommended. The standard T-joint reinforcement details are shown in Figure 6.1.3.1.7-4 - Figure 6.1.3.1.7-6. If any reinforcement requirement based on eqs. (9) through (14) is greater than that shown in Figures 6.1.3.1.7-4 - 6.1.3.1.7-6, the greater requirement shall be used.

**Example 6.1.3.1.7-1:** A column is subjected to an axial load (due to dead and seismic earthquake loads) of 520 kips. The column diameter is 36 inches with 20-#8 bars for longitudinal reinforcement. The beam cap dimensions are 3'-9" wide by 3'-7" deep with 5-#11's for the top reinforcement and 7-#10's for the bottom reinforcement as shown in Figure 6.1.3.1.7-7. The column overstrength moment-axial load curve is shown in Figure 6.1.3.1.7-8. Design the reinforcement details for the beam-column joint.

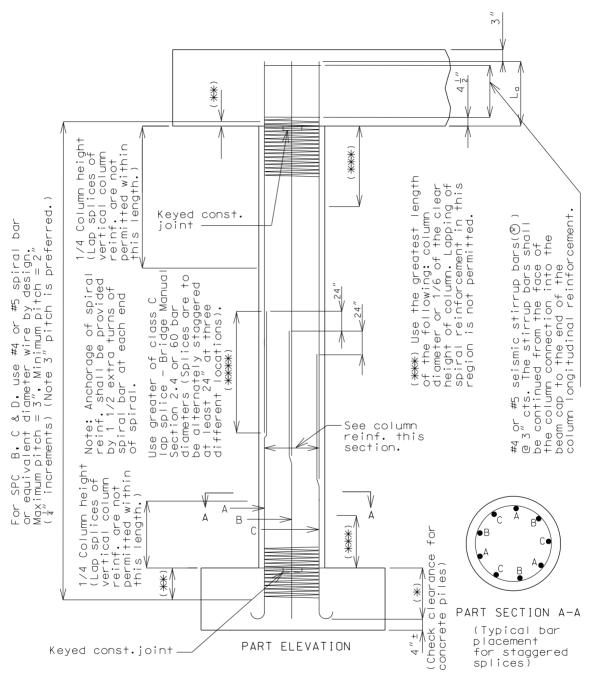


 $f_c' = 3000 \text{ psi and } f_y = 60,000 \text{ psi}$ 

Figure 6.1.3.1.7-7 Properties for Example Design

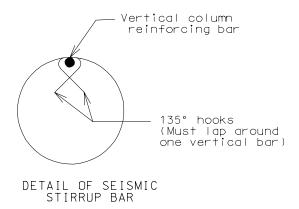
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### Seismic Design Procedure



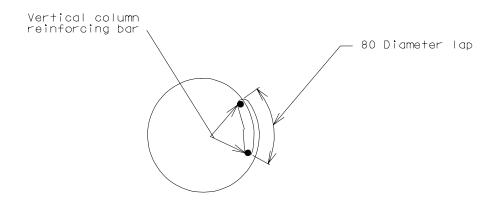
(\*\*) Increase by 25% the development length (other than top bars) or the standard hook in tension "Ldh" of Bridge Manual Section 2.4. (\*\*\*) The spiral bars or wire shall be continued for a distance equal to 1/2 the column diameter but not less than 15" from the face of the column connection into the footing and 1-1/2" from the column connection into the beam cap or the bottom of the beam cap stirrup reinforcing bar. (\*\*\*\*\*\*\*) Splices may be eliminated when column height is 20'-0" or less or restrictions do not practically allow for lap splices.

Figure 6.1.3.1.7-4 Int. Bent "T-Joint" Details

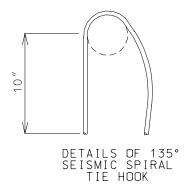


Note: Show the above details on the bridge plans.

### SEISMIC SPIRAL BAR OR WIRE DETAILS

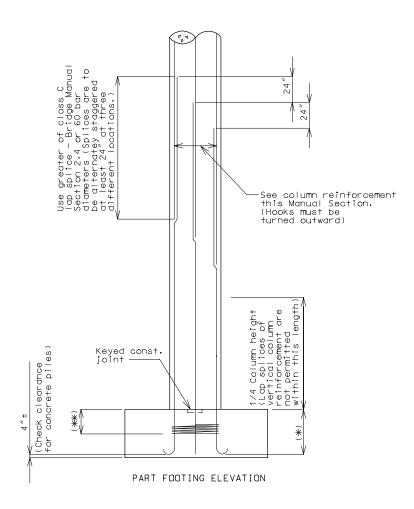


ANCHOR SPLICES IN SPIRAL AROUND VERTICAL BAR (USE FOR INTERMEDIATE SPLICES OF SPIRALS)



Note: Show the above details on the bridge plans.

Figure 6.1.3.1.7-5 Seismic Bar Details



### Notes:

See this Manual Section for footing reinforcement not shown.

\*\* Increase by 25% the development length(Other than top bars) or the standard hook minimum in tension "L<sub>dh</sub>" of Bridge Manual Section 2.4.

\*\*\* The spirals shall be continued for a distance equal to 1/2 the column diameter but not less than 15" from the face of the column connection into the footing.

Figure 6.1.3.1.7-6 Beam - Footing "T-Joint" Details

SD001 New: April 2000

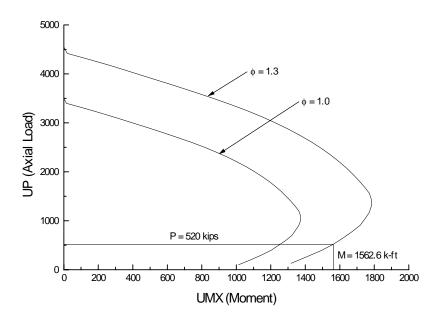


Figure 6.1.3.1.7-8 Column Overstrength Interaction Diagram

### Solution:

The axial load for the column = 520 kips. From Figure 6.1.3.1.7-8,  $M^0$  = 1562.6 k-ft.

From eq. (1): 
$$V_{jh} = \frac{M}{h_b}^0 = \frac{1562.6 * 12}{43} = 436.07 \text{ kips}$$

From eq. (3):  $b_{je} = \sqrt{2}D = 50.9$  in. >  $b_b = 45$  in. ; Use  $b_{je} = b_b = 45$  in.

From eq. (2): 
$$v_{jh} = \frac{V_{jh}}{b_{je}(h_c)} = \frac{436.07}{45(36)} = 269.18 \text{ psi.}$$

### **Vertical Axial Stress:**

From eq. (6):

$$f_v = \frac{P_c}{b_{ie}(h_c + h_b)} = \frac{520}{45(36 + 43)} = 146.27 \text{ psi.}$$

### Horizontal Stress:

$$f_h = 0 \text{ psi.}$$

$$p_{c} = \frac{f_{v} + f_{h}}{2} + \sqrt{\left(\frac{f_{v} - f_{h}}{2}\right)^{2} + v_{jh}^{2}} = \frac{146.27 + 0}{2} + \sqrt{\left(\frac{146.27 - 0}{2}\right)^{2} + 269.18^{2}}$$

 $p_c = 352.07 \text{ psi} \le 0.3(3000 \text{ psi}) = 900 \text{ psi } \textbf{O.K.}$ 

From eq. (8):

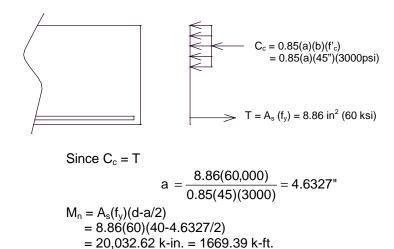
$$p_t = \frac{f_v + f_h}{2} - \sqrt{\left(\frac{f_v - f_h}{2}\right)^2 + {v_{jh}}^2} = \frac{146.27 + 0}{2} - \sqrt{\left(\frac{146.27 - 0}{2}\right)^2 + 269.18^2}$$

$$p_t = -205.80 \text{ psi } \ge 3.5\sqrt{3000} = 191.7 \text{ psi Not O.K.}$$

Since  $p_t$  is greater than  $3.5\sqrt{f_c^{'}}$ , special joint reinforcement based on eqs. (9) through (14) are needed.

Check if moment capacity of the beam is greater than the overstrength moment capacity of the column.

Neglect the effect of the compression steel (conservative).



Compare moment capacity of beam versus overstrength moment capacity of the column:

1669.39 k-ft. > 1562.60 k-ft.

Moment capacity of beam is greater than the overstrength moment capacity of the column. **O.K.** 

### Design of reinforcement for the beam-column joint

Vertical reinforcement should be placed throughout a distance of h<sub>b</sub>/2 from the column face on each side of the column.

New: April 2000

From eq.(9): 
$$A_{jv} = 0.125A_{sc} \frac{f_{yc}^{0}}{f_{yv}}$$
  
 $A_{sc} = 15.70 \text{ in}^{2}$   
 $f_{yc}^{0} = 1.1f_{y} = 66 \text{ ksi.}$   
 $f_{yv} = 60 \text{ ksi.}$   
 $A_{jv} = 0.125(15.70) \frac{66}{60} = 2.16 \text{ in}^{2}$ 

- Reinforcement within the joint confines:

From eq. (10): 
$$A_{vi} = 0.0625A_{sc} \frac{f_{yc}^{\circ}}{f_{yv}}$$
  
= 0.0625(15.70) $\frac{66}{60}$  = 1.08 in<sup>2</sup>

Additional bottom of beam longitudinal reinforcement:

From eq. (11): 
$$A_{sb} = 0.0625A_{sc} \frac{f_{yc}^0}{f_{yb}}$$
  
=  $0.0625(15.70) \frac{66}{60} = 1.08 \text{ in}^2$ 

This reinforcement must be developed at a distance  $h_b/2$  away from the face of the column.

- Hoop Reinforcement:

From eq. (13): 
$$\rho_s = \frac{0.3 A_{sc} f_{yc}^0}{L_a^2 f_{yh}}$$
 
$$L_a = 40 \text{ in.}$$
 
$$f_{yh} = 60 \text{ ksi}$$
 
$$\rho_s = \frac{0.3 (15.70)(66)}{40^2 (60)} = 0.003238$$
 
$$\rho_{s,min} = \frac{3.5 \sqrt{3000}}{60000} = 0.003195$$
 
$$\rho_s > \rho_{s,min} \therefore \textbf{use } \rho_s$$

use #4 hoop reinforcement

$$\begin{array}{l} A_s = 0.1963 \text{ in}^2 \\ D' = 36 - 2(2) - 4/8 = 31.5 \text{ "} \\ \rho_s = 0.003238 \end{array}$$

From eq. (15): 
$$S = \frac{4A_s}{D'\rho_s} = \frac{4(0.1963)}{31.5(0.003238)} = 7.70"$$
 spacing > 3" max. from

Figure 6.1.3.1.7-4 Therefore, **Use S = 3**"

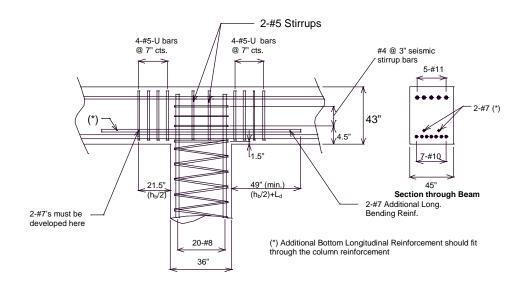


Figure 6.1.3.1.7-9 Summary of "T-Joint" Reinforcement

### Principal Tension and Compression Stresses in Column-Footing Joints

Column – Footing joints are essentially the same as inverted beam-column T joints. Eqs. (1) through (8) are applicable to column-footing joints except the beam height,  $h_b$ , shall be changed to the footing height,  $h_f$ .

### Design of Reinforcement for Column-Footing Joint

The design of the reinforcement for column-footing joints is similar to that for beam-column T joint. From a joint performance viewpoint, it is desirable to bend the column bars inward toward the joint by using 90° hook bars, but this will cause undue congestion. Bending column bars away from the joint will increase the diagonal tension stress within the joint region. However, it makes a stable platform for supporting the column cage and prevents congestion. When the column reinforcement is bent outward, eqs. (9) through (14) shall be applied. Since the column inelastic action may develop in directions other than parallel to one of the principal axes of the footing, the amount of vertical reinforcement in eq. (9) shall be placed in each of the four quadrant areas outside the joint. In other words, a total vertical stirrup area of:

$$A_{jv} = 0.5A_{sc} \frac{f_{yc}^{o}}{f_{vv}}$$
 (16)

shall be placed around the column.

Extra top reinforcement in the footing is also required in accordance with eq. (11). This reinforcement should pass through the column reinforcement or be placed as close as possible to the sides of the column and extend a distance of not less than  $I = 0.5^*D + L_d$ , where  $L_d$  is the bar development length, beyond the face on both sides of the column.

**Example 6.1.3.1.7-2:** A column is subjected to an axial load (due to dead and seismic loads) of 520 kips. The column diameter is 36 inches with 20-#8 bars for longitudinal reinforcement. All column reinforcement is bent outward into the footing away from the joint. The footing depth is 39 inches. The top and bottom reinforcement for the footing is shown in Figure 6.1.3.1.7-10. Design the reinforcement details for the column-footing joint.

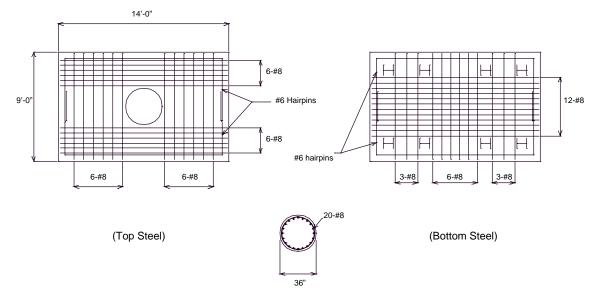
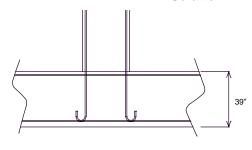


Figure 6.1.3.1.7-10 Details of Footing Reinforcement for Example 6.1.3.1.7-2

### Solution:



The axial load for the column = 520 kips. From Figure 6.1.3.1.7-8 in Example 6.1.3.1.7-1,  $M^0 = 1562.6 \text{ k-ft}$ .

From eq.(1): 
$$V_{jh} = \frac{M^0}{h_f} = \frac{1562.6(12)}{39} = 480.8 \text{ kips}$$

From eq. (3): 
$$b_{je} = \sqrt{2}D = \sqrt{2} \times 36" = 50.9"$$

From eq. (2): 
$$v_{jh} = \frac{V_{jh}}{b_{je}h_c} = \frac{480.8}{50.9(36)} = 262.39 \text{ psi.}$$

### Vertical Axial Stress:

From eq. (6):

$$f_v = \frac{P_c}{b_{ie}(h_c + h_f)} = \frac{520}{50.9(36 + 39)} = 136.21 psi.$$

### **Horizontal Axial Stress:**

$$f_h = 0$$
 psi.

### **Principal Stresses:**

From eq. (7):

$$p_{c} = \frac{f_{v} + f_{h}}{2} + \sqrt{\left(\frac{f_{v} - f_{h}}{2}\right)^{2} + v_{jh}^{2}} = \frac{136.21 + 0}{2} + \sqrt{\left(\frac{136.21 - 0}{2}\right)^{2} + 262.39^{2}}$$

$$= 339.19 \text{ psi.} \le 0.3(3000 \text{psi.}) = 900 \text{ psi.} \quad \textbf{O.K.}$$

From eq. (8):

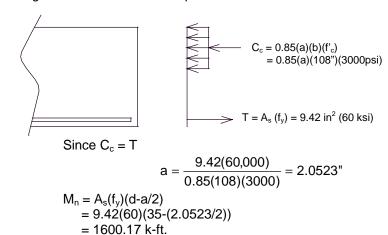
$$p_{t} = \frac{f_{v} + f_{h}}{2} - \sqrt{\left(\frac{f_{v} - f_{h}}{2}\right)^{2} + v_{jh}^{2}} = \frac{136.21 + 0}{2} - \sqrt{\left(\frac{136.21 - 0}{2}\right)^{2} + 262.39^{2}}$$
$$= -202.98 \text{ psi.} > 3.5\sqrt{3000} = 191.7 \text{ psi. Not O.K.}$$

Since  $p_t$  is greater than allowed, special joint reinforcement based on eqs. (9) through (14) are needed.

### Check moment capacity

Check the moment capacity of footing in the long direction to see if it is greater than the overstrength moment capacity of the column.

Neglect the effect of the compression reinforcement.



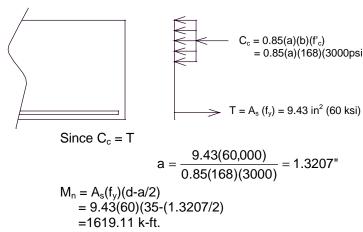
Compare moment capacity of footing overstrength moment capacity of the column:

1600.17 k-ft>1562.60 k-ft.

Moment capacity of the footing is greater than the overstrength moment of capacity of the column. **O.K.** 

Check the moment capacity of the footing in the short direction to see if it is greater than the overstrength moment capacity of the column.

Neglect the effect of the compression reinforcement.



Compare moment capacity of footing overstrength moment capacity of the column:

Moment capacity of the footing is greater than the overstrength moment of capacity of the column. **O.K.** 

### Design of reinforcement for the column-footing joint

- Vertical reinforcement should be placed throughout a distance of  $h_{\mbox{\scriptsize f}}/2$  from the column face on each side of the column.

From eq. (16): 
$$A_{jv} = 0.5A_{sc} \frac{f_{yc}^{0}}{f_{yv}}$$
  
 $A_{sc} = 15.71 \text{ in}^{2}$   
 $f_{yc}^{0} = 1.1f_{y} = 66 \text{ ksi.}$   
 $f_{yv} = 60 \text{ ksi.}$   
 $A_{jv} = 0.5(15.71) \frac{66}{60} = 8.641 \text{ in}^{2}$ 

- Reinforcement within the joint confines:

From eqs. (9),(10)&(16):

$$A_{vi} = 0.25A_{sc} \frac{f_{yc}^{o}}{f_{yv}}$$
$$= 0.25(15.71) \frac{66}{60} = 4.320 \text{ in}^{2}$$

- Additional top of footing longitudinal reinforcement:

$$A_{sb} = 0.0625A_{sc} \frac{f_{yc}^{o}}{f_{yf}}$$
$$= 0.0625(15.70) \frac{66}{60} = 1.08 \text{ in}^{2}$$

This reinforcement must be developed at a distance  $h_b/2$  away from the face of the column and must be placed so that the reinforcement goes through the column reinforcement.  $A_{sb}$  is required in both directions in the footing.

- Hoop Reinforcement:

Use 9" Spacing

From eq. (13): 
$$\rho_s = \frac{0.3 A_{sc} f_{yc}^o}{L_a^2 f_{yh}}$$

$$L_a = 35 \text{ in.}$$

$$f_{yh} = 60 \text{ ksi}$$

$$\rho_s = \frac{0.3(15.71)(66)}{35^2(60)} = 0.004232$$

$$\rho_{s,min} = \frac{3.5 \sqrt{3000}}{60000} = 0.003195 \qquad \rho_s > \rho_{s,min} \therefore \textbf{use } \rho_s$$
Use #5 hoop reinforcement
$$A_s = 0.3068$$

$$D' = 36-2(2)-5/8" = 31.375"$$

$$\rho_s = 0.004232$$
From eq. (15): 
$$S = \frac{4A_s}{D'\rho_s} = \frac{4(0.3068)}{31.375(0.004232)} = 9.24"$$

Note: By adding 3" to footing depth in this example problem, the principal tensile stress in the joint would have been less than the maximum allowed tensile stress, thus eliminating the need for the special joint reinforcement other than the minimum required reinforcement. However, the practice of increasing footing depth to eliminate the need for the special joint reinforcement should be limited to increasing the footing dept a maximum of 6 inches.

New: April 2000

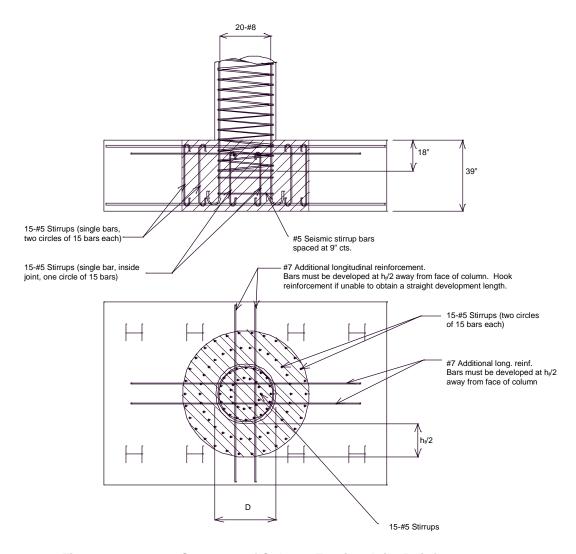


Figure 6.1.3.1.7-11 Summary of Column-Footing Joint Reinforcement

Revised: April 2001 SD002

## 3.2 - Abutment Component Design

After Iterative Abutment Design has shown that abutment forces and displacements are acceptable, and after connection design is completed, the abutment components may be designed.

## **Abutment Components**

### Wings (Integral OR Non-Integral Abutments)

- 1) Design the wing thickness for the applied shear on the wing. The design section is where the corner brace meets the inside edge of the wing. Use  $\phi = 1.0$  for shear. It is sometimes satisfactory to treat wing walls as fuse elements (i.e., broken off elements). This is mainly for integral abutment on very wide structures where large forces are drawn to the abutment. In this case, a second analysis with reduced stiffness in the transverse direction is required. Divide the wing up into two sections of f'c = 3 ksi and f'c = 4 ksi. Soil pressure acts below the bottom of the approach slab. See Bridge Manual Sections 3.76 or 3.77.
- 2) Design the flexural steel in the inside face of the wing (minimum #6 H bars @ 8" cts.) for the applied wing moment. Moment = (wing Area)\*(soil pressure)\*(arm from edge of corner brace to c.g. of wing area). The design section is where the corner brace meets the inside edge of the wing. Use φ = 1.0 for flexure. Divide the wing up into two sections of f'c = 3 ksi and f'c = 4 ksi. Soil pressure acts below the bottom of the approach slab. Position the wing reinforcement so that it does not interfere with girders or piles. The top of intermediate wings shall clear the bottom of the approach slab by a minimum of 3". See Bridge Manual Sections 3.76 or 3.77.

### Non-Integral Abutments

- 3) For non-integral abutments, check the stability under application of active soil pressure. Find the Mononobe-Okabe (combined seismic and non-seismic) pressure and the Rankine (non-seismic) pressure. For the stability and reinforcement computations for non-integral Abutment Design, the height of the soil force resultant could be obtained by assuming that the non-seismic resultant force by Rankine theory acts at H/3 from the bottom of the backwall, while the seismic resultant force should be taken to act at a height of 0.6H. H is defined as the height of the backwall. See AASHTO Div. I-A Commentary for a description of Mononobe-Okabe active seismic soil pressure computations.
- 4) Design non-integral bent backwalls for shear due to soil pressure on the fill face of the backwall. The design section is at the base of the backwall, just above the beam. Use  $\phi$  = 0.85 for shear, as in AASHTO 8.16.6.

- 5) Design non-integral bent backwalls for flexure due to soil pressure on the cantilevered backwall. The design section is at the base of the backwall, just above the beam. Use  $\phi = 0.90$  for flexure in AASHTO 8.16.3.
- 6) Design the backwall for flexure with the restrainers engaged (in tension) on the cantilevered backwall. In general, the soil pressure on the backwall can be neglected because it will be tensile when the restrainers are in tension, due to the separating motion of the superstructure. The design section is at the base of the backwall, just above the beam. Use  $\phi = 0.90$  for flexure in AASHTO 8.16.3.
- 7) Design the thickness of the backwall when restrainer anchor plates are present. For two-way shear (AASHTO 8.16.6), the design section is a rectangle surrounding the anchor plate. The design of anchor studs for restrainer anchor plates is described in Bridge Manual Section 6.1.3.1.3.

### **Deadman Anchors**

8) Design deadman anchors, if present, as in Bridge Manual Section 3.76, pp. 1.4-1 - 1.4-5, 2.4-1 and 3.2-1.

## 3.3- Intermediate Bent Design

### 3.3.1 - Column/Footing Intermediat Bents

## Column/Footing Intermediate Bents

### Analysis

- 1) From dynamic analysis, determine seismic (EQ) force and moment demands at top and bottom of columns. These full elastic (R=1) forces assume elastic response under seismic loads.
- 2) Determine dead load demands (DL) at top and bottom of columns.
- 3) Calculate magnified moment due to full elastic,  $M_{FE} = M_{DL} + \frac{M_{eq}}{(R=1)}$ ,

and modified elastic,  $M_{ME}=M_{DL}+\frac{M_{eq}}{(R=5)}$ , moments (including minimum moment from eccentricity) at top and bottom of columns. Second-order effects shall also be considered.

### Elastic Design, Without Plastic Hinging

4) Check the column (the size and reinforcement required for Groups I-VI is the minimum size column) using the full elastic (R=1) moments from Step (3) and  $\phi$ =0.75 to 0.9, as per AASHTO 8.16.1.2. Calculate 8 cases at 8 axial loads (P3max, P3min, P4max, P4min, at both top and bottom of each column):

For LC 1.0\*L + 0.3\*T: a) P3max = DL + EQ, b) P3min = DL - EQ For LC 0.3\*L + 1.0\*T: a) P4max = DL + EQ, b) P4min = DL - EQ If the column requires only a few bars to be designed elastically, then add a few bars rather than design the column for plastic hinging.

If  $UP/AP \ge 1.0$  (Ultimate moment over Applied resultant moment), then skip to Step (7) for no plastic hinging. Else, if UP/AP < 1.0, then perform Steps (5) and (6) first, considering plastic hinging.

### Plastic Design, With Hinging

- 5) If UP/AP < 1.0 in Step (4), then determine the column size and reinforcement required for modified elastic (R=5) moments using  $\varphi=0.5$  to 0.9 as per AASHTO Div. I-A, Section 7.6.2(B). The column design required for Groups I-VI loads is the minimum size. Generate the column P-M interaction capacity curve. Plot the 8 combinations of axial and modified elastic moment on the same graph. If all the points lie within the curve, then the design is sufficient. If not, add bars and re-plot the curve until all points barely lie within the curve.
- 6) Determine the overstrength ( $\phi$  = 1.3) plastic moment capacities of the column sized in step (5) as per AASHTO Div. I-A, Section 7.2.2. Use any non-linear push-over analysis program to determine the column overstrength moment, 1.3M<sub>p</sub>, at the bent failure mechanism stage. If a non-linear push-over analysis program is not available, any static analysis program can be used by designating the hinging locations at top and/or bottom of column,

use a joint release, then apply the overstrength plastic moment as a joint load.

### Column Shear

7) Check column shear reinforcement (spirals) as required in AASHTO Div. I-A, Section 6.6.2 & 7.6.2, which specifies the required reinforcement ratio.

$$\rho_s = \frac{A_s \pi (D_c - d_b)}{A_c(s)}$$
 = ratio of volume of provided spiral reinforcement to

total volume of concrete core, no units

A<sub>s</sub>= cross-sectional area of one leg of spiral, sq. in.

D<sub>c</sub>= diameter of spiral, out-to-out, inches

d<sub>b</sub>= bar diameter of spiral, inches

A<sub>c</sub>= area of core, out-to-out of spirals, sq. in.

s = spiral pitch or spacing, inches

For computation of shear demand, consider the possibility that hinging could occur between the top of the footing and the mud line, instead of at the column/footing junction. This situation could occur on footings with large overburdens and soils with high SPT blow counts, which could cause a shorter effective column length and a larger column shear demand.

### Footing Design

- 8) Design footings under Load Factor Design with  $\phi$ = 0.90 for flexure and  $\phi$ = 0.85 for shear, as per AASHTO 8.16.1.2.
  - Compare the moments from steps (4) and (6). If step (4) moments are lesser, then size the footings for the full elastic loads from step (4).

If step (6) moments are lesser, then size the footings for the overstrength plastic column moment capacities ( $M_{op}$ ) from step (6) in all directions of possible hinging: a) In-plane hinging at its corresponding axial load, b) Out-of-plane hinging at its corresponding axial load

- For spread footing pressure, keep resultants in the middle 2/3 of the footing.
- For the footing shear check, use Load Factor Design, with  $\phi = 0.85$ .
- For footing reinforcement design, use Load Factor Design, with φ = 0.90. For spread footings, design top steel for weight of footing + weight of soil. For pile footings, design the top of footing reinforcement for weight of footing + weight of soil + seismic pile tension. Check pile requirements in AASHTO Division I-A, Section 6.4.2 or 7.4.2.

### Beam Design

- 9) Design beams under Load Factor Design, with  $\phi$  = 0.90 for flexure and  $\phi$  = 0.85 for shear, as per AASHTO 8.16.1.2.
  - If the column design was OK (no hinging) under full elastic loads from Step (4), then consider dead loads and the seismic in-plane top-of-column shears and axial loads (for P-∆ effects) for the beam design.

# Seismic Design - Section 6.1

Page 3.3.1-3

Seismic Design Procedure

- If the column design was controlled by modified elastic loads (with plastic hinging) from Step (5), then consider dead loads and the overstrength (φ = 1.3) plastic moments from Step (6) for the beam design. In this case, designate the hinging location as a support, use a joint release, then apply the overstrength plastic moment as a joint load.
- For either elastic or plastic loads, design the beam for negative moments and for shear at faces of equivalent square columns, and design for maximum positive moments in between columns.

## T-Joint Connection Design

10) Check the beam/column T-joint stresses and the column/footing T-joint stresses as described in Section 6.1.3.1.7

#### 3.3.2 - Pile Cap Intermediate Bents

#### **Definitions of Terms**

In AASHTO Div. I-A Sections 6 & 7, some AASHTO terms are different from MoDOT terms. AASHTO's "pile caps" are caps of pile footings or beam caps of pile bents, and are considered "foundations". AASHTO's "pile bents" are what MoDOT calls pile cap intermediate bents, and piles on pile bents are treated as columns, not as "foundations". MoDOT's CIP piles are considered in AASHTO both as "concrete-filled pipe piles" and as "Cast-in-Place concrete piles" with the shell considered as both longitudinal reinforcement and as shear reinforcement.

AASHTO LRFD Specs., 5.10.11.4.1c&d&e, 5.13.4.5, 5.13.4.6 AASHTO Division I, 4.5.17.4

For drilled shafts and piles, a plastic hinge developed above the ground line is allowed for trestle piles (at intermediate bents), but not for foundation piles (below the ground line). "Trestle" and "foundation" piles are as defined in Bridge Manual Section 3.74, page 1.2.2.

## Analysis of Bent

- 1) Model the bent according to Sections 6.1.2.8.1 or 6.1.2.8.2.
- 2) From dynamic analysis, determine seismic (EQ) axial, moment and shear force demands of the piles. These full elastic (R=1) forces assume elastic response under seismic loads.
- Determine dead load (DL) axial, moment and shear force demands 3) of the piles.

## Elastic Design, Without Hinging

The minimum pile size and reinforcement is that which was required 4) for Groups I-VI. Check the minimum pile size using the full elastic (R=1) moments from Step (2) and  $\phi$  = 0.75 to 0.9, as per AASHTO 8.16.1.2. Analyze the pile for axial / moment (P-M) interaction capacity for CIP piles. Steel piles are analyzed for buckling and for combined stresses as described in the following references.

# AASHTO Div. I-A,7.5.2 & AASHTO Div. I, 10.36&10.54

Analyze the pile at 4 axial loads (P3max, P3min, P4max, and P4min): For LC  $1.0^*L + 0.3^*T$ : a) P3max = DL + EQ, b) P3min = DL - EQFor LC 0.3\*L + 1.0\*T: a) P4max = DL + EQ, b) P4min = DL - EQ The shell of CIP piles provides shear reinforcement and longitudinal flexural reinforcement (see equations below). See Bridge Manual Section 3.74, page 1.2.4 for the design thickness of the shell. If UP/AP  $\geq$  1.0, or if UP/AP  $\geq$ 1.0 by adding only a few bars, then skip to Step (8) for no hinging. Else, if UP/AP < 1.0 or if it takes too many added bars to increase UP/AP to more than 1.0, then perform Steps (5) or (6) first, considering plastic hinging.

#### Plastic Design, With Hinging

If UP/AP < 1.0 for pile above the ground line in Step (4), then 5) determine the pile size and reinforcement required for modified elastic (R=3 for vertical piles only and R=2 for one or more battered piles) moments using  $\phi = 0.5$  to 0.9 as described in AASHTO Div. I-A, Section 7.6.2(B). The pile design required for Groups I-VI loads

should be the minimum design. Generate the pile P-M interaction curve. For steel HP piles, combined stresses are computed as described in Section 6.1.2.10.2. Plot the 4 points of axial and modified elastic moment on the same graph. If all the points lie within the curve, then the design is sufficient. If not, add bars or use a larger pile size, and re-plot the capacity curve until all points barely lie within the curve. Use R=1 to design pile under the ground line.

- 6) If a non-linear push-over analysis program is available, determine the plastic hinge locations based on the horizontal bent displacements from the seismic analysis. If any plastic hinges occurred below the ground line, redesign the bent by increasing the total number of pile or pile size, etc.
- 7) The end regions of concrete piles should be reinforced for plastic hinging. Refer to Figure 6.1.3.3.2-1 for the following terms.

A =the greater of (D/2 or 15")

B =the greater of (2\*D or H/6 or 24")

D = the pile diameter, in inches

G = A + B = the length of the upper plastic hinging region, in inches

H = the pile clear height, from bottom of beam to mud line, inches

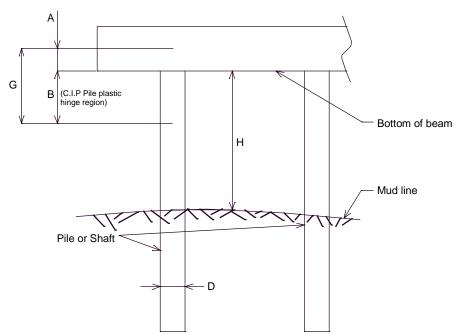


Figure 6.1.3.3.2-1 C.I.P. Pile Plastic Hinge Region

AASHTO Div. I-A, 7.6.2(D) specifies the reinforcement ratio required, and the provided reinforcement ratio is given by: Shells of CIP Piles:

Provided  $\rho = \frac{4t}{D}$  = the ratio of volume of reinforcement provided by

the shell to the total volume of the concrete core, no units.

Where: t = Shell thickness

D = Core Diameter

Spirals:

Provided 
$$\rho_s = \frac{A_s \pi (D_c - d_b)}{A_c(s)}$$
 = the ratio of volume of reinforcement

provided by the spiral to the total volume of the concrete core, no units.

$$A_s = \frac{\pi * D_c^2}{4}$$
 = cross-sectional area of one leg of spiral, sq. in.

Where: D<sub>C</sub>= diameter of spiral, out-to-out, inches

d<sub>b</sub>= bar diameter of spiral, inches

A<sub>c</sub>= area of core, out-to-out of spirals, sq. in.

s = spiral pitch or spacing, inches

Steel piles shall be provided with shear connector angles for anchorage.

AASHTO Div. I-A, 7.4.2(C) & Bridge Manual Section 3.72, 4.6 & 5.5

#### Beam Design

8) Design beams under Load Factor Design, with  $\phi$ = 0.90. If the pile design was OK (no hinging) under full elastic loads from Step (4), then consider dead loads and the seismic in-plane top-of-column shears and axial loads (for  $P-\Delta$  effects) for the beam design. If the column design was controlled by modified elastic loads (hinging) from Steps (5) or (6), then apply dead loads and the overstrength (6) = 1.3) plastic moments from Steps (5) or (6). For either elastic or plastic loads, design the beam for the negative moments at faces of equivalent square piles and for the maximum positive moments in between piles. Check shear in the beam at the faces of the equivalent square piles. Minimum beam width shall be as per Bridge Manual Section 3.72, but should also provide 6" concrete cover outside piles as per AASHTO Div. I Section 4.5.15.2. Note that for 20" and 24" CIP piles, the standard 30" integral end bent beam width must be enlarged to 32" and 36", respectively.

## T-Joint Connection Design

 Check the beam/pile T-joint stresses as described in Section 6.1.3.1.7.

#### 3.3.3 - Drilled Shaft Intermediate Bents

# **Drilled Shaft Intermediate Bents**

Drilled shafts (also called "Pedestal Piles") are described in Bridge Manual Section 3.52.3.9. In the following discussion, the portion of the pedestal pile above ground will be referred to as the "column". The portion of the pedestal pile below ground will be referred to as the "shaft". Most drilled shafts have a shaft diameter larger than the column diameter, as shown below in Figure 6.1.3.3.3-1. Drilled shafts are drilled or augered in, whereas piles are driven into place.

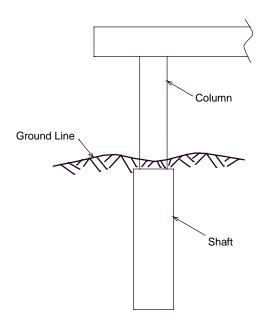


Figure 6.1.3.3.3-1 Drilled Shaft (Pedestal Pile) Int. Bent

The following discussion of drilled shafts assumes that the pile diameter is larger than the column diameter. The column portion is allowed to plastic hinge, but the shaft portion is not allowed to hinge.

Sometimes, there is an enlarged bell at the bottom when required for bearing pressure. Bridge Manual Section 3.52.3.9 allows this bell only in SPC A, but unusual situations might require a bell in other Seismic Performance Categories. If a bell is required in SPC B, C or D, then reinforcement should be provided around the outside of the bell, in order to prevent local crushing of the bell.

Drilled shafts with no bell are socketed into rock a minimum distance of 1.5 times the shaft diameter and are considered fixed at the rock line. Drilled shafts with a bell are considered pinned at the rock line.

## Analysis of Bent

- 1) Model the bent according to Sections 6.1.2.8.1 and 6.1.2.8.2.
- 2) From the dynamic analysis, determine seismic (EQ) axial, moment and shear force demands at "top of column" (near the beam/column joint) and at "bottom of column" (near the column/shaft joint). These full elastic (R=1) forces assume elastic response under seismic loads.
- 3) Determine dead load (DL) axial, moment and shear force demands at "top of column" and at "bottom of column".
- 4) Plastic hinging of the column portion of a drilled shaft is allowed for trestle piles (intermediate bents), but not for foundation piles (end bents), as defined in Section 3.74, page 1.2.2. The shaft portion of a drilled shaft is considered a "foundation" in AASHTO Div. I-A, 7.2.1(B), so plastic hinging of the shaft portion of a drilled shaft is not allowed. Calculate the full elastic [ $M_{FE} = M_{DL} + \frac{M_{EQ}}{(R=1)}$ ] moments at all tenth-points of the entire column & shaft, and calculate the modified elastic [ $M_{ME} = M_{DL} + \frac{M_{EQ}}{(R=5)}$ ] moments at tenth-points of the column portion.

## Column Design, Without Hinging

5) Check the column portion and shaft portion (the minimum size and reinforcement is that which was required for Groups I-VI) using the full elastic (R=1) moments from Step 5 and φ=0.75 to 0.9, as per AASHTO 8.16.1.2. Analyze the column and shaft for axial / moment (P-M) interaction capacity. Analyze the column at 8 axial loads (P3max, P3min, P4max, and P4min, top and bottom): For LC 1.0\*L + 0.3\*T, a) P3max = DL + EQ, b) P3min = DL - EQ For LC 0.3\*L + 1.0\*T, a) P4max = DL + EQ, b) P4min = DL - EQ If UP/AP ≥ 1.0 or if UP/AP ≥ 1.0 by adding only a few bars, then skip to Step (8) for no hinging. Else, if UP/AP < 1.0 or if too many bars must be added, then perform Steps (6) and (7) first, for column plastic hinging.

# Plastic Column Design, With Hinging

If UP/AP < 1.0 in Step (4), then the column portion is designed for modified elastic moments (R=5), and the shaft portion is designed as a foundation (R=1). Determine the column size and reinforcement required for modified elastic (R=5) moments using  $\varphi=0.5$  to 0.9 as described in AASHTO Div. I-A, Section 7.6.2(B), with the column design required for Groups I-VI loads as the minimum. Generate the column P-M interaction curve for drilled shafts. Plot the combinations (as in Step (5) above) of axial and modified elastic moment on the same graph for all 8 points on the column portion. If all the points lie within the curve, then the column design is sufficient. If not, add bars and re-plot the capacity curve until all points barely lie within the curve.

7) The end regions of columns should be reinforced for plastic hinging. The end region length at either end of the column is the larger of (two times the column diameter, one-sixth of the clear height of the column, and 24 inches). The spiral at the bottom end of the column shall continue into the shaft for a distance equal to the greater of (half the column diameter or 15 inches).

AASHTO Div. I-A, 7.2.2(B), Step 2

Design column shear reinforcement (spirals) for the required reinforcement ratio described in the reference below.

AASHTO Div. I-A, Section 7.4.2 & 7.6.2

For the provided reinforcement ratio of spirals:

Prov'd 
$$\rho_s = \frac{A_s \pi (D_c - d_b)}{A_c(s)}$$
 = the ratio of volume of provided

spiral reinforcement to total volume of concrete core, no units.

Where:

A<sub>s</sub>= cross-sectional area of one leg of spiral, sq. in.

D<sub>c</sub>= diameter of spiral, out-to-out, inches

d<sub>b</sub>= bar diameter of spiral, inches

A<sub>c</sub>= area of core, out-to-out of spirals, sq. in.

s = spiral pitch or spacing, inches

# Shaft Design

8) The design moments for the shaft shall be the lesser of the full elastic moments (R=1) from Step (5) and the overstrength plastic moment capacity ( $\phi = 1.3$ ) of the column sized in step (6).

AASHTO Div. I-A, Section 7.2.1(B) & 7.2.2 & 7.2.6

#### Beam Design

9) Design the beam under Load Factor Design, with a flexural  $\phi$ = 0.90 and a shear  $\phi$ = 0.85. If the column design was OK (no hinging) under full elastic loads from Step (5), then apply dead loads and the seismic in-plane top-of-column shears and axial loads for the beam design. If the column design was controlled by modified elastic loads (hinging) from Step (6), then apply dead loads and the overstrength ( $\phi$  = 1.3) plastic moments from Step (6). For either elastic or plastic loads, design the beam for the negative moments at faces of equivalent square columns and for the maximum positive moments in between columns. Check shear in beams according to hinging or no hinging.

#### T-Joint Connection Design

10) Check the beam/column T-joint stresses as described in Bridge Manual Section 6.1.3.1.7.

## 3.3.4 - Integral Intermediate Bents

# Integral Intermediate Bents

The difference between a standard intermediate bent and an integral intermediate bent is shown in Figure 6.1.3.3.3-1.

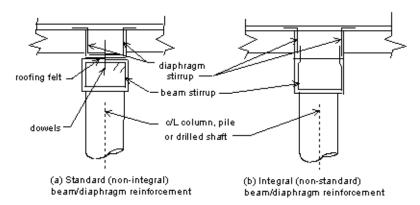


Figure 6.1.3.3.4-1 Difference Between Standard and Integral Diaphragms

On standard intermediate bents, the beam stirrups are completely contained within the beam, and a line of dowels creates only a "pinned" connection with the diaphragm and superstructure. Due to the roofing felt and the dowels, the "pinned" connection theoretically does not transfer moments between the superstructure and the substructure. A standard (non-integral) intermediate bent therefore exhibits single-curvature bending out of the plane of the bent. In-plane bending is double-curvature due to the moment connections between beam and columns or between beam and piles.

On an integral intermediate bent (non-standard), the beam stirrups extend up into the diaphragm (similar to standard integral end bents), making a "fixed" connection which can transfer moments between the superstructure and the substructure. This fixed connection makes the integral intermediate bent exhibit double-curvature bending out of the plane of the bent. In-plane bending is also double-curvature due to the moment connections between beam and columns or beam and piles.

#### When to Use Integral Intermediate Bents

- 1) When  $\frac{KL}{R}$  > 100 for piles or drilled shafts and a larger diameter member is not acceptable. This situation can be improved by making the intermediate bent integral, causing double-curvature out-of-plane bending (K=1.2) instead of single-curvature out-of-plane bending (K=2.0), thus reducing  $\frac{KL}{R}$ .
- 2) When the percentage of the total seismic force at the end bents is so high that other remedial actions are ineffective (see Section 6.1.2.10). This situation can be improved by making the intermediate bents integral, which makes them stiffer and helps to distribute some of the excessive force from the end bents to the intermediate bents.
- 3) Sometimes, making the bent integral can help to stiffen up the entire bridge, decrease the period, and may improve the situation.

# 3.4 - Cross Frame Analysis and Design

Recent earthquakes indicate that many steel bridges have suffered cross frame damage. Cross frames provide an important load path for the seismic force acting on slab-on-girder steel bridges. Cross frames shall be able to transmit all lateral forces from the superstructure to the bearings. The lateral seismic force at an individual bent calculated from the seismic analysis shall be proportionally distributed to the individual cross frames over the bent.

For details of cross frames, see Bridge Manual Section 3.42. The components of cross frames including top and bottom chords and diagonal angle members shall be designed based on allowable stress design with consideration of the eccentric axial load and buckling stresses. Welding sizes at gusset plate connection shall also be designed for the seismic load. Cross frames shall remain elastic when subjected to the seismic force.

The following cross frame model may be used for the structural analysis of cross frames:

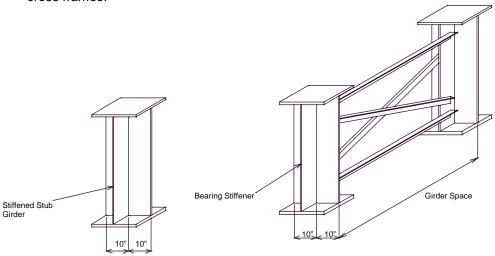


Figure 6.1.3.4-1 Cross Frame Model (S.M. Zahrai & M. Bruneau, 1999)

Study (S.M. Zahrai and M. Bruneau, 1999) has shown that bearing stiffeners provide the main stiffness for girders; in other words, using a longer length of girder (greater than 20 inches) in the model in Figure 6.1.3.4-1 results in no significant difference in model stiffness. Based on the cross frame model in Figure 6.1.3.4-1, the following structural analysis model can be considered:

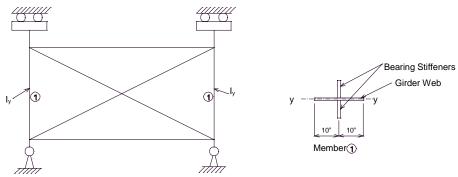


Figure 6.1.3.4-2 Structural Model for Cross Frames

In Figure 6.1.3.4-2,  $I_y$  = moment of inertia of the stiffened stub girder (mainly due to the bearing stiffeners) in the lateral direction (i.e. y-y direction). The above model assumes full fixity at the concrete deck and zero fixity at the flexible bearings such as elastomeric bearings.

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# 4.1 - References

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